

Lecture 12

2024/2025

Microwave Devices and Circuits for Radiocommunications

2024/2025

- 2C/1L, **MDCR**
- Attendance at minimum 7 sessions (course or laboratory)
- Lectures- **associate professor Radu Damian**
 - Tuesday 16-18, ~~Online~~, P8
 - E – 50% final grade
 - problems + (2p atten. lect.) + (3 tests) + (bonus activity)
 - first test L1: 20-27.02.2024 (t2 and t3 not announced, lecture)
 - 3att.=+0.5p
 - all materials/equipments authorized

2024/2025

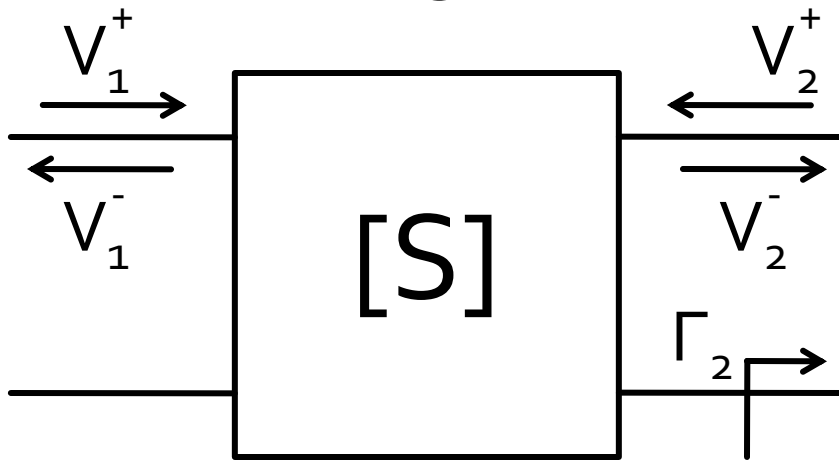
- Laboratory – **associate professor Radu Damian**
 - Tuesday 10-12, Il.13 / (even weeks)
 - L – 25% final grade
 - ADS, 4 sessions
 - Attendance + **personal results**
 - P – 25% final grade
 - ADS, 3 sessions (-1? 25.02.2025)
 - personal homework

General theory

Microwave Network Analysis

Scattering matrix – S

- Scattering parameters



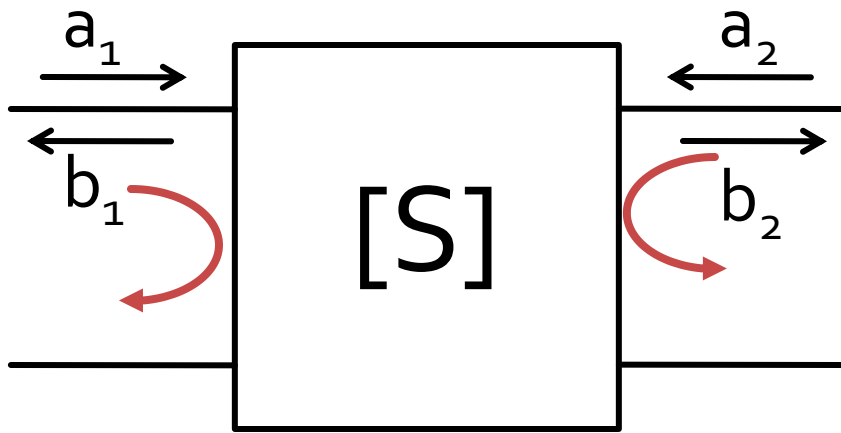
$$\begin{bmatrix} V_1^- \\ V_2^- \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \cdot \begin{bmatrix} V_1^+ \\ V_2^+ \end{bmatrix}$$

$$S_{11} = \left. \frac{V_1^-}{V_1^+} \right|_{V_2^+ = 0} \quad S_{21} = \left. \frac{V_2^-}{V_1^+} \right|_{V_2^+ = 0}$$

- $V_2^+ = 0$ meaning: port 2 is terminated in matched load to avoid reflections towards the port

$$\Gamma_2 = 0 \rightarrow V_2^+ = 0$$

Scattering matrix – S

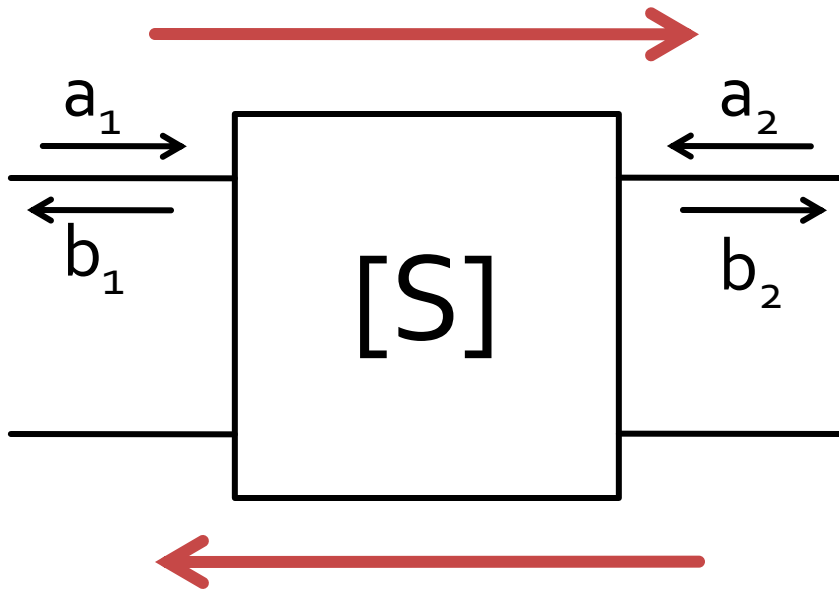


$$\begin{bmatrix} b_1 \\ b_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \cdot \begin{bmatrix} a_1 \\ a_2 \end{bmatrix}$$

$$S_{11} = \left. \frac{b_1}{a_1} \right|_{a_2=0} \quad S_{22} = \left. \frac{b_2}{a_2} \right|_{a_1=0}$$

- S_{11} and S_{22} are reflection coefficients at ports 1 and 2 when the other port is matched

Scattering matrix – S

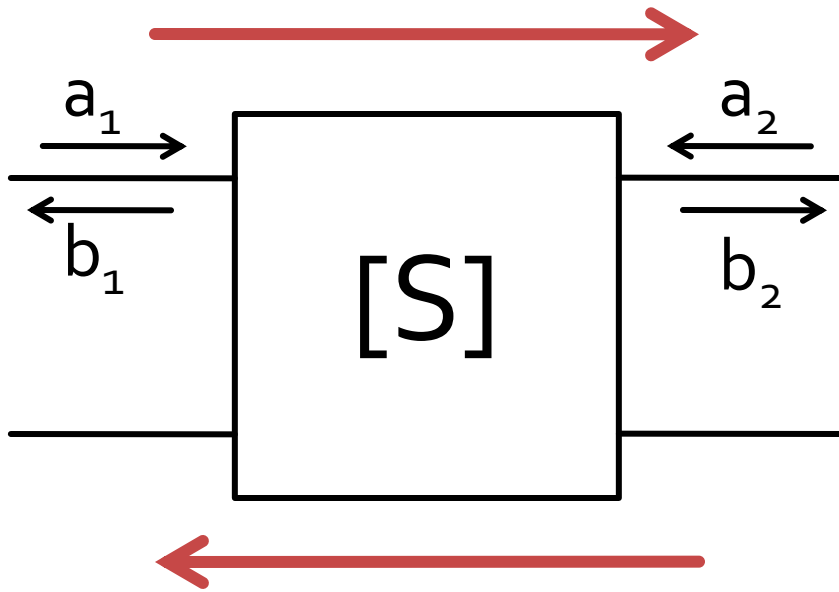


$$\begin{bmatrix} b_1 \\ b_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \cdot \begin{bmatrix} a_1 \\ a_2 \end{bmatrix}$$

$$S_{21} = \left. \frac{b_2}{a_1} \right|_{a_2=0} \quad S_{12} = \left. \frac{b_1}{a_2} \right|_{a_1=0}$$

- S_{21} si S_{12} are signal amplitude gain when the other port is matched

Scattering matrix – S



$$\begin{bmatrix} b_1 \\ b_2 \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \cdot \begin{bmatrix} a_1 \\ a_2 \end{bmatrix}$$

$$|S_{21}|^2 = \frac{\text{Power in } Z_0 \text{ load}}{\text{Power from } Z_0 \text{ source}}$$

- a, b
 - information about signal power **AND** signal phase
- S_{ij}
 - network effect (gain) over signal power **including** phase information

Impedance Matching

The Smith Chart

Course Topics

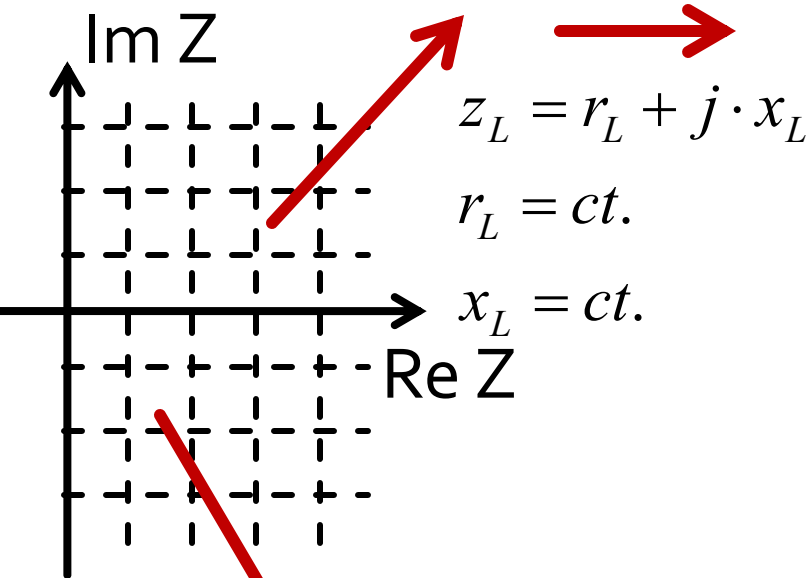
- Transmission lines
 - Impedance matching and tuning
 - Directional couplers
 - Power dividers
 - Microwave amplifier design
 - Microwave filters
 - ~~■ Oscillators and mixers?~~
- 

The image shows a standard Smith Chart used in electrical engineering for impedance calculations. The chart is a circular grid with the following features:

- Outer Scales:**
 - Top: SWR (Standing Wave Ratio) scale from 1.0 to infinity.
 - Bottom: dBS (Return Loss) scale from infinity down to 0.
 - Left: Reflection Coefficient (V) scale from 0 to 1.0.
 - Right: Reflection Coefficient (P) scale from 0 to 1.0.
- Inner Scales:**
 - Top: SWR (Standing Wave Ratio) scale from 1.0 to infinity.
 - Bottom: dBS (Return Loss) scale from infinity down to 0.
 - Left: Reflection Coefficient (V) scale from 0 to 1.0.
 - Right: Reflection Coefficient (P) scale from 0 to 1.0.
- Main Chart:**
 - A circular grid with radial lines for constant SWR and concentric circles for constant dBS.
 - Radial lines are labeled with SWR values (1.0, 1.5, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0, 9.0, 10.0, 15.0, 20.0, 30.0, 40.0, 50.0, 60.0, 70.0, 80.0, 90.0, 100.0).
 - Concentric circles are labeled with dBS values (0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.0, 1.2, 1.5, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0, 9.0, 10.0, 15.0, 20.0, 30.0, 40.0, 50.0, 60.0, 70.0, 80.0, 90.0, 100.0).
 - The chart is divided into four quadrants by a horizontal line (labeled 'TOWARD LOAD' on the left and 'TOWARD GENERATOR' on the right) and a vertical line (labeled 'TOWARD GENERATOR' on the left and 'TOWARD LOAD' on the right).
- Labels:**
 - Top: SWR (Standing Wave Ratio)
 - Bottom: dBS (Return Loss)
 - Left: Reflection Coefficient (V)
 - Right: Reflection Coefficient (P)
 - Center: TOWARD LOAD (left) and TOWARD GENERATOR (right)

The Smith Chart

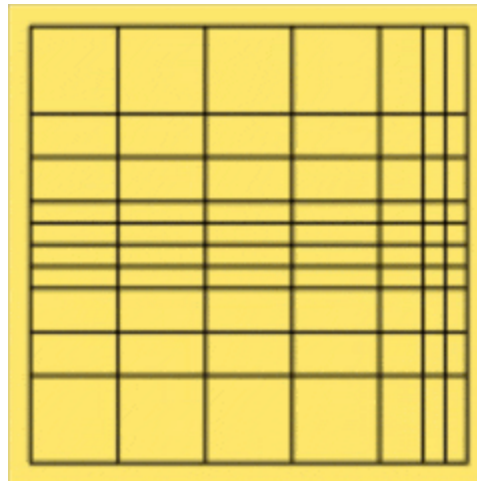
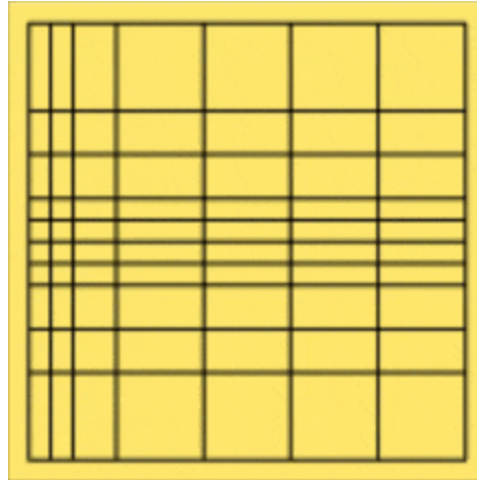
$$\Gamma = \frac{Z_L - Z_0}{Z_L + Z_0} = \frac{z_L - 1}{z_L + 1}$$



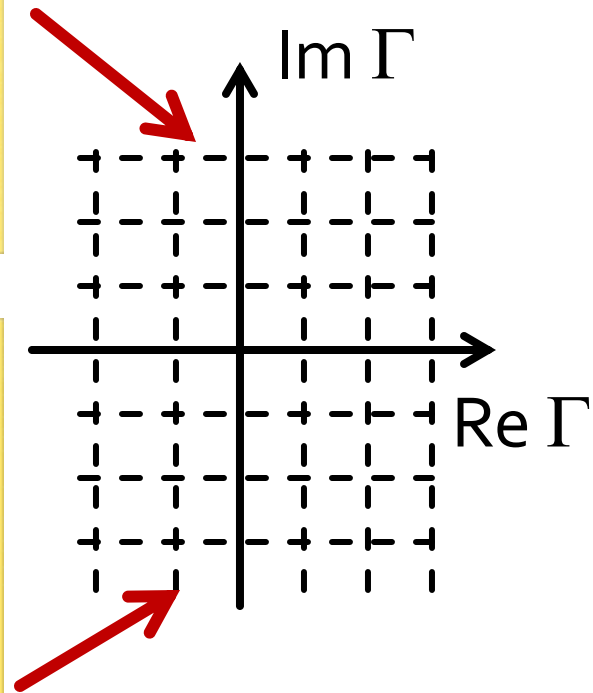
$$z_L = r_L + j \cdot x_L$$

$$r_L = ct.$$

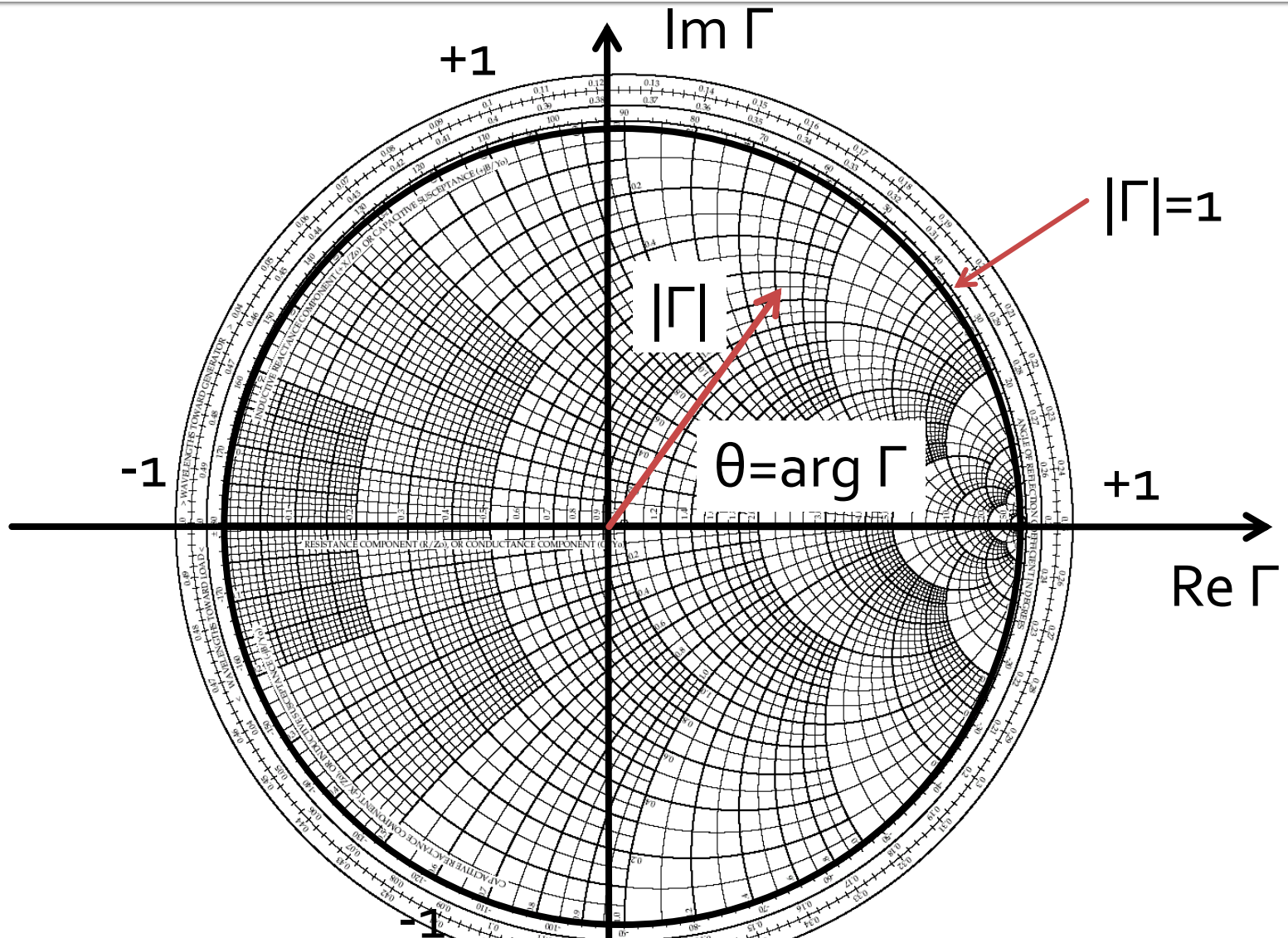
$$x_L = ct.$$



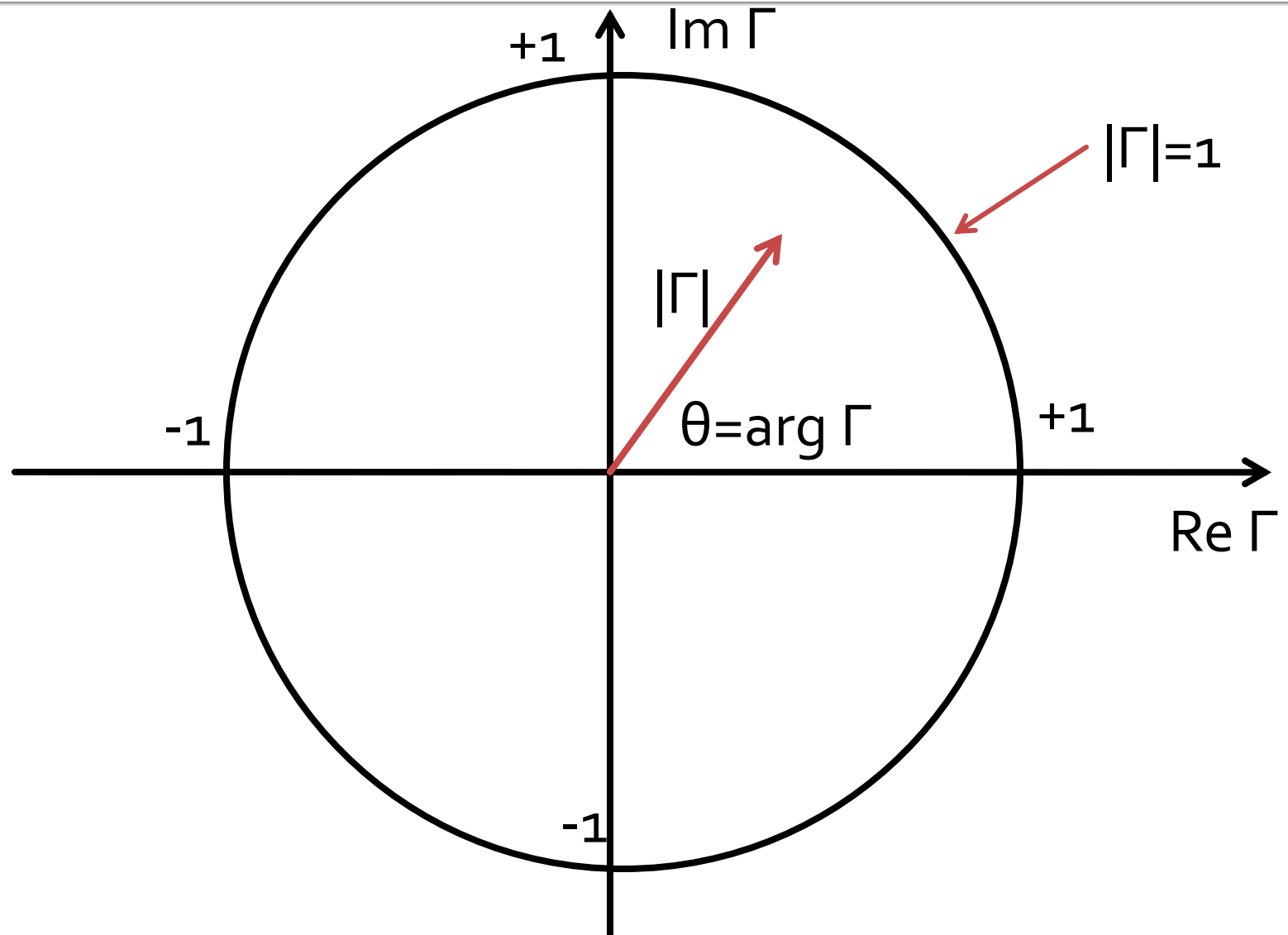
$$\Gamma = \frac{Z_L - Z_0}{Z_L + Z_0} = \frac{Y_0 - Y_L}{Y_0 + Y_L} = \frac{1 - y_L}{1 + y_L}$$



The Smith Chart



The Smith Chart



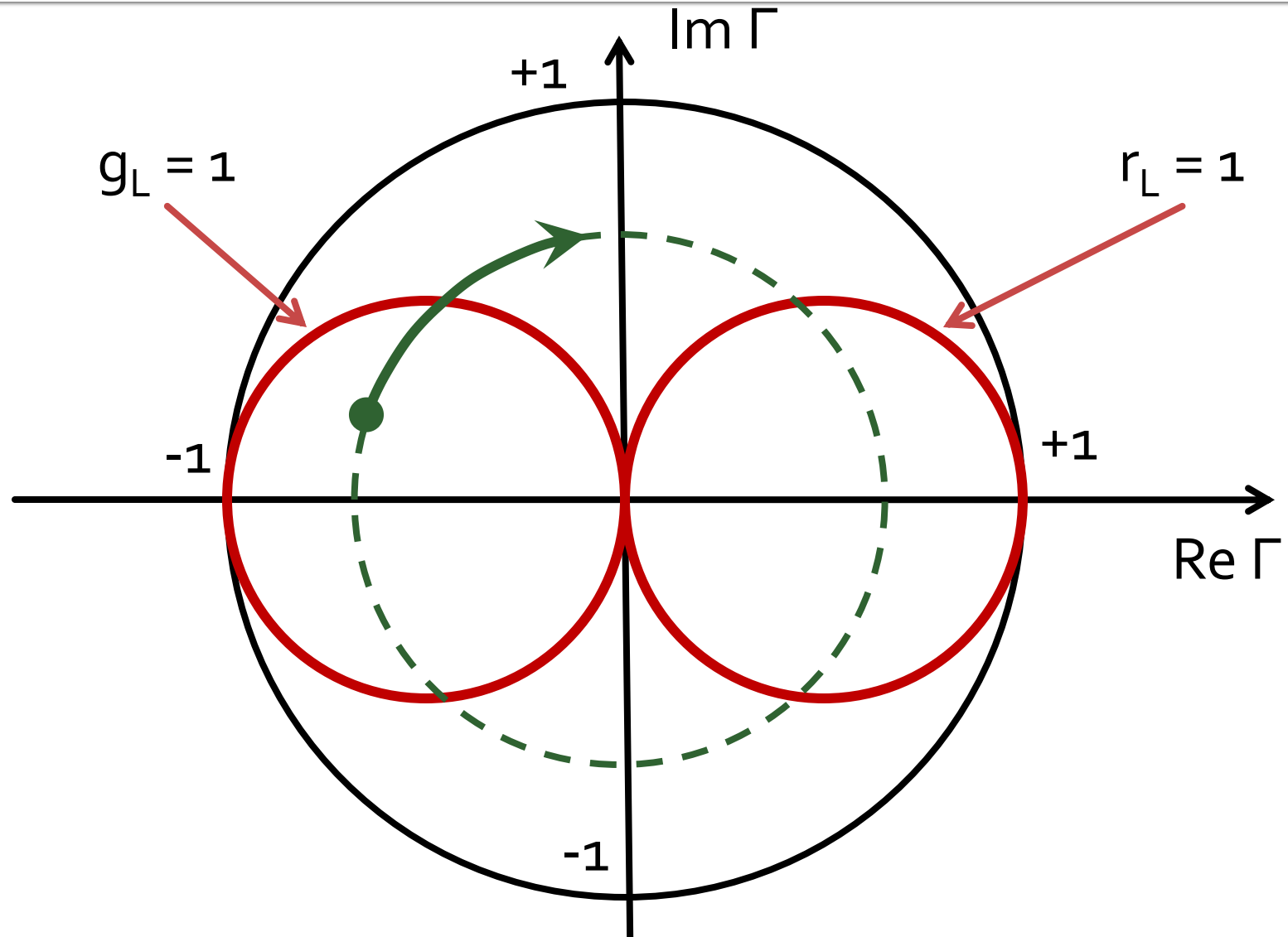
Impedance Matching

Impedance Matching with Stubs

Course Topics

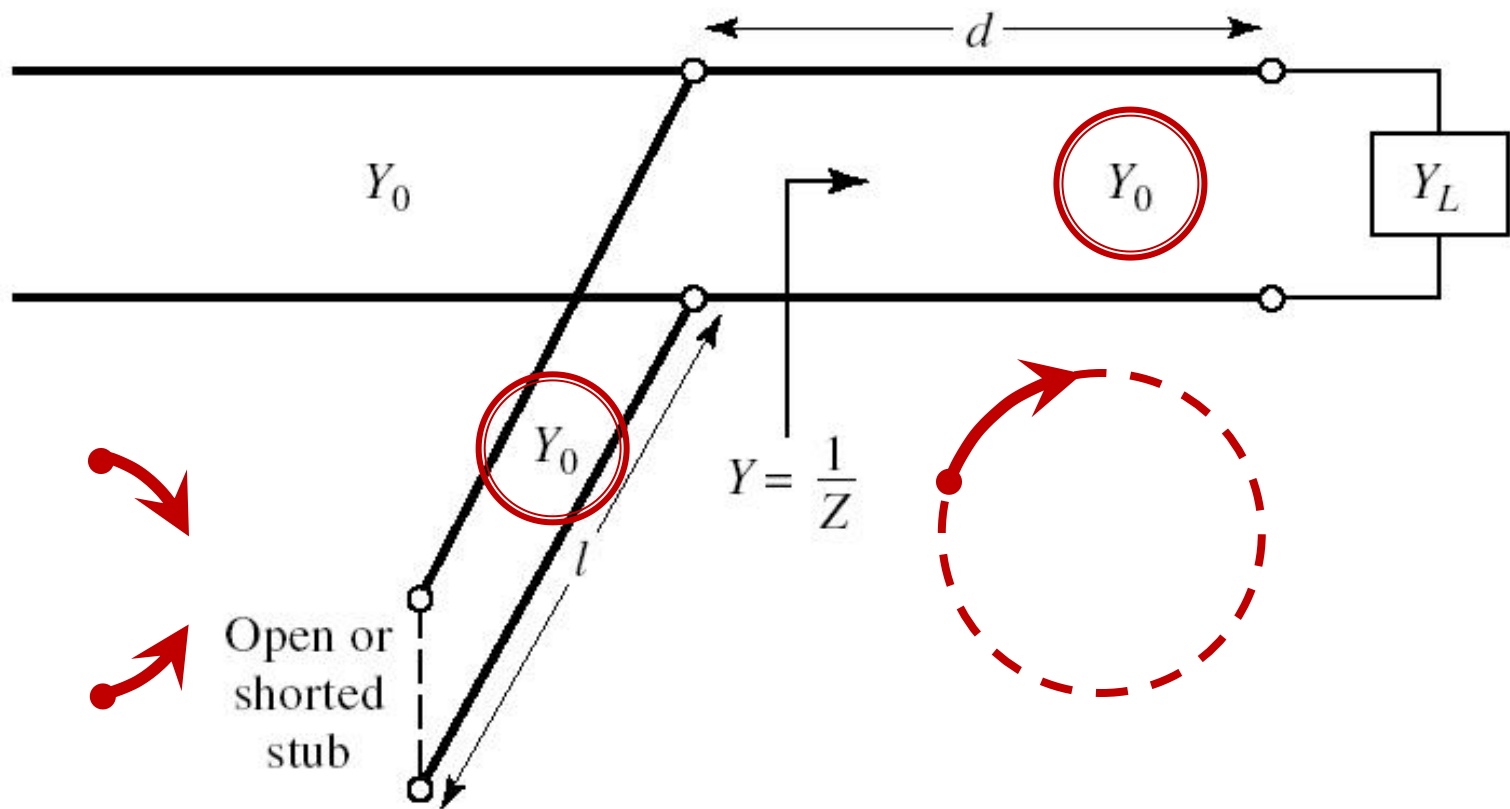
- Transmission lines
- Impedance matching and tuning
- Directional couplers
- Power dividers
- Microwave amplifier design
- Microwave filters
- ~~Oscillators and mixers?~~

Smith chart, $r=1$ and $g=1$



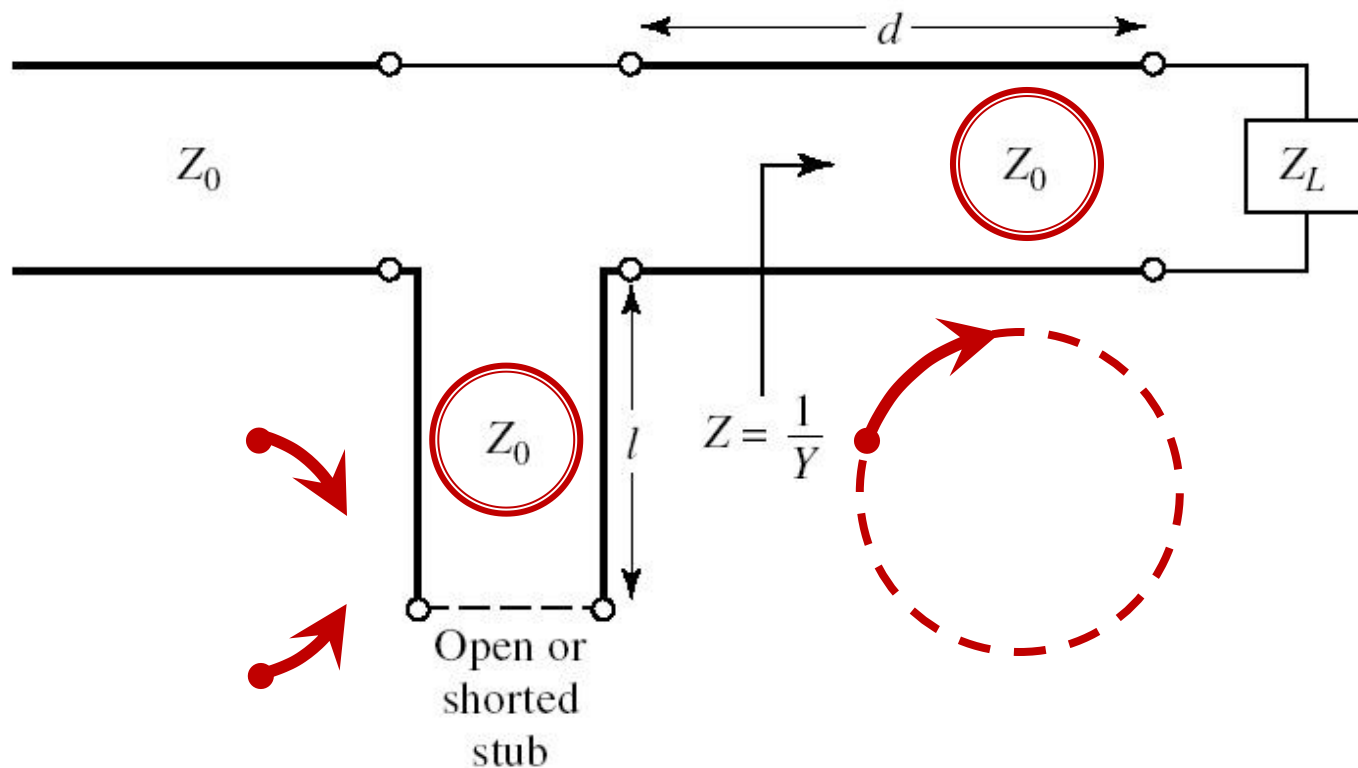
Single stub tuning

- Shunt Stub



Single stub tuning

- Series Stub
- difficult to realize in single conductor line technologies (microstrip)

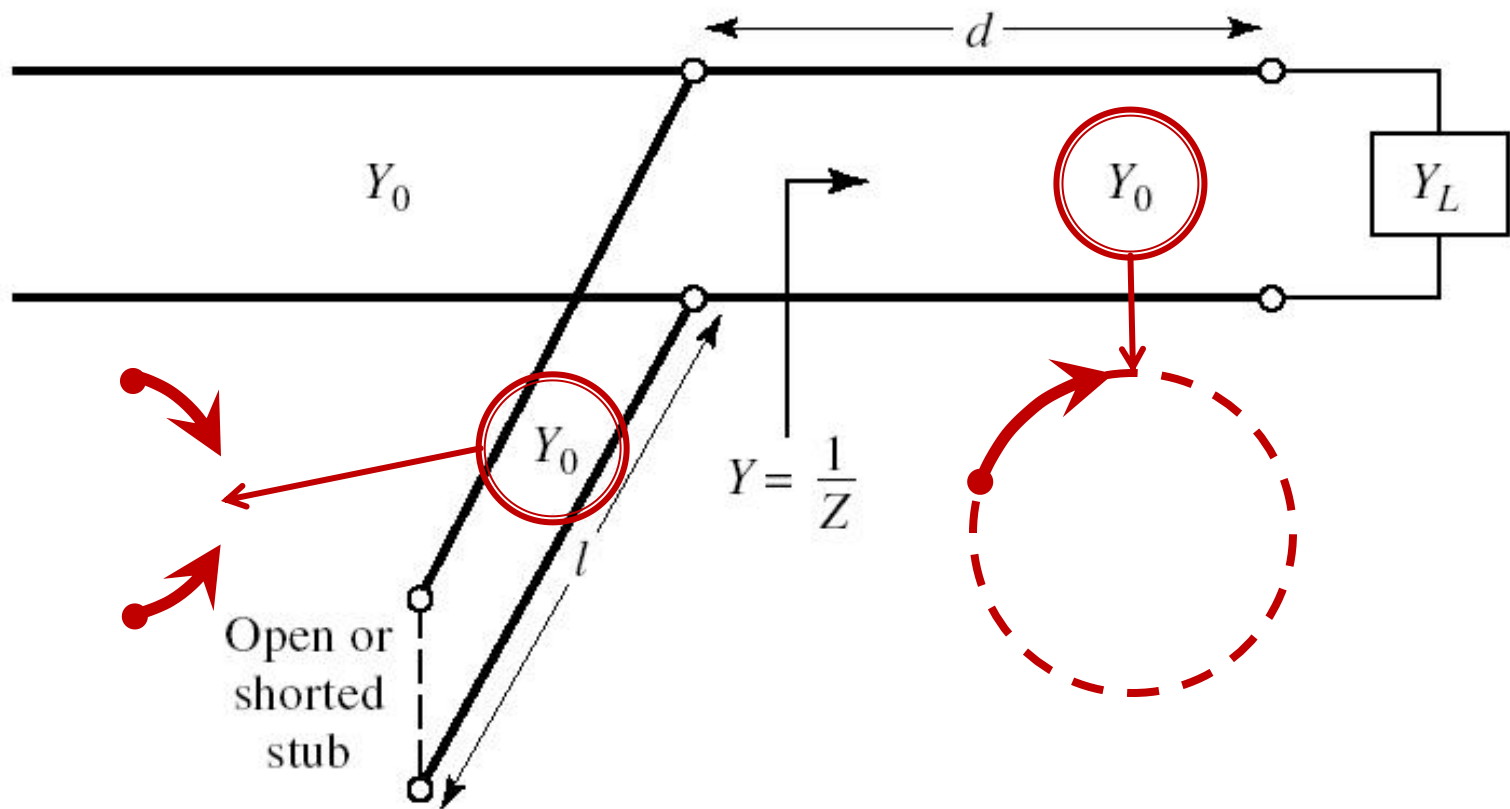


Analytical solutions

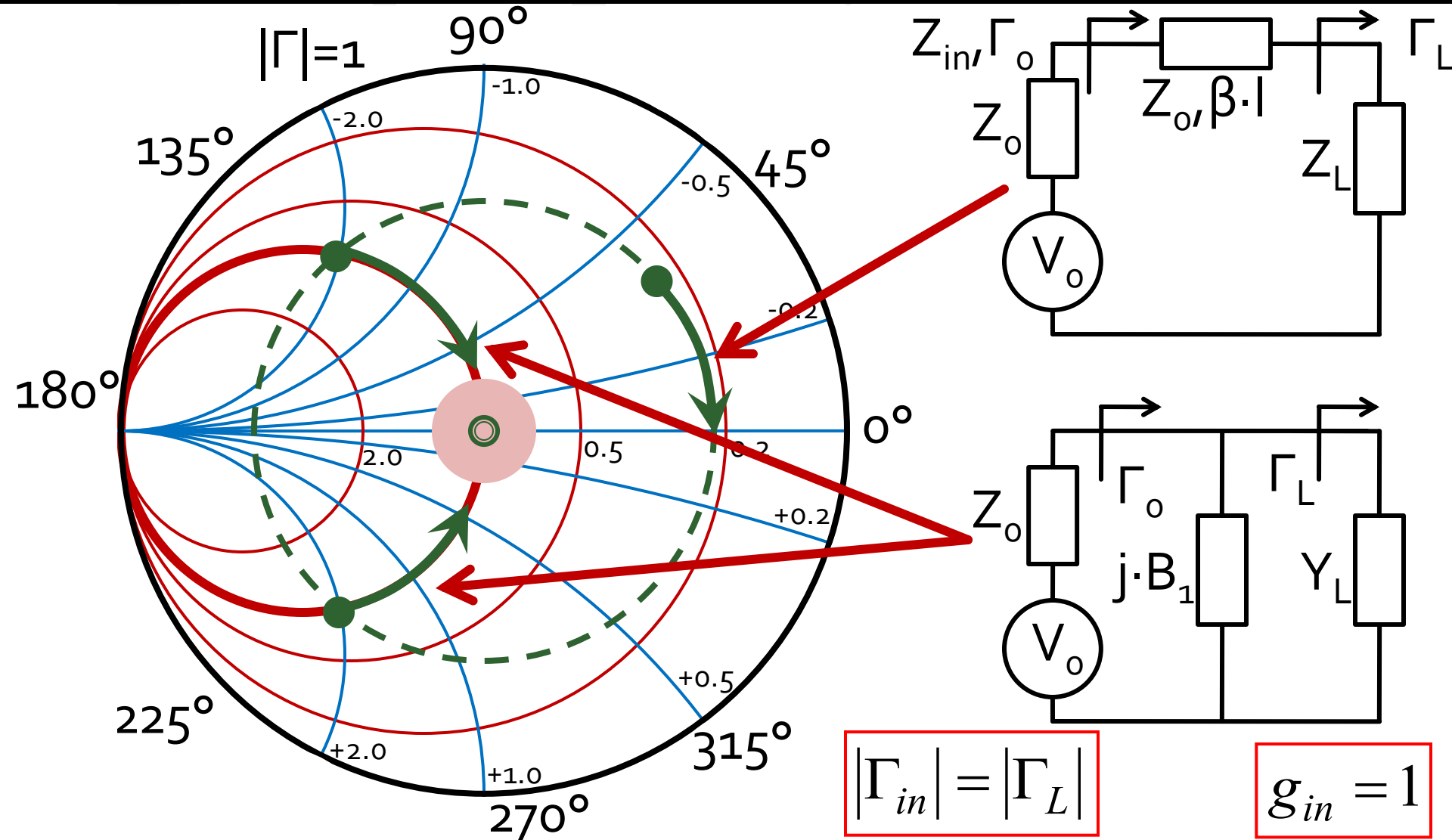
Exam / Project

Case 1, Shunt Stub

- Shunt Stub



Matching, series line + shunt susceptance



Analytical solution, usage

$$\cos(\varphi + 2\theta) = -|\Gamma_S|$$

$$\Gamma_S = 0.593 \angle 46.85^\circ$$

$$\theta_{sp} = \beta \cdot l = \tan^{-1} \frac{\mp 2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}}$$

$$|\Gamma_S| = 0.593; \quad \varphi = 46.85^\circ \quad \cos(\varphi + 2\theta) = -0.593 \Rightarrow (\varphi + 2\theta) = \pm 126.35^\circ$$

- The **sign** (+/-) chosen for the **series line** equation imposes the **sign** used for the **shunt stub** equation

- **"+" solution** 

$$(46.85^\circ + 2\theta) = +126.35^\circ \quad \theta = +39.7^\circ \quad \text{Im } y_s = \frac{-2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}} = -1.472$$

$$\theta_{sp} = \tan^{-1}(\text{Im } y_s) = -55.8^\circ (+180^\circ) \rightarrow \theta_{sp} = 124.2^\circ$$

- **"-" solution** 

$$(46.85^\circ + 2\theta) = -126.35^\circ \quad \theta = -86.6^\circ (+180^\circ) \rightarrow \theta = 93.4^\circ$$

$$\text{Im } y_s = \frac{+2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}} = +1.472 \quad \theta_{sp} = \tan^{-1}(\text{Im } y_s) = 55.8^\circ$$

Analytical solution, usage

$$(\varphi + 2\theta) = \begin{cases} +126.35^\circ \\ -126.35^\circ \end{cases} \quad \theta = \begin{cases} 39.7^\circ \\ 93.4^\circ \end{cases} \quad \text{Im}[y_s(\theta)] = \begin{cases} -1.472 \\ +1.472 \end{cases} \quad \theta_{sp} = \begin{cases} -55.8^\circ + 180^\circ = 124.2^\circ \\ +55.8^\circ \end{cases}$$

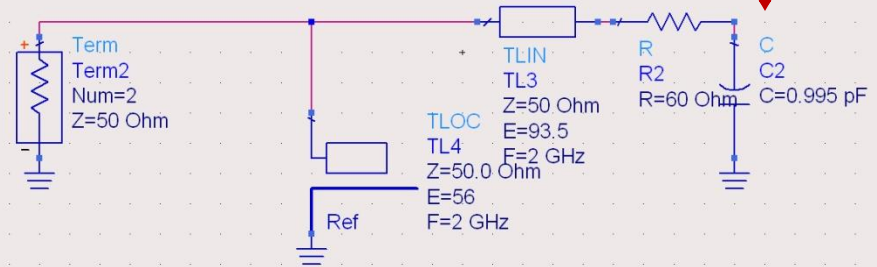
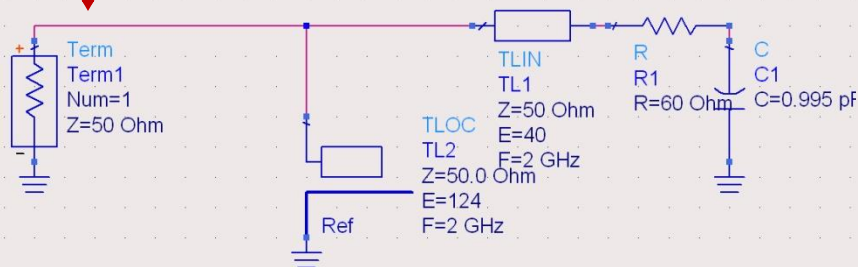
- We choose **one** of the two possible solutions
- The **sign** (+/-) chosen for the **series line** equation imposes the **sign** used for the **shunt stub** equation

$$l_1 = \frac{39.7^\circ}{360^\circ} \cdot \lambda = 0.110 \cdot \lambda$$

$$l_2 = \frac{124.2^\circ}{360^\circ} \cdot \lambda = 0.345 \cdot \lambda$$

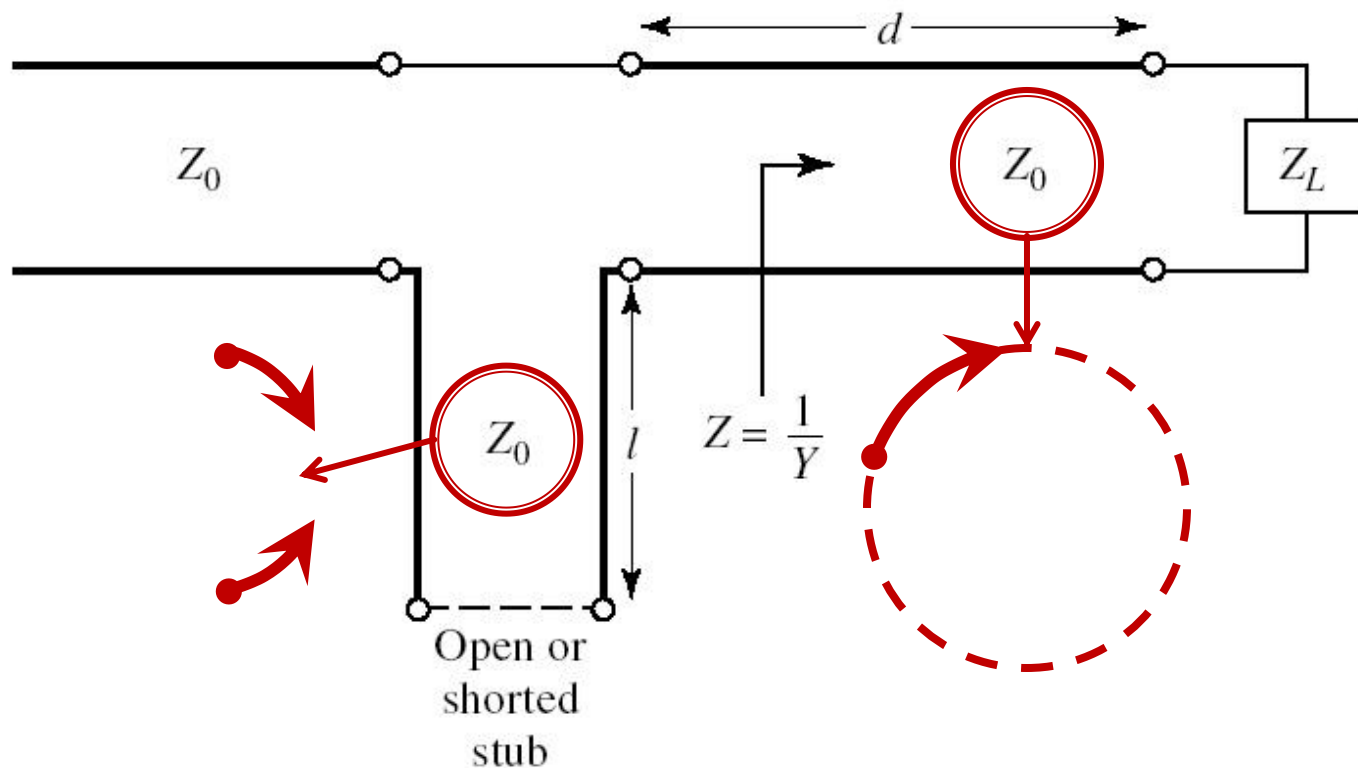
$$l_1 = \frac{93.4^\circ}{360^\circ} \cdot \lambda = 0.259 \cdot \lambda$$

$$l_2 = \frac{55.8^\circ}{360^\circ} \cdot \lambda = 0.155 \cdot \lambda$$

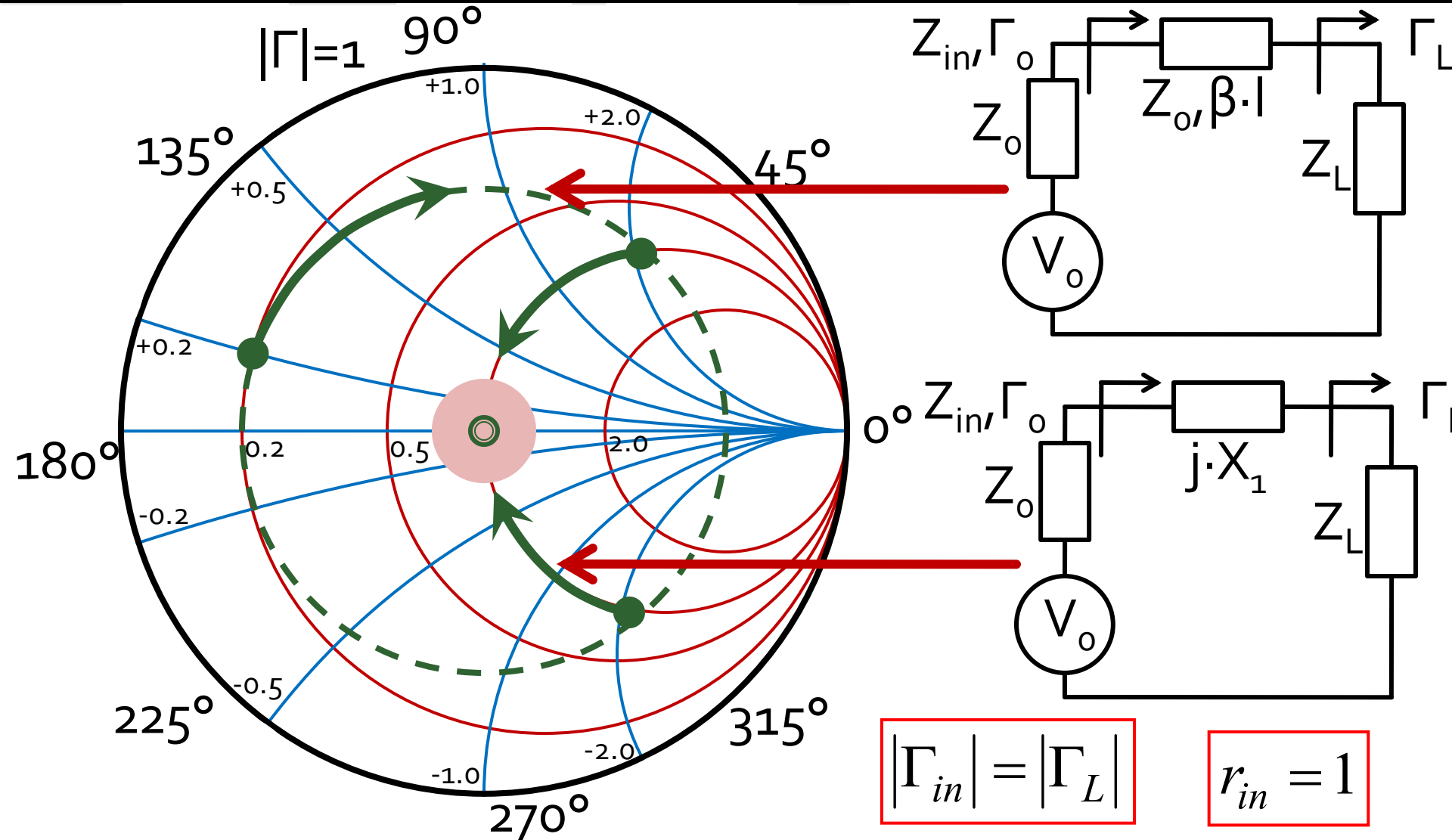


Case 2, Series Stub

- Series Stub
- difficult to realize in single conductor line technologies (microstrip)



Matching, series line + series reactance



Analytical solution, usage

$$\cos(\varphi + 2\theta) = |\Gamma_S|$$

$$\theta_{ss} = \beta \cdot l = \cot^{-1} \frac{\mp 2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}}$$

$$\Gamma_S = 0.555 \angle -29.92^\circ$$

$$|\Gamma_S| = 0.555; \quad \varphi = -29.92^\circ \quad \cos(\varphi + 2\theta) = 0.555 \Rightarrow (\varphi + 2\theta) = \pm 56.28^\circ$$

- The **sign** (+/-) chosen for the **series line** equation imposes the **sign** used for the **series stub** equation

- **"+" solution** ↓

$$(-29.92^\circ + 2\theta) = +56.28^\circ$$

$$\theta = 43.1^\circ$$

$$\text{Im } z_S = \frac{+2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}} = +1.335$$

$$\theta_{ss} = -\cot^{-1}(\text{Im } z_S) = -36.8^\circ (+180^\circ) \rightarrow \theta_{ss} = 143.2^\circ$$

- **"-" solution** ↓

$$(-29.92^\circ + 2\theta) = -56.28^\circ$$

$$\theta = -13.2^\circ (+180^\circ) \rightarrow \theta = 166.8^\circ$$

$$\text{Im } z_S = \frac{-2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}} = -1.335$$

$$\theta_{ss} = -\cot^{-1}(\text{Im } z_S) = 36.8^\circ$$

Analytical solution, usage

$$(\varphi + 2\theta) = \begin{cases} +56.28^\circ \\ -56.28^\circ \end{cases} \quad \theta = \begin{cases} 43.1^\circ \\ 166.8^\circ \end{cases} \quad \text{Im}[z_s(\theta)] = \begin{cases} +1.335 \\ -1.335 \end{cases} \quad \theta_{ss} = \begin{cases} -36.8^\circ + 180^\circ = 143.2^\circ \\ +36.8^\circ \end{cases}$$

- We choose **one** of the two possible solutions
- The **sign** (+/-) chosen for the **series line** equation imposes the **sign** used for the **series stub** equation

$$l_1 = \frac{43.1^\circ}{360^\circ} \cdot \lambda = 0.120 \cdot \lambda$$

$$l_2 = \frac{143.2^\circ}{360^\circ} \cdot \lambda = 0.398 \cdot \lambda$$

$$l_1 = \frac{166.8^\circ}{360^\circ} \cdot \lambda = 0.463 \cdot \lambda$$

$$l_2 = \frac{36.8^\circ}{360^\circ} \cdot \lambda = 0.102 \cdot \lambda$$



Stub, observations

- adding or subtracting **180°** ($\lambda/2$) doesn't change the result (full rotation around the Smith Chart)

$$E = \beta \cdot l = \pi = 180^\circ \quad l = k \cdot \frac{\lambda}{2}, \forall k \in \mathbb{N}$$

- if the lines/stubs result with **negative** "length"/ "electrical length" we add $\lambda/2$ / 180° to obtain physically realizable lines
- adding or subtracting **90°** ($\lambda/4$) change the stub impedance:

$$Z_{in,sc} = j \cdot Z_0 \cdot \tan \beta \cdot l \quad \Leftrightarrow \quad Z_{in,g} = -j \cdot Z_0 \cdot \cot \beta \cdot l$$

- for the stub we can add or subtract 90° ($\lambda/4$) while in the same time changing **open-circuit** $\Leftrightarrow$ **short-circuit**

Microwave Filters

Insertion loss method

- We control the power loss ratio/attenuation introduced by the filter:
 - in the passband (pass all frequencies)
 - in the stopband (reject all frequencies)

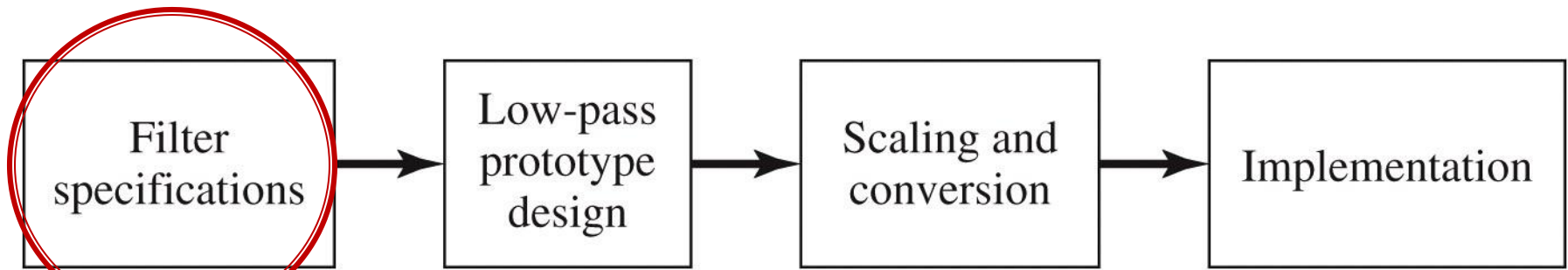
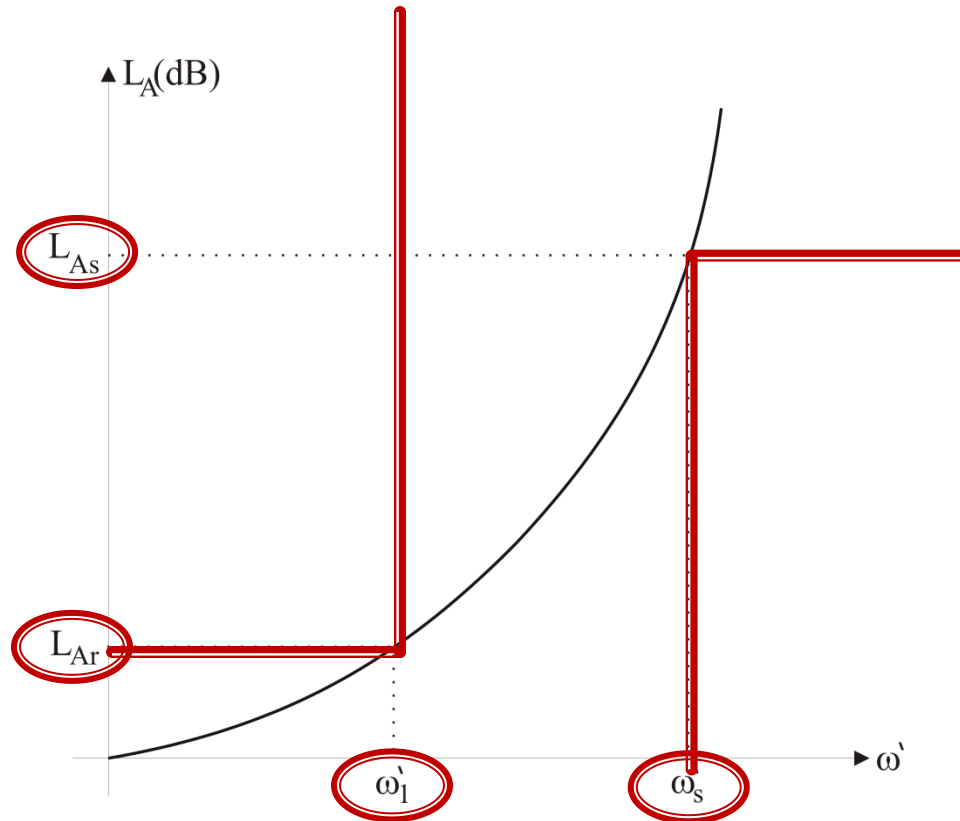


Figure 8.23

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Filter specifications

- Attenuation
 - in passband
 - in stopband
 - most often in **dB**
- Frequency range
 - passband
 - stopband
 - cutoff frequency ω_1'
usually normalized
(= **1**)



Insertion loss method

- We choose the right polynomials to design an **low-pass** filter (prototype)
- The low-pass prototype are then converted to the desired other types of filters
 - low-pass, high-pass, bandpass, or bandstop

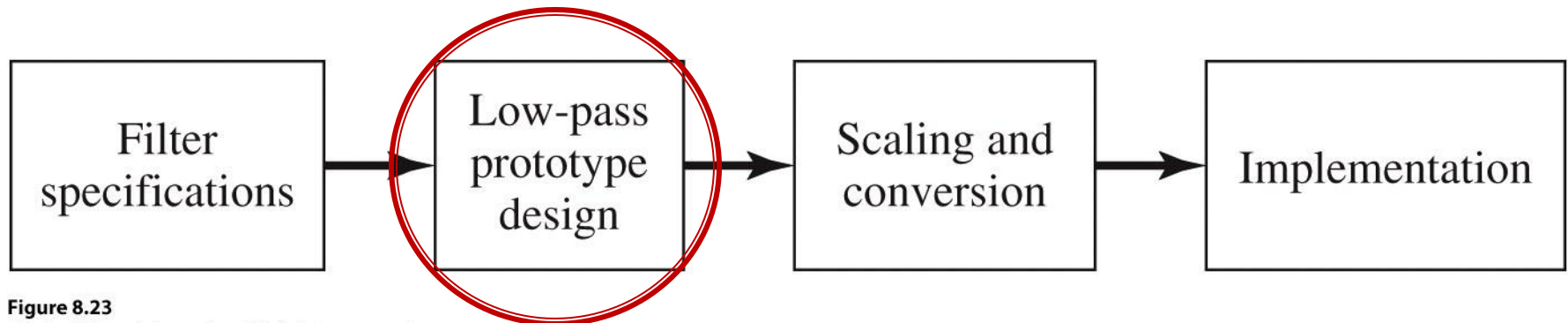
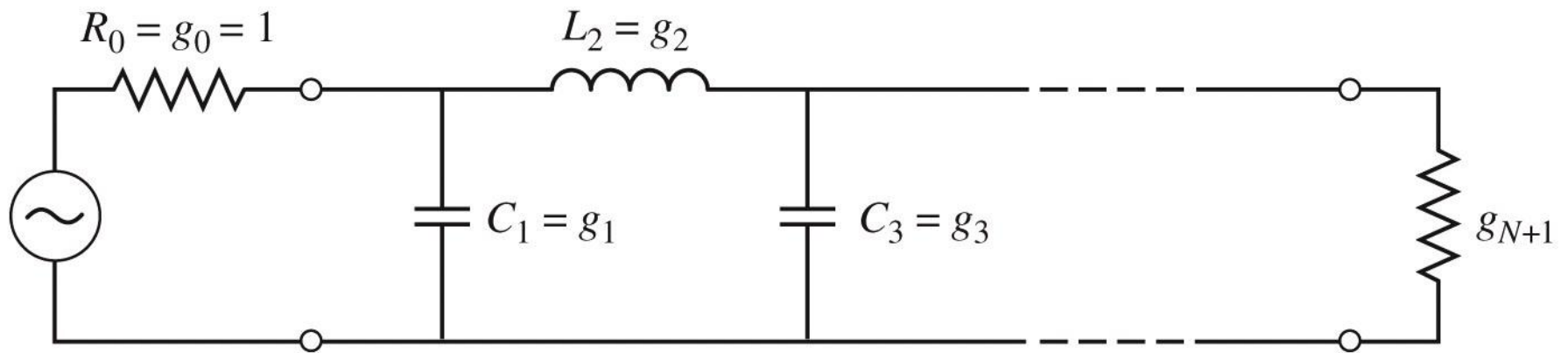
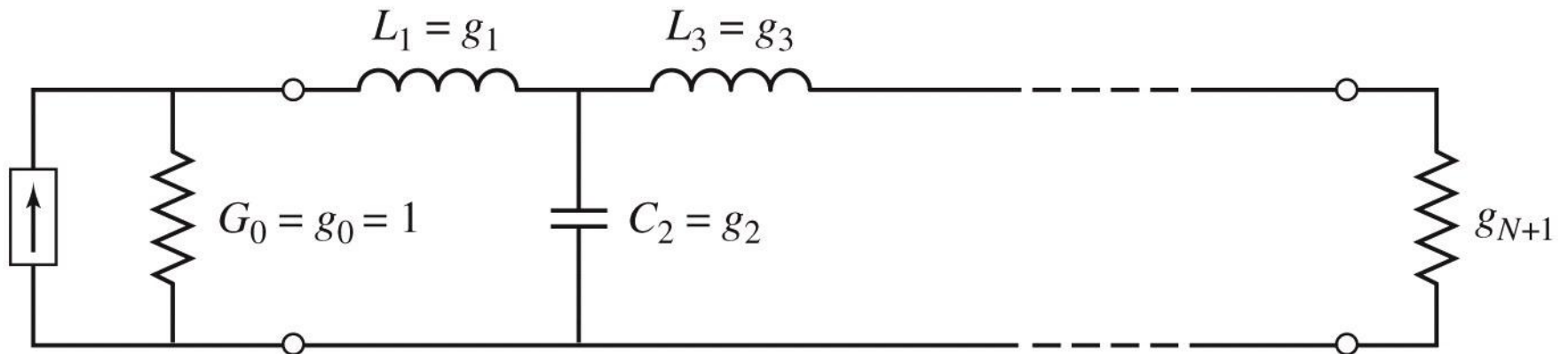


Figure 8.23

Prototype Filters



(a)



(b)

Maximally Flat LPF Prototype

TABLE 8.3 Element Values for Maximally Flat Low-Pass Filter Prototypes ($g_0 = 1$, $\omega_c = 1$, $N = 1$ to 10)

N	g_1	g_2	g_3	g_4	g_5	g_6	g_7	g_8	g_9	g_{10}	g_{11}
1	2.0000	1.0000									
2	1.4142	1.4142	1.0000								
3	1.0000	2.0000	1.0000	1.0000							
4	0.7654	1.8478	1.8478	0.7654	1.0000						
5	0.6180	1.6180	2.0000	1.6180	0.6180	1.0000					
6	0.5176	1.4142	1.9318	1.9318	1.4142	0.5176	1.0000				
7	0.4450	1.2470	1.8019	2.0000	1.8019	1.2470	0.4450	1.0000			
8	0.3902	1.1111	1.6629	1.9615	1.9615	1.6629	1.1111	0.3902	1.0000		
9	0.3473	1.0000	1.5321	1.8794	2.0000	1.8794	1.5321	1.0000	0.3473	1.0000	
10	0.3129	0.9080	1.4142	1.7820	1.9754	1.9754	1.7820	1.4142	0.9080	0.3129	1.0000

Source: Reprinted from G. L. Matthaei, L. Young, and E. M. T. Jones, *Microwave Filters, Impedance-Matching Networks, and Coupling Structures*, Artech House, Dedham, Mass., 1980, with permission.

TABLE 8.4 Element Values for Equal-Ripple Low-Pass Filter Prototypes ($g_0 = 1, \omega_c = 1, N = 1$ to 10, 0.5 dB and 3.0 dB ripple)

N	0.5 dB Ripple										
	g_1	g_2	g_3	g_4	g_5	g_6	g_7	g_8	g_9	g_{10}	g_{11}
1	0.6986	1.0000									
2	1.4029	0.7071	1.9841								
3	1.5963	1.0967	1.5963	1.0000							
4	1.6703	1.1926	2.3661	0.8419	1.9841						
5	1.7058	1.2296	2.5408	1.2296	1.7058	1.0000					
6	1.7254	1.2479	2.6064	1.3137	2.4758	0.8696	1.9841				
7	1.7372	1.2583	2.6381	1.3444	2.6381	1.2583	1.7372	1.0000			
8	1.7451	1.2647	2.6564	1.3590	2.6964	1.3389	2.5093	0.8796	1.9841		
9	1.7504	1.2690	2.6678	1.3673	2.7239	1.3673	2.6678	1.2690	1.7504	1.0000	
10	1.7543	1.2721	2.6754	1.3725	2.7392	1.3806	2.7231	1.3485	2.5239	0.8842	1.9841

N	3.0 dB Ripple										
	g_1	g_2	g_3	g_4	g_5	g_6	g_7	g_8	g_9	g_{10}	g_{11}
1	1.9953	1.0000									
2	3.1013	0.5339	5.8095								
3	3.3487	0.7117	3.3487	1.0000							
4	3.4389	0.7483	4.3471	0.5920	5.8095						
5	3.4817	0.7618	4.5381	0.7618	3.4817	1.0000					
6	3.5045	0.7685	4.6061	0.7929	4.4641	0.6033	5.8095				
7	3.5182	0.7723	4.6386	0.8039	4.6386	0.7723	3.5182	1.0000			
8	3.5277	0.7745	4.6575	0.8089	4.6990	0.8018	4.4990	0.6073	5.8095		
9	3.5340	0.7760	4.6692	0.8118	4.7272	0.8118	4.6692	0.7760	3.5340	1.0000	
10	3.5384	0.7771	4.6768	0.8136	4.7425	0.8164	4.7260	0.8051	4.5142	0.6091	5.8095

Source: Reprinted from G. L. Matthaei, L. Young, and E. M. T. Jones, *Microwave Filters, Impedance-Matching Networks, and Coupling Structures*, Artech House, Dedham, Mass., 1980, with permission.

- For even N order of the filter ($N = 2, 4, 6, 8 \dots$) equal-ripple filters **must** closed by a load impedance **$g_{N+1} \neq 1$**
- If the application doesn't allow this, supplemental impedance matching is required (quarter-wave transformer, binomial ...) to **$g_L = 1$**

Impedance and Frequency Scaling

- After computing prototype filter's elements:
 - Low-Pass Filters (**LPF**)
 - cutoff frequency **$\omega_o = 1 \text{ rad/s}$** ($f_o = 0.159 \text{ Hz}$)
 - connected to a source with **$R = 1\Omega$**
- component values can be scaled in terms of impedance and frequency

Impedance and Frequency Scaling

- LPF Prototype is only used as an intermediate step
 - Low-Pass Filter (LPF)
 - cutoff frequency $\omega_o = 1 \text{ rad/s}$ ($f_o = 0.159 \text{ Hz}$)
 - connected to a source with $R = 1\Omega$

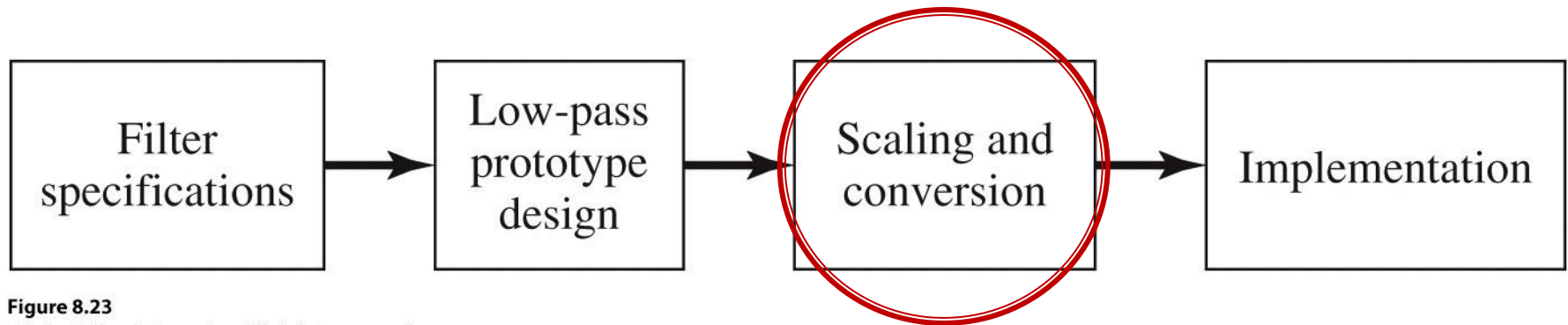


Figure 8.23

Summary of Prototype Filter Transformations

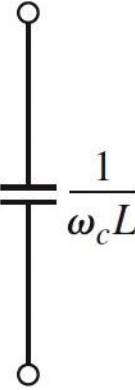
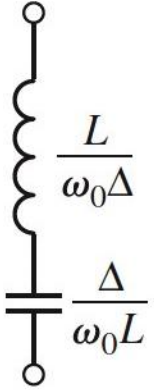
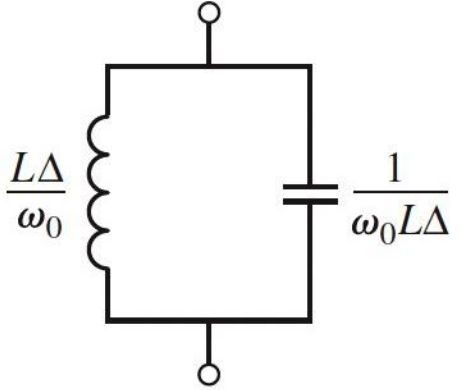
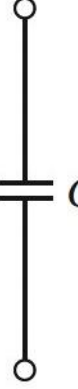
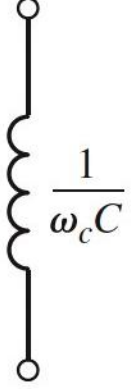
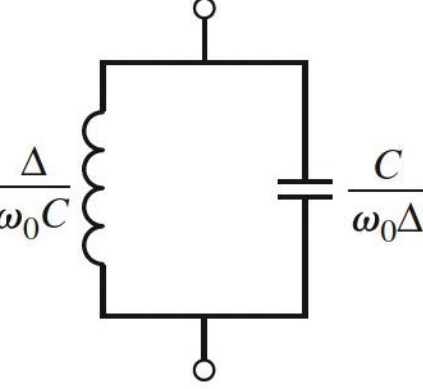
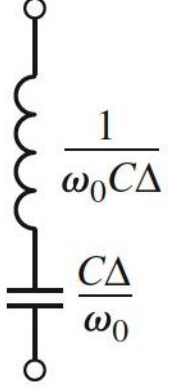
Low-pass	High-pass	Bandpass	Bandstop
			
			

Table 8.6

Microwave Filters Implementation

Microwave Filters Implementation

- The lumped-element (L, C) filter design generally works well **only** at low frequencies (RF):
 - lumped-element inductors and capacitors are generally available only for a limited range of values, and can be difficult to implement at microwave frequencies
 - difficulty to obtain the (very low) required tolerance for elements

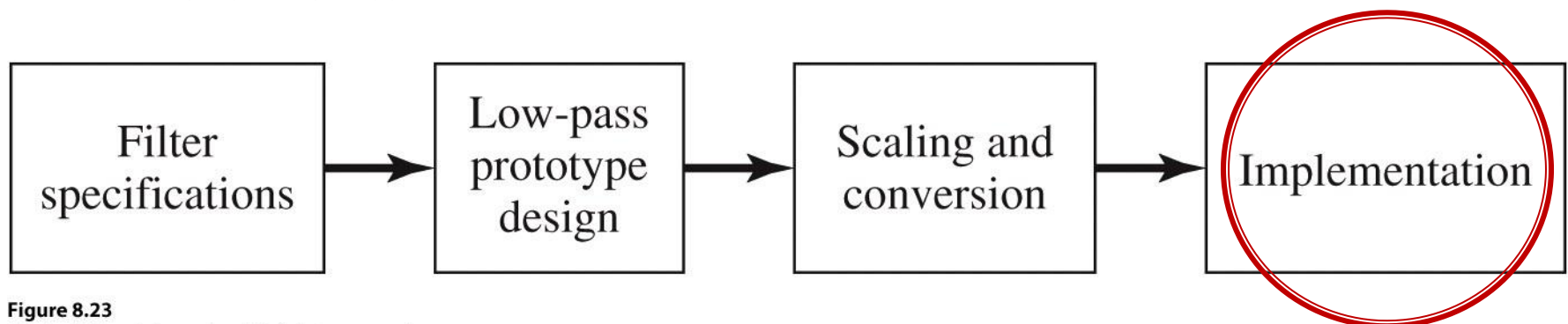
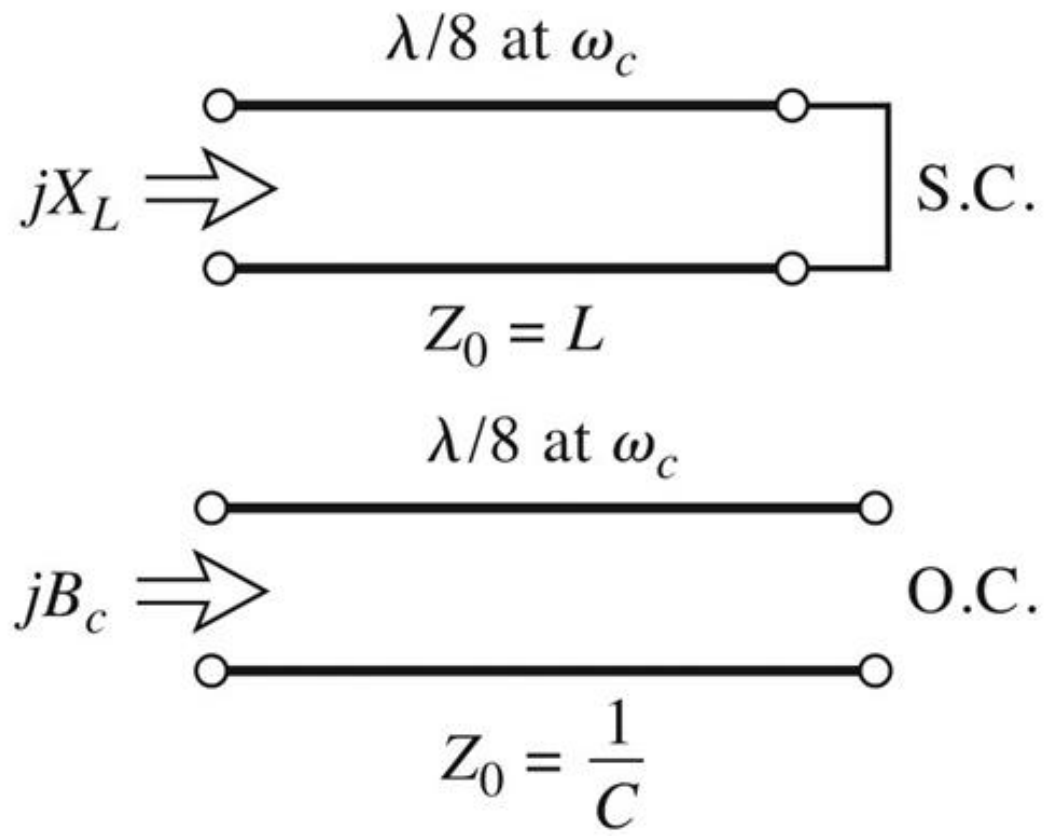
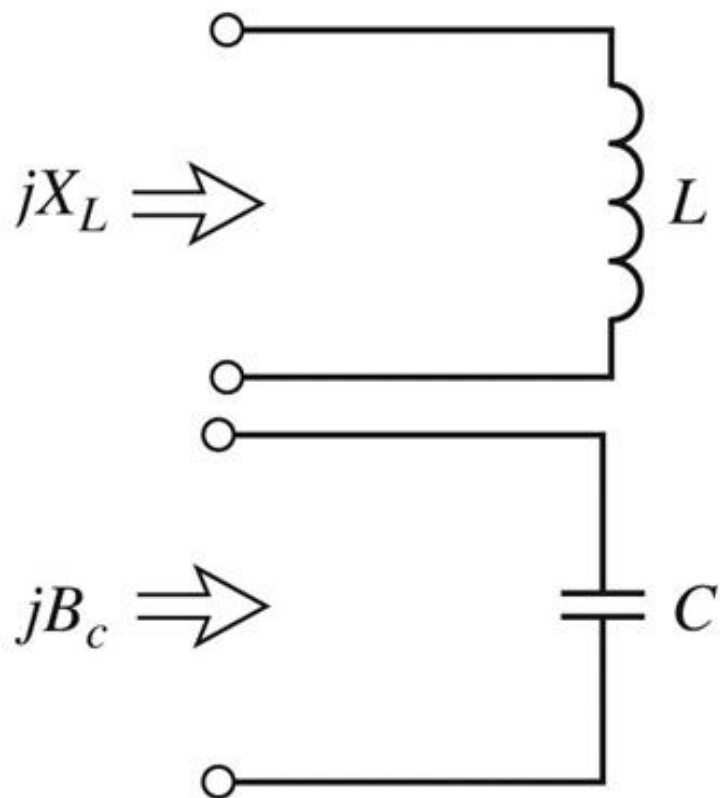


Figure 8.23

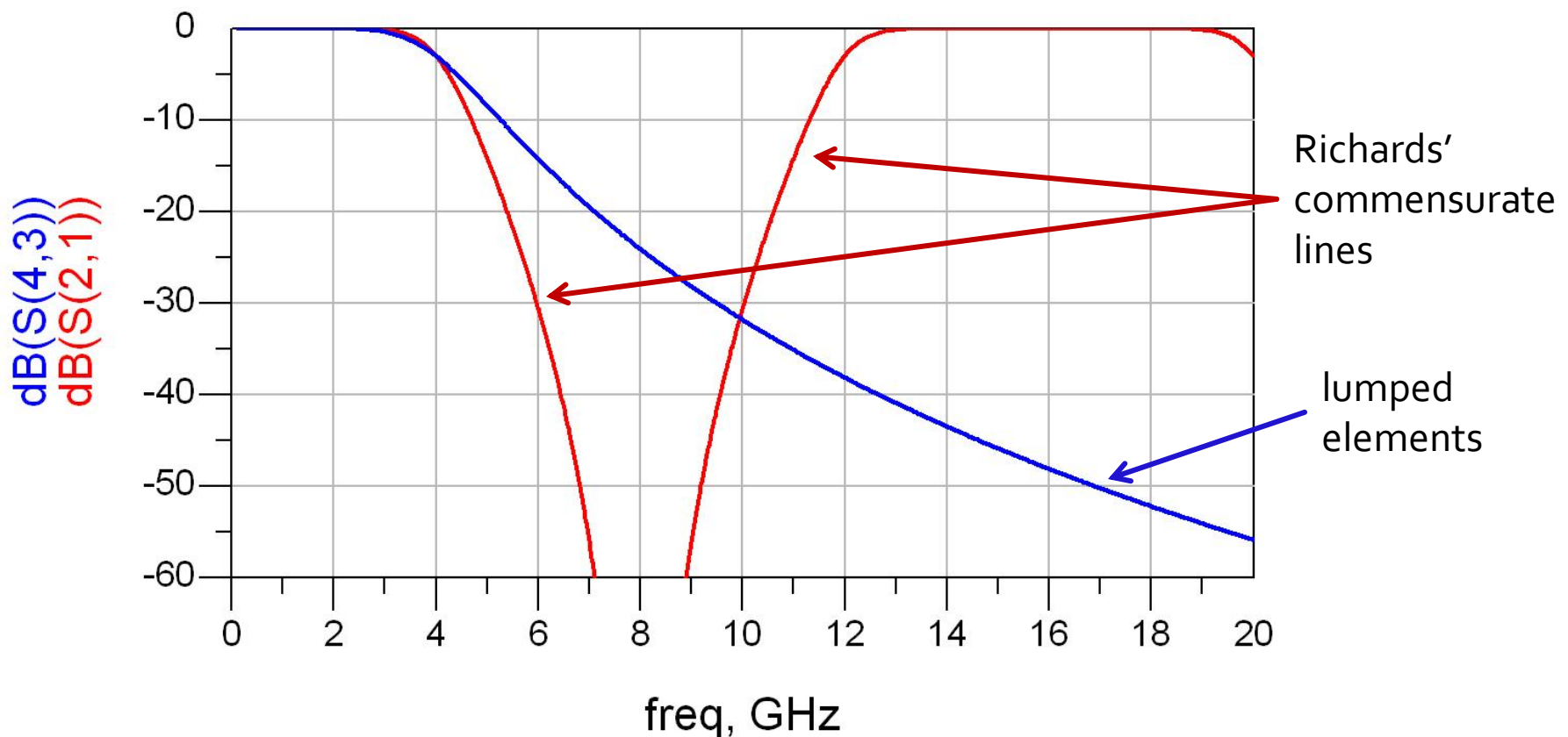
Richards' Transformation

- allows implementation of the inductors and capacitors with lines **after** the transformation of the LPF prototype to the required type (LPF/HPF/BPF/BSF)



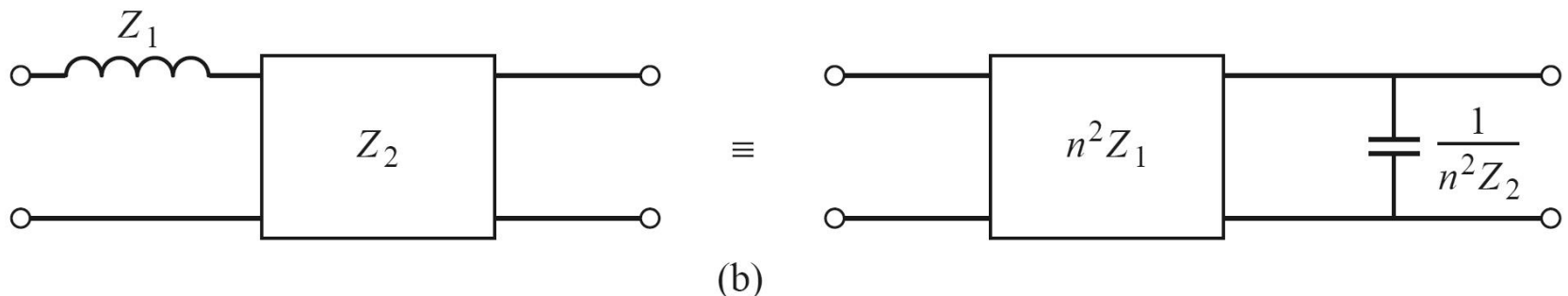
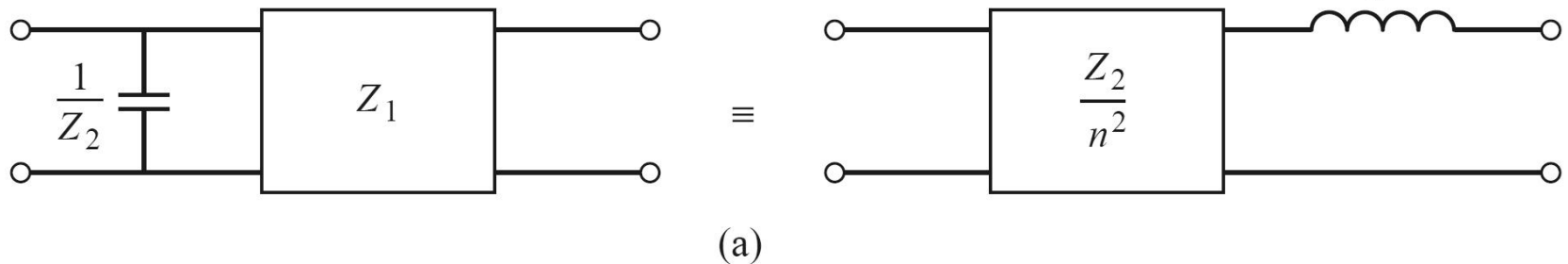
Richards' Transformation

- Filters implemented with Richards' Transformation
 - beneficiate from the supplemental pole at $2 \cdot \omega_c$
 - have the major disadvantage of frequency periodicity, a supplemental non-periodic LPF must be inserted if needed



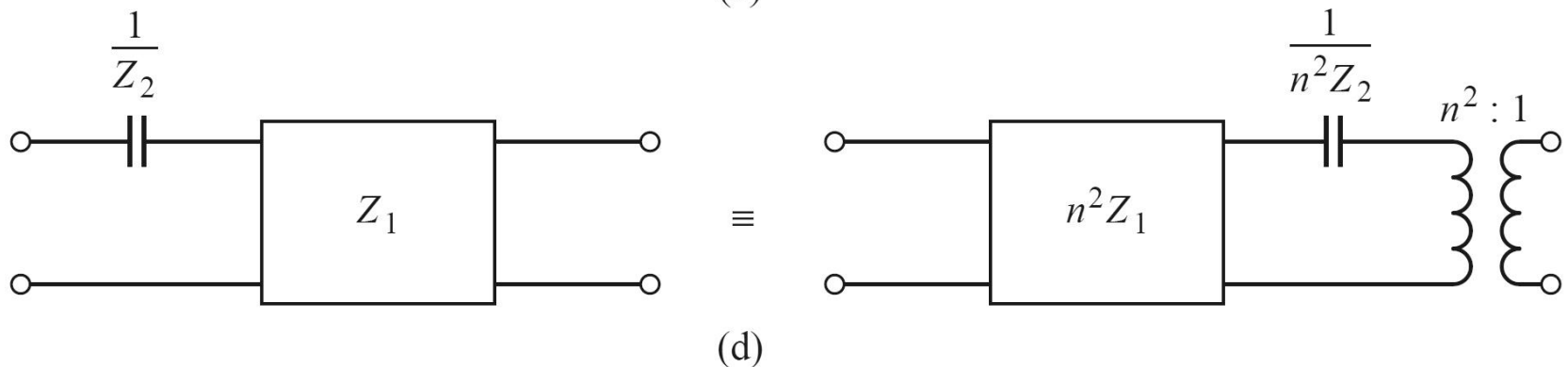
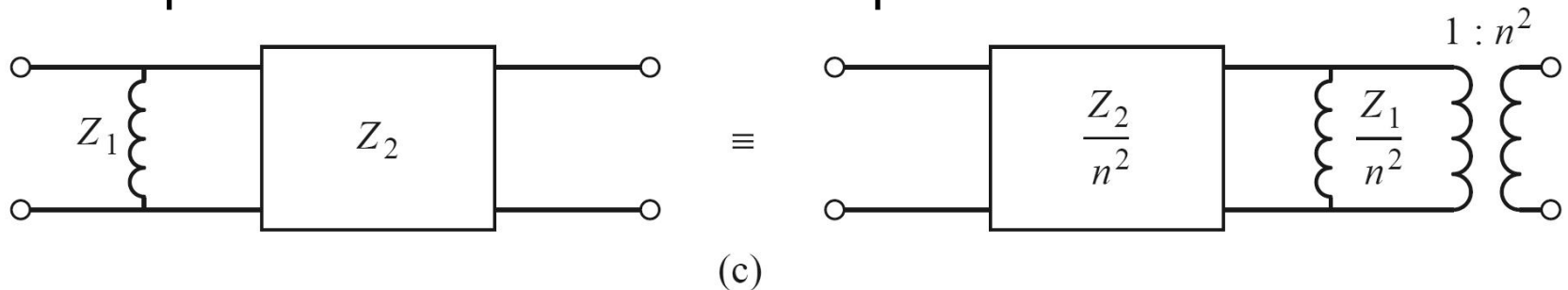
Kuroda's Identities

- 4 circuit equivalents (a,b)
 - each box represents a unit element, or transmission line, of the indicated characteristic impedance and length ($\lambda/8$ at ω_c). The inductors and capacitors represent short-circuit and open-circuit stubs $\frac{Z_1}{n^2}$



Kuroda's Identities

- 4 circuit equivalents (c,d)
 - each box represents a unit element, or transmission line, of the indicated characteristic impedance and length ($\lambda/8$ at ω_c). The inductors and capacitors represent short-circuit and open-circuit stubs



First Kuroda's Identity

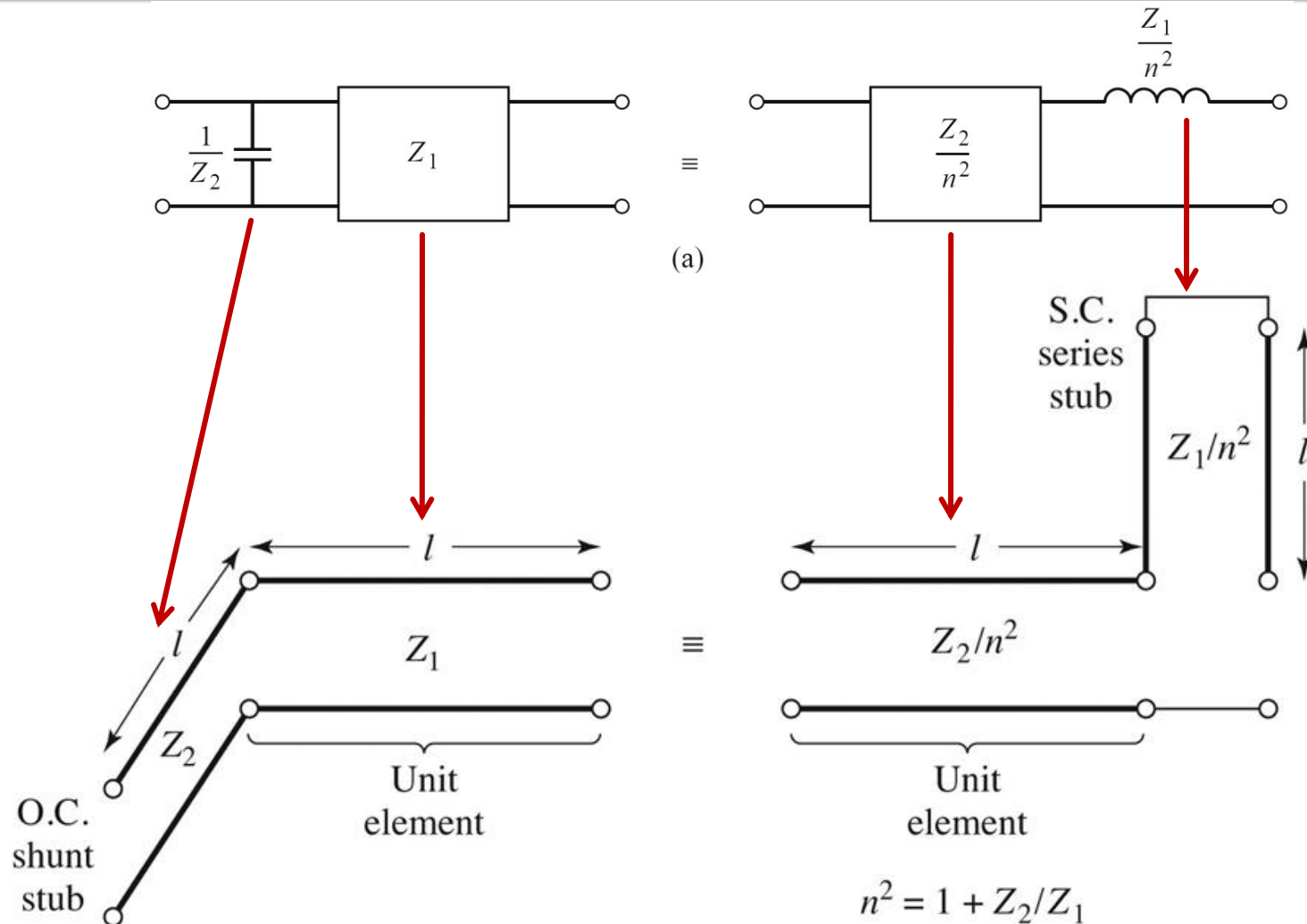
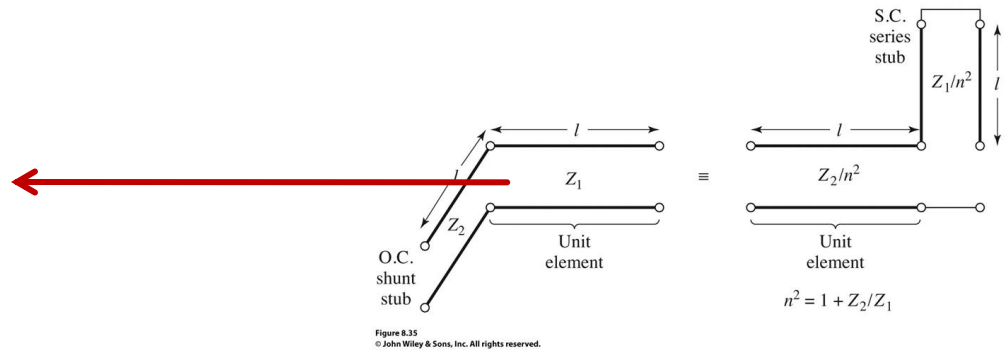
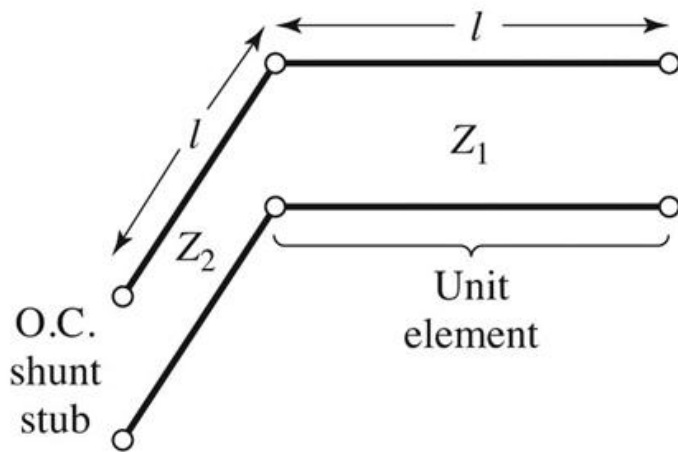
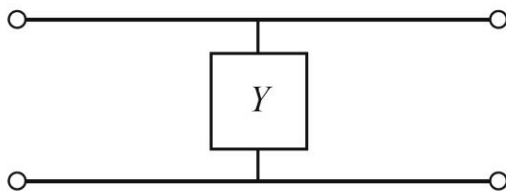


Figure 8.35
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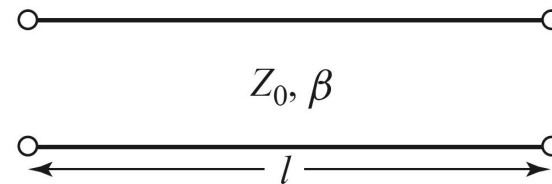
First Kuroda's Identity – Proof



■ ABCD matrices, L_4



+



$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ Y & 1 \end{bmatrix}$$

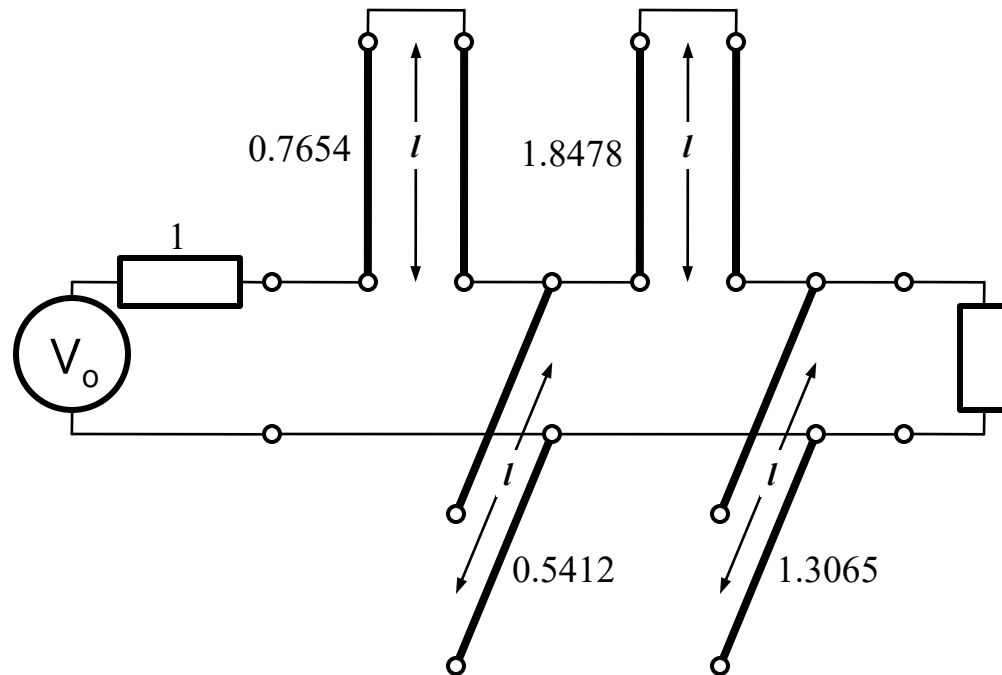
$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} \cos \beta \cdot l & j \cdot Z_0 \cdot \sin \beta \cdot l \\ j \cdot Y_0 \cdot \sin \beta \cdot l & \cos \beta \cdot l \end{bmatrix}$$

Example

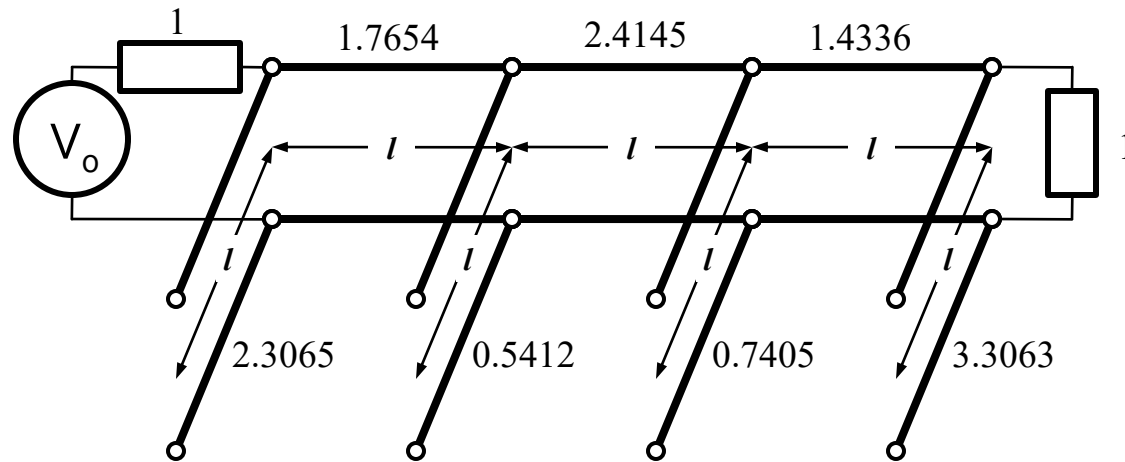
■ Apply Richards's transformation

■ Problems:

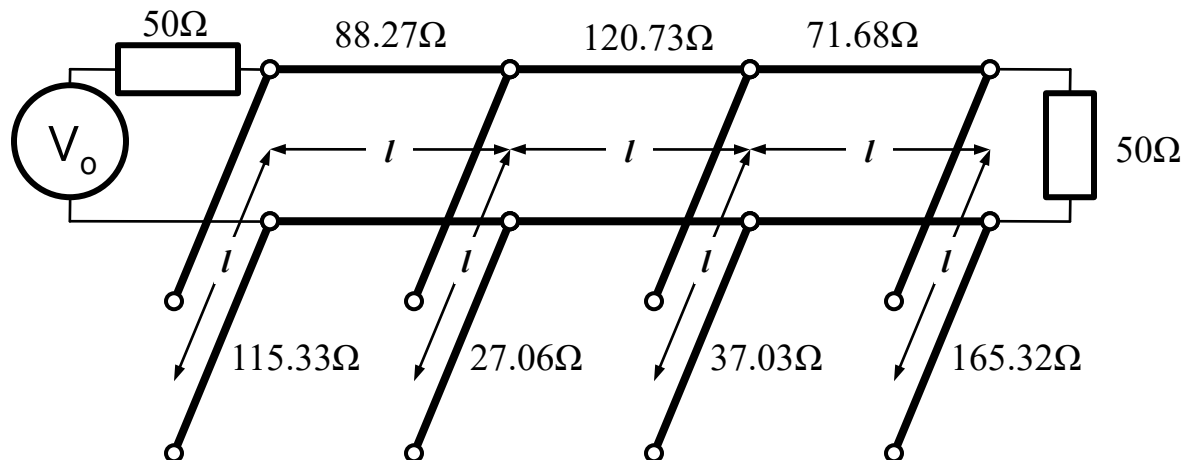
- the series stubs would be **very difficult** to implement in microstrip line technology
- in microstrip technology it is preferable to have open-circuit stubs (short-circuit requires a **via-hole** to the ground plane)
- the 4 stubs are physically connected at the same point, an implementation that eliminates/reduces the **coupling** between these lines is impossible
- not the case here, but sometimes the normalized impedances are much different from 1. Most circuit technologies are designed for 50Ω lines



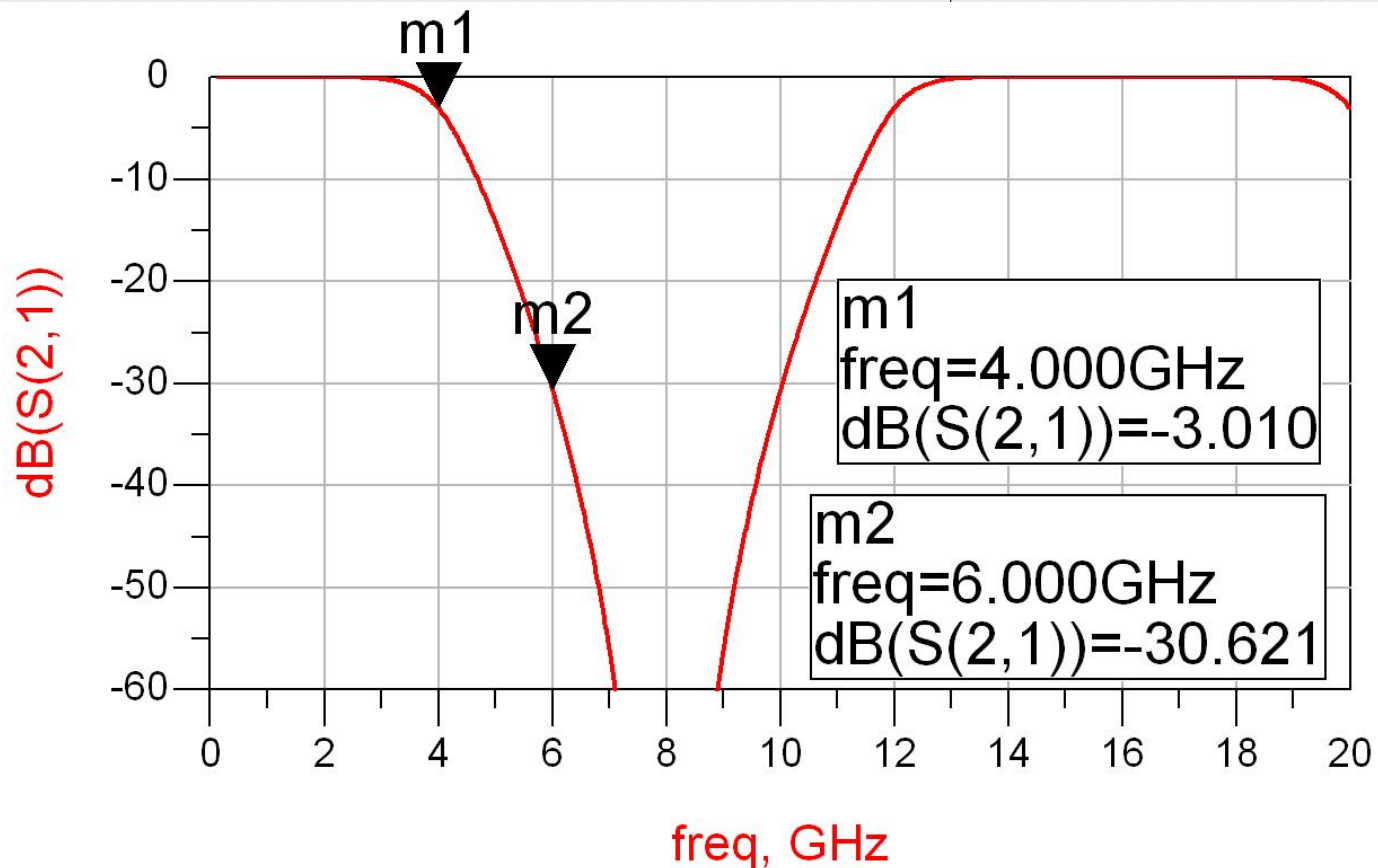
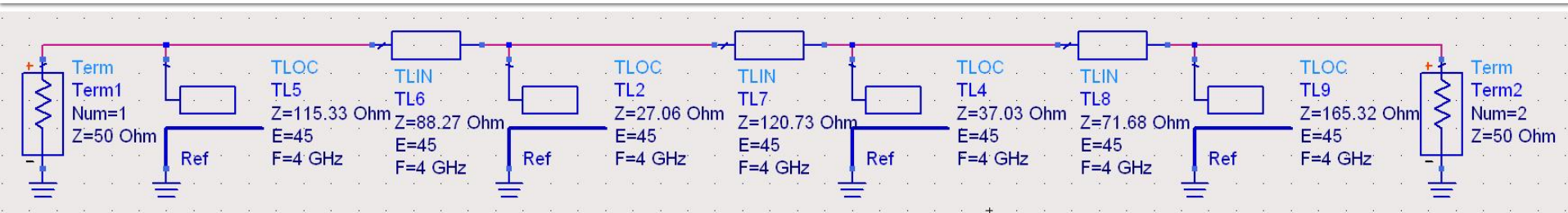
Example



- Impedance scaling (multiply by 50Ω)



Kuroda's Identities – ADS



Continue

Impedance and Admittance Inverters

- Richards' transformation and Kuroda's identities are useful especially for low-pass filters in technologies where the series stubs would be very difficult/impossible to implement (microstrip)
- In the case of other filters (example 3rd order BPF):
 - series inductance can be implemented using K1-K2
 - series capacitance cannot be implemented using shunt stubs

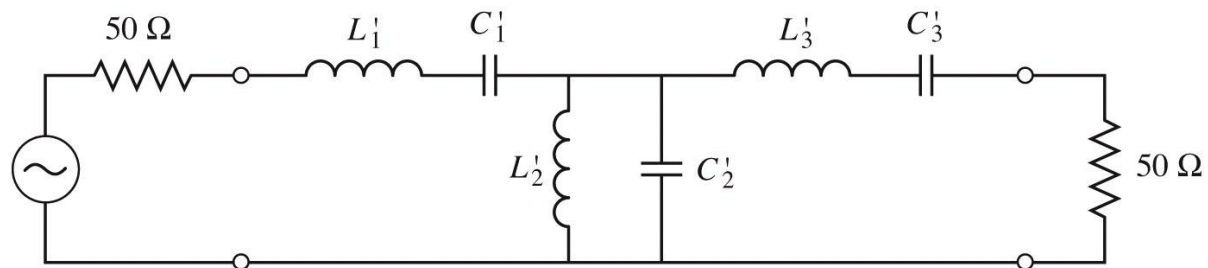


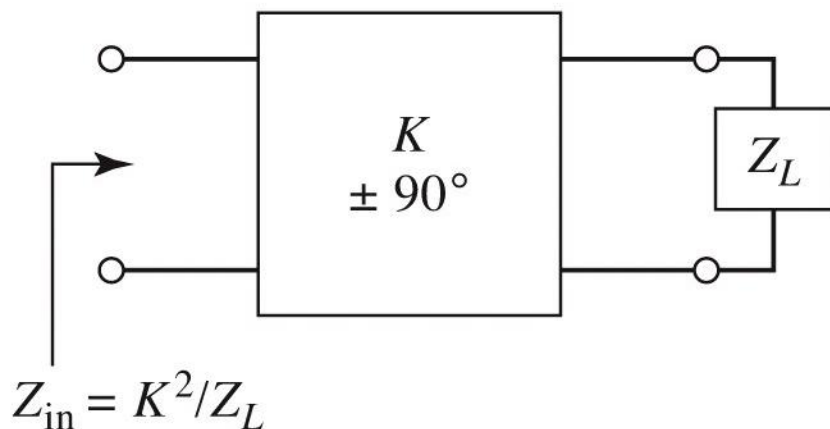
Figure 8.32
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Impedance and Admittance Inverters

- For cases where Richards + Kuroda do not offer practical solutions we use circuits called **impedance and admittance inverters**

$$Z_{in} = \frac{K^2}{Z_L}$$

Impedance inverters



$$Y_{in} = \frac{J^2}{Y_L}$$

Admittance inverters

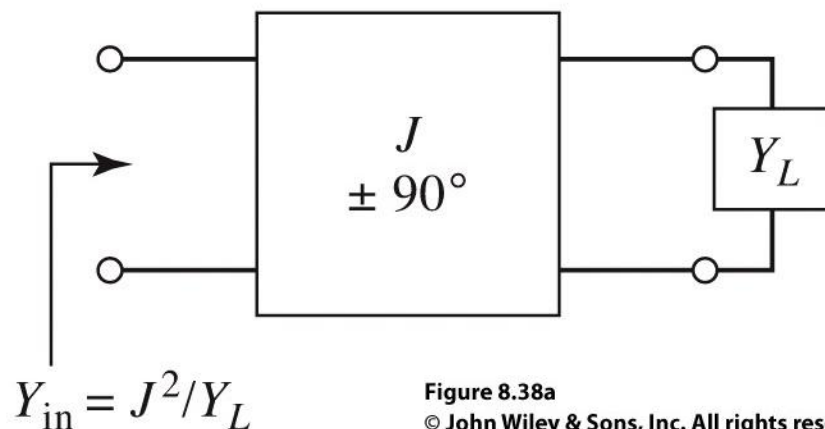


Figure 8.38a

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Impedance and Admittance Inverters

- The simplest example of impedance and admittance inverter is the **quarter-wave transformer** (L_3)

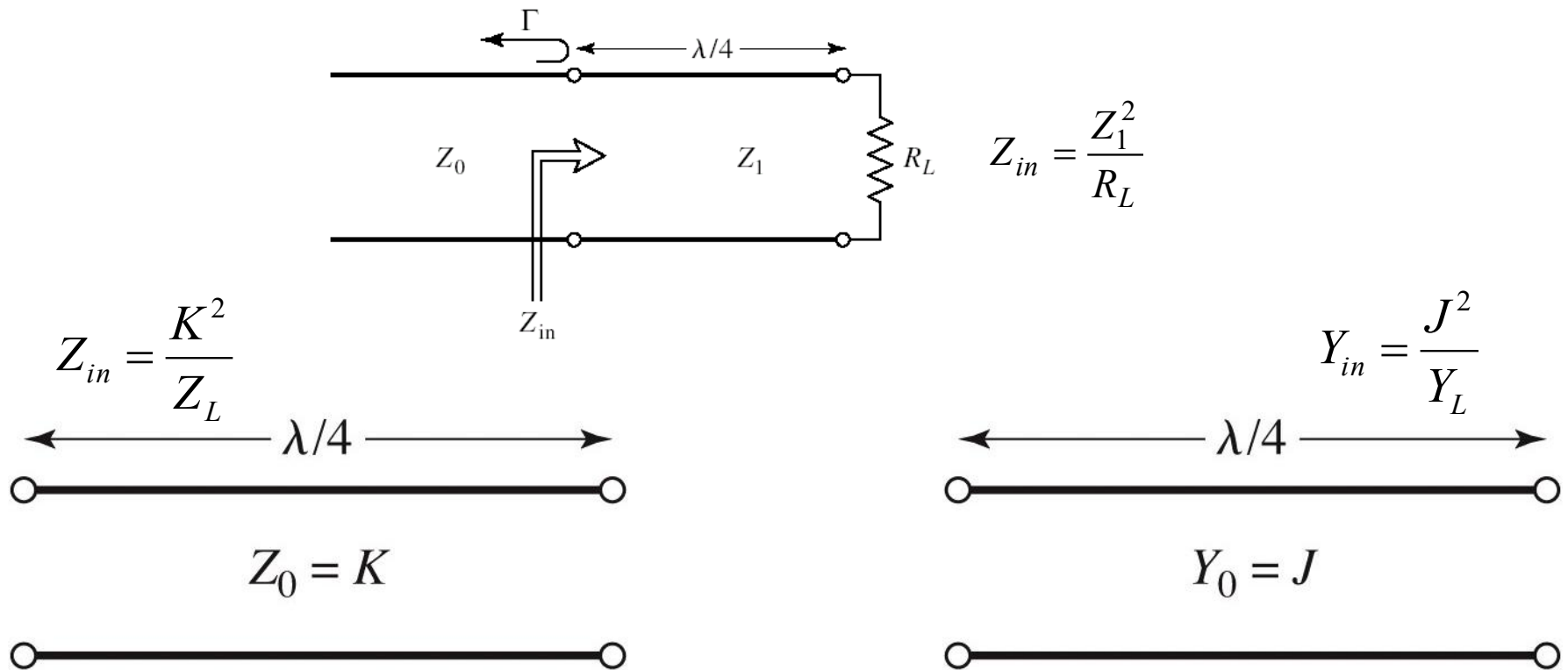
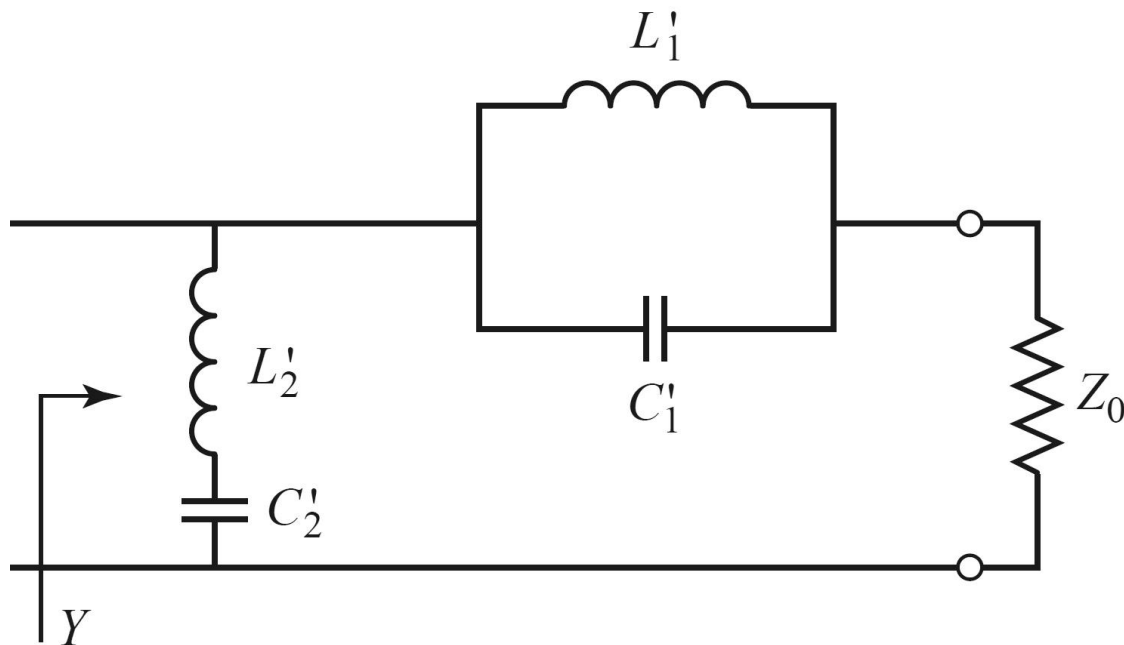


Figure 8.38b

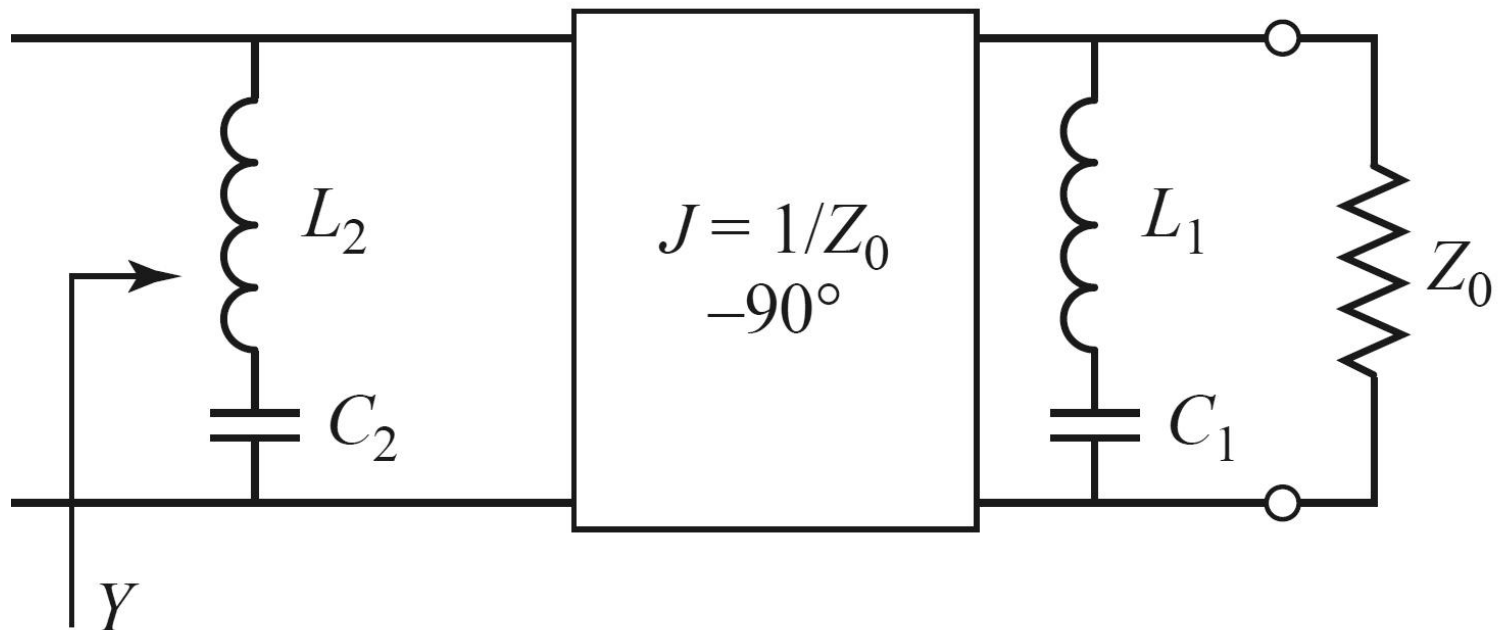
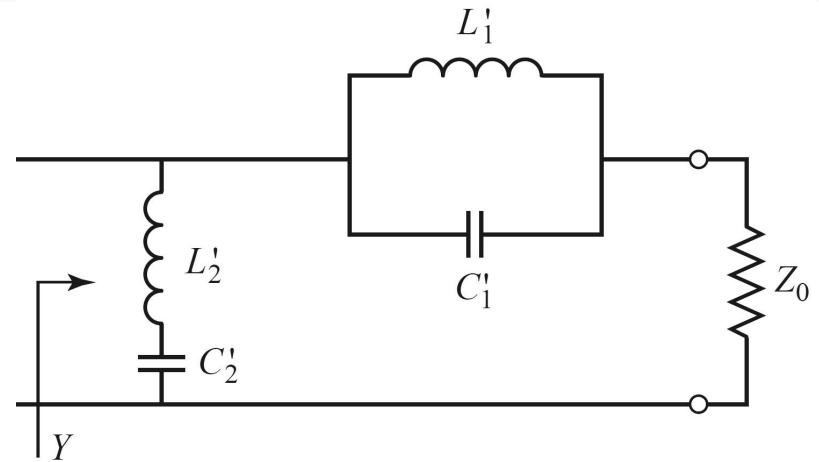
Impedance and Admittance Inverters

- Impedance/admittance inverters can be used to change the structure of a designed filter to a realizable form
- For example a 2nd order BSF



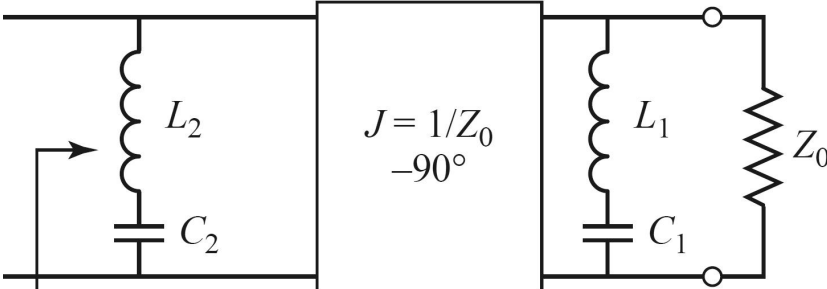
Impedance and Admittance Inverters

- The series elements can be eliminated/replaced using an admittance inverter



Impedance and Admittance Inverters

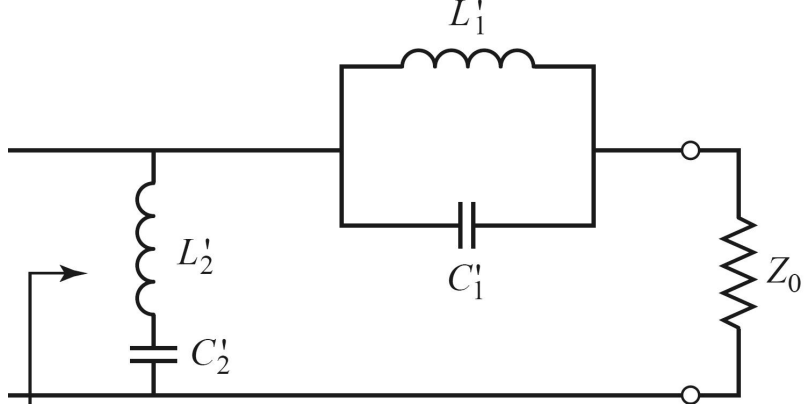
- The equivalence of the two schematics (when looking from the left) is proved by obtaining the same input admittance



$$Y = \frac{1}{j \cdot \omega \cdot L_2 + \frac{1}{j \cdot \omega \cdot C_2}} + \frac{1}{Z_0^2} \cdot \left(\frac{1}{j \cdot \omega \cdot L_1 + \frac{1}{j \cdot \omega \cdot C_1}} + \frac{1}{Z_0} \right)^{-1}$$

$$L_n \cdot C_n = L'_n \cdot C'_n = \frac{1}{\omega_0^2} \Rightarrow \frac{1}{Z_0^2} \cdot \sqrt{\frac{L_1}{C_1}} = \sqrt{\frac{C'_1}{L'_1}} \Rightarrow Y = Y'$$

$$\sqrt{\frac{L_2}{C_2}} = \sqrt{\frac{L'_2}{C'_2}}$$

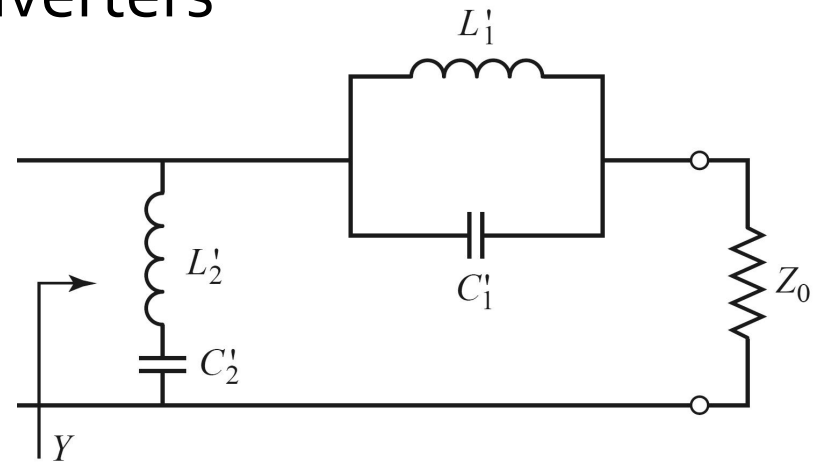
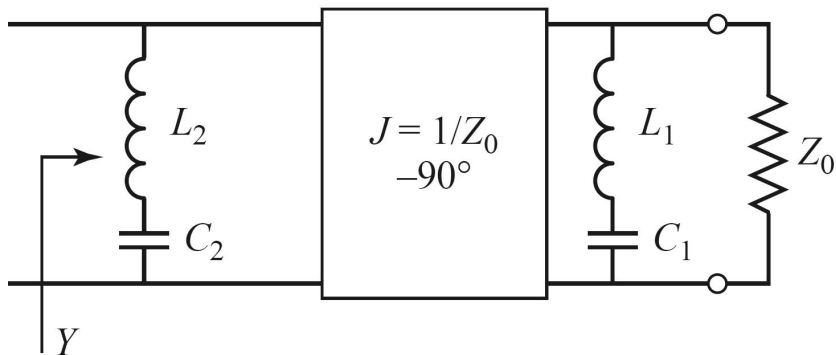


$$Y' = \frac{1}{j \cdot \omega \cdot L'_2 + \frac{1}{j \cdot \omega \cdot C'_2}} + \left(\frac{1}{j \cdot \omega \cdot C'_1 + \frac{1}{j \cdot \omega \cdot L'_1}} + Z_0 \right)^{-1}$$

- A similar result can be obtained for a bandpass filter

Impedance and Admittance Inverters

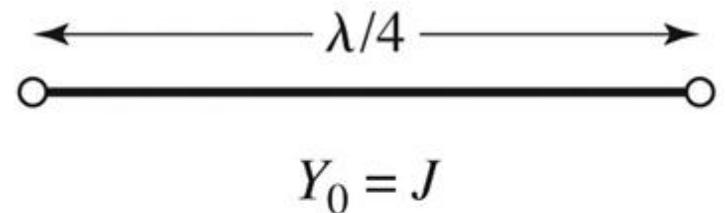
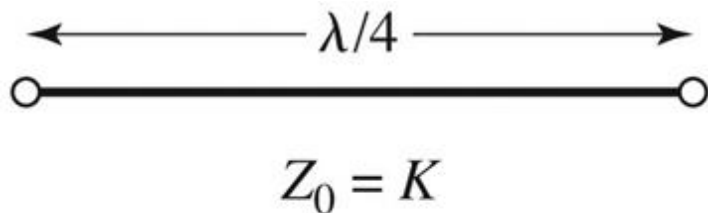
- The complete equivalence (when looking from both sides) is obtained by enclosing the series LC circuit between two admittance inverters



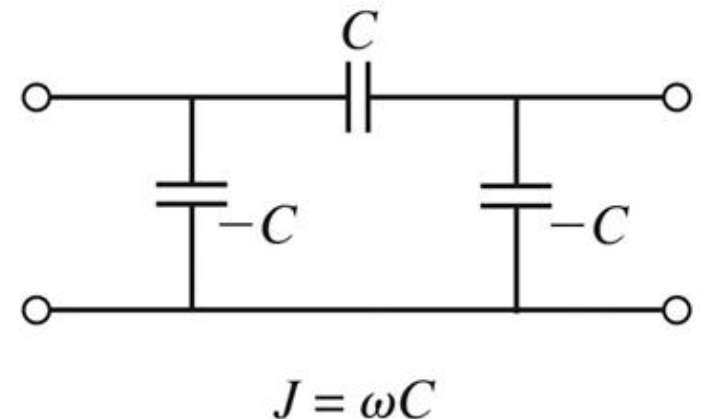
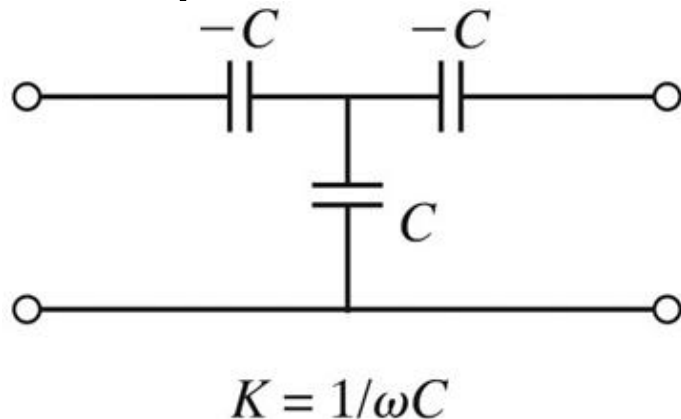
- A **series LC** circuit inserted in series in the circuit can be replaced by a **shunt LC** circuit inserted in parallel enclosed between 2 admittance inverters
- A **shunt LC** circuit inserted in series in the circuit can be replaced by a **series LC** circuit inserted in parallel enclosed between 2 admittance inverters

Practical implementations of impedance/admittance inverters

- Most often the quarter-wave transformer is used

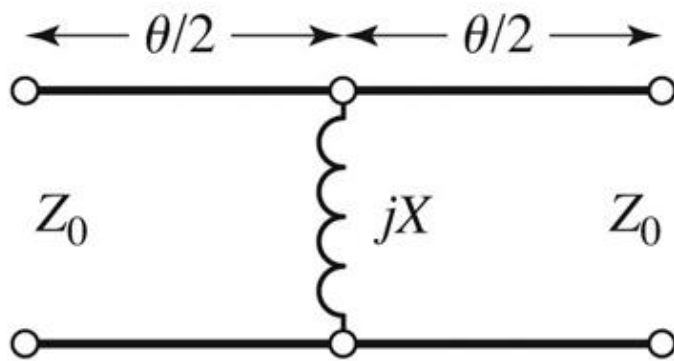


- Implementation with capacitor networks



Practical implementations of impedance/admittance inverters

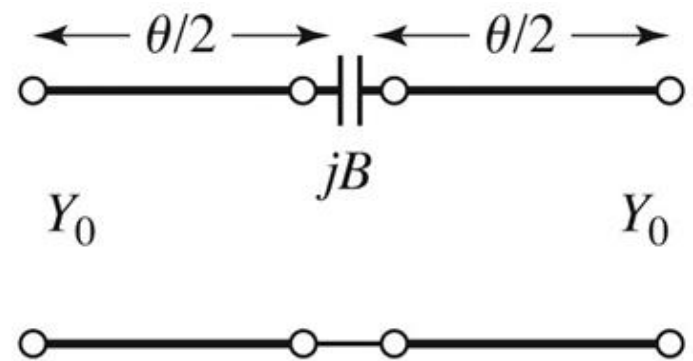
- Implementation with transmission lines and reactive elements



$$K = Z_0 \cdot \tan\left|\frac{\theta}{2}\right|$$

$$X = \frac{K}{1 - \left(\frac{K}{Z_0}\right)^2}$$

$$\theta = -\tan^{-1} \frac{2 \cdot X}{Z_0}$$



$$J = Y_0 \cdot \tan\left|\frac{\theta}{2}\right|$$

$$B = \frac{J}{1 - \left(\frac{J}{Y_0}\right)^2}$$

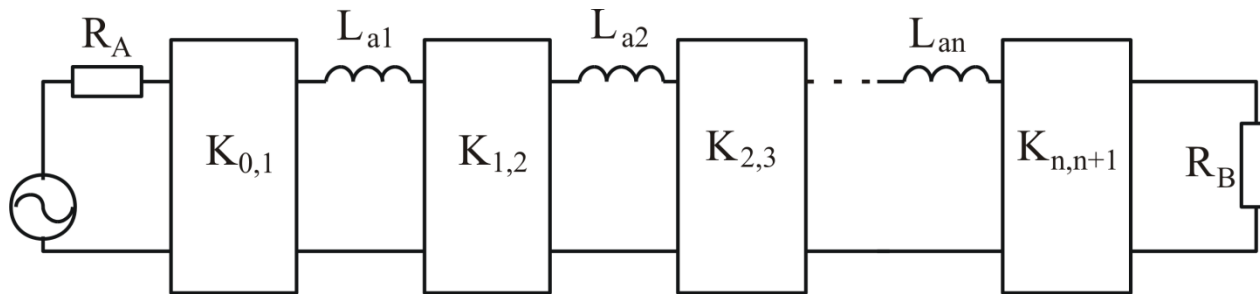
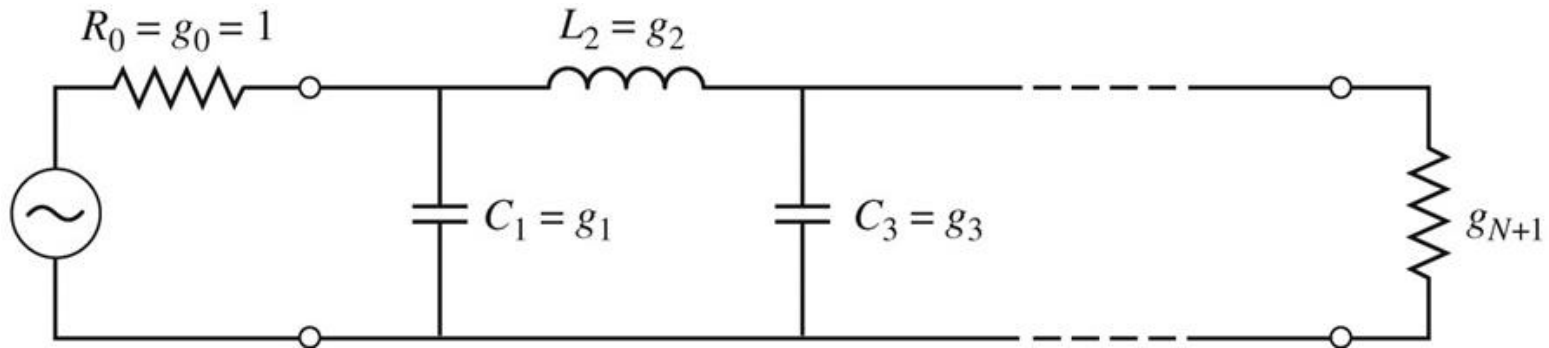
$$\theta = -\tan^{-1} \frac{2 \cdot B}{Y_0}$$

Two red arrows point from the circuit diagrams to the following equation:

$$\theta < 0$$

Prototype filters using inverters

- Using impedance/admittance inverters we can implement prototype filters using a single type of reactive elements
 - Shunt C replaced by series L enclosed between 2 inverters



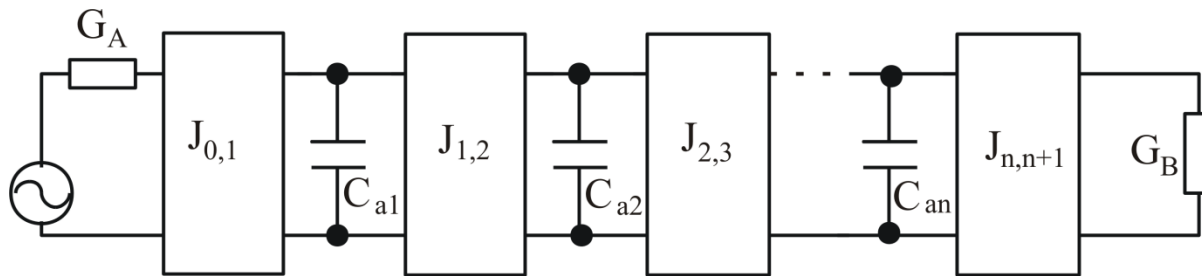
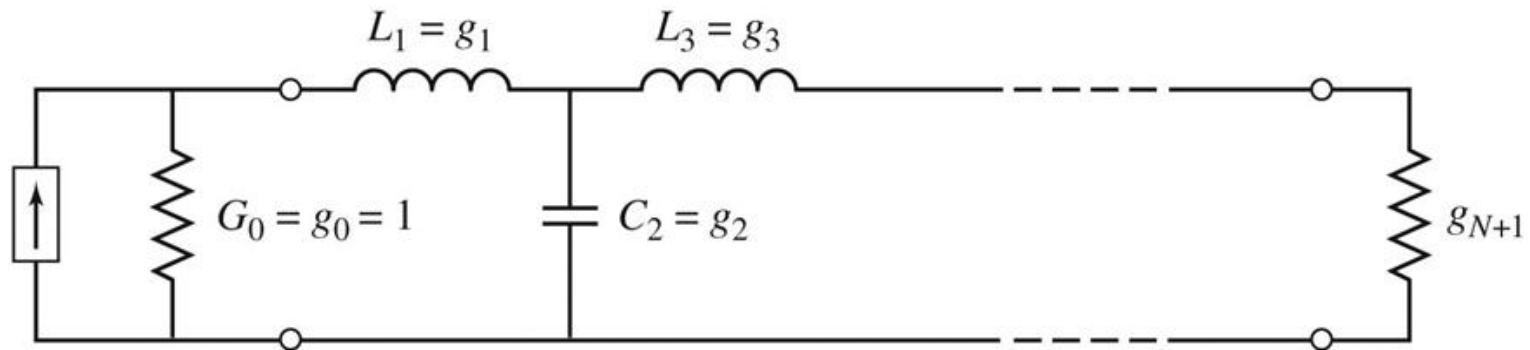
$$K_{0,1} = \sqrt{\frac{R_A \cdot L_{a,1}}{g_0 \cdot g_1}}$$

$$K_{k,k+1} \Big|_{k=1, n-1} = \sqrt{\frac{L_{a,k} \cdot L_{a,k+1}}{g_k \cdot g_{k+1}}}$$

$$K_{n,n+1} = \sqrt{\frac{L_{a,n} \cdot R_B}{g_n \cdot g_{n+1}}}$$

Prototype filters using inverters

- Using impedance/admittance inverters we can implement prototype filters using a single type of reactive elements
 - Series L replaced by shunt C enclosed between 2 inverters



$$J_{0,1} = \sqrt{\frac{G_A \cdot C_{a,1}}{g_0 \cdot g_1}}$$

$$J_{k,k+1} \Big|_{k=1, n-1} = \sqrt{\frac{C_{a,k} \cdot C_{a,k+1}}{g_k \cdot g_{k+1}}}$$

$$J_{n,n+1} = \sqrt{\frac{C_{a,n} \cdot g_B}{g_n \cdot g_{n+1}}}$$

Prototype filters using inverters

- For prototype filters using inverters formulas we have $2 \cdot N + 1$ parameters and $N + 1$ equations (to ensure the equivalence of the 2 schematics) so N parameters can be chosen freely
 - convenient values for the reactance can be chosen, and the required inverters will be computed from the equivalence equations or,
 - convenient inverters can be chosen, and the required reactance values will be computed from the equivalence equations

BPF and BSF using inverters

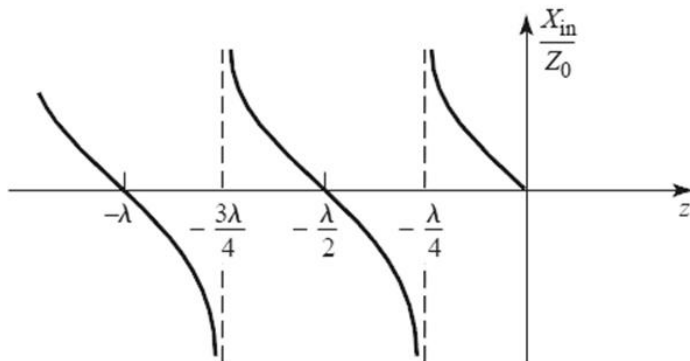
- The same principle can be applied to the BPF and BSF filters, those can be implemented using $N+1$ inverters and N resonators (**series or shunt LC circuits** with resonant frequency ω_o) connected either in series or in parallel enclosed between 2 inverters
 - BPF are implemented with
 - series LC circuits connected in series between inverters
 - shunt LC circuits connected in parallel between inverters
 - BSF are implemented with
 - shunt LC circuits connected in series between inverters
 - series LC circuits connected in parallel between inverters

Lines as resonators

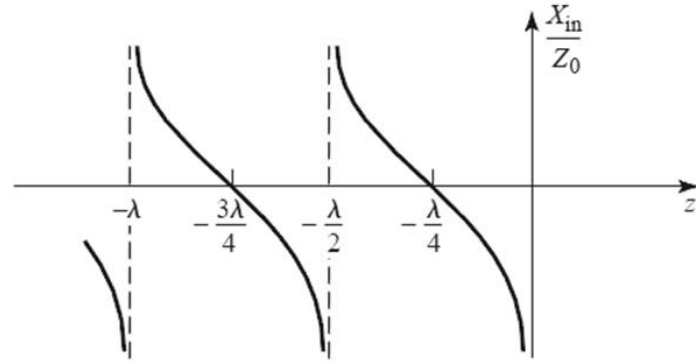
- The impedance of short-circuited or open-circuited line (stub) shows a resonant behavior that can be used to implement required resonators

$$Z_{in} = Z_0 \cdot \frac{Z_L + j \cdot Z_0 \cdot \tan \beta \cdot l}{Z_0 + j \cdot Z_L \cdot \tan \beta \cdot l}$$

$$Z_{in,sc} = j \cdot Z_0 \cdot \tan \beta \cdot l$$

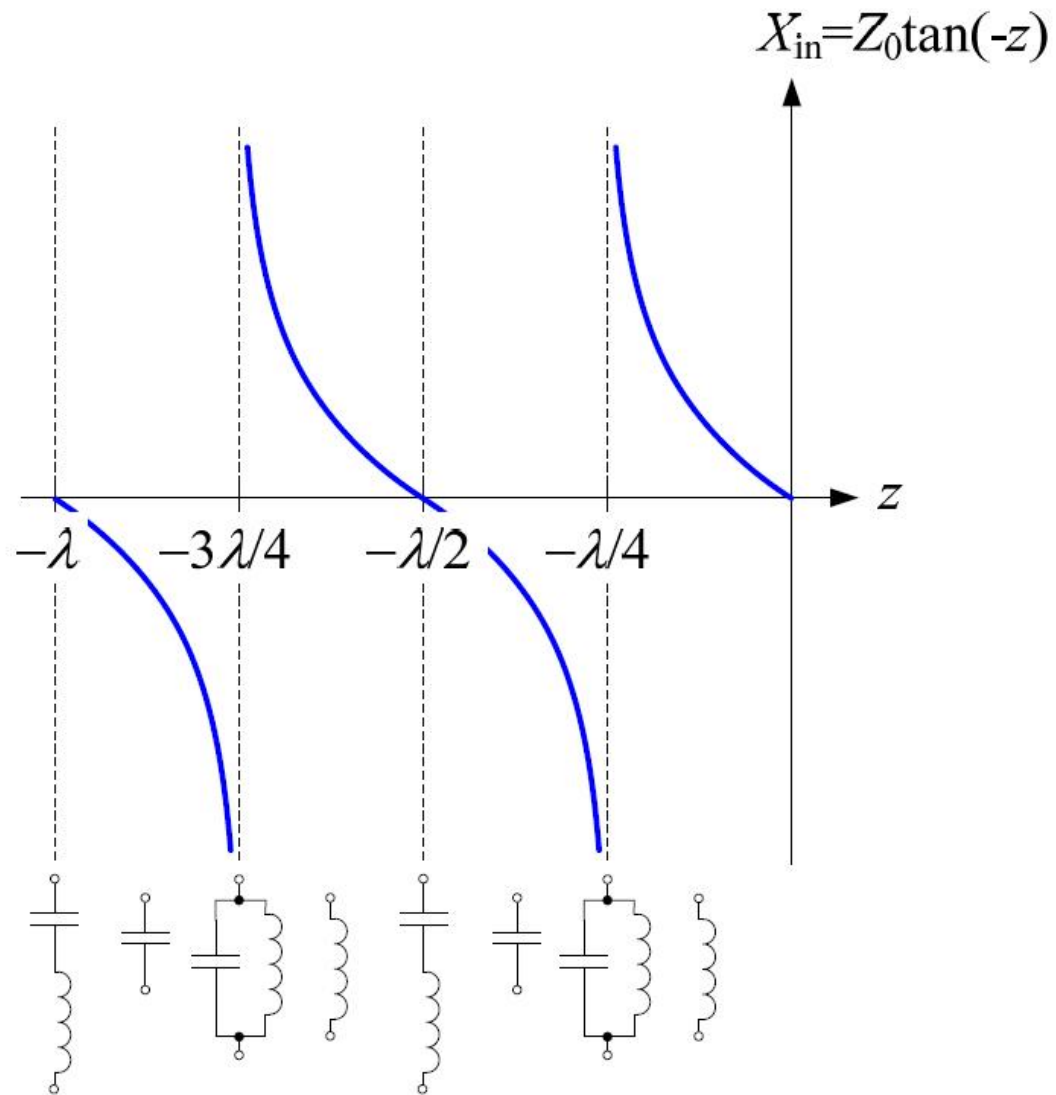


$$Z_{in,oc} = -j \cdot Z_0 \cdot \cot \beta \cdot l$$



Lines as resonators

- Short-circuited line
- For the frequency at which $l = \lambda/4$ (ω_0) the line behaves as a shunt LC resonator circuit
 - the line shows capacitive behavior for lower frequencies ($l > \lambda/4$)
 - the line shows inductive behavior for higher frequencies ($l < \lambda/4$)
- Similar discussion for the open circuited line (equivalent to a series LC resonator around the frequency at which $l = \lambda/4$)



BPF/BSP design formulas

- When the admittance inverters are implemented with quarter-wave transformers with Z_0 characteristic impedance
 - BPF – short-circuited shunt stubs with $l = \lambda/4$

$$Z_{0n} \approx \frac{\pi \cdot Z_0 \cdot \Delta}{4 \cdot g_n}$$

- BSF – open-circuited shunt stubs with $l = \lambda/4$

$$Z_{0n} \approx \frac{4 \cdot Z_0}{\pi \cdot g_n \cdot \Delta}$$

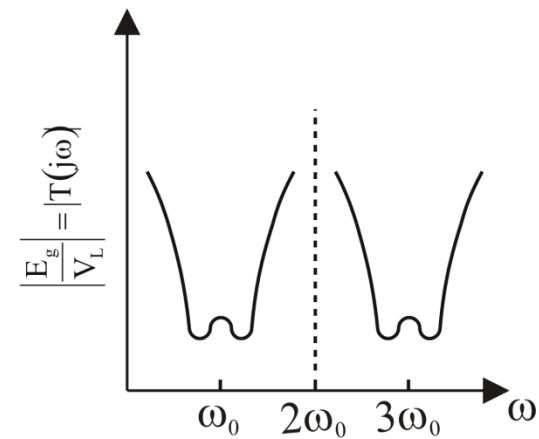
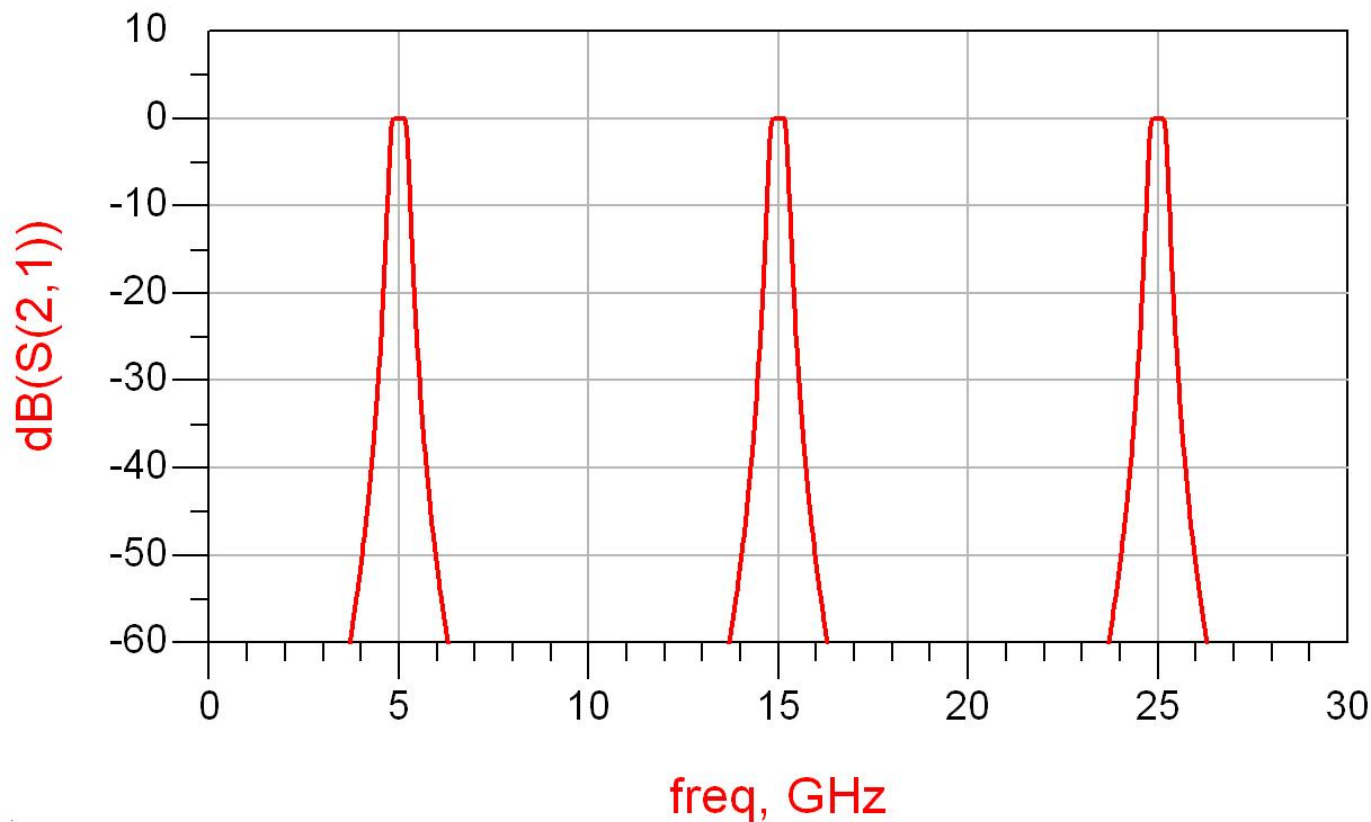
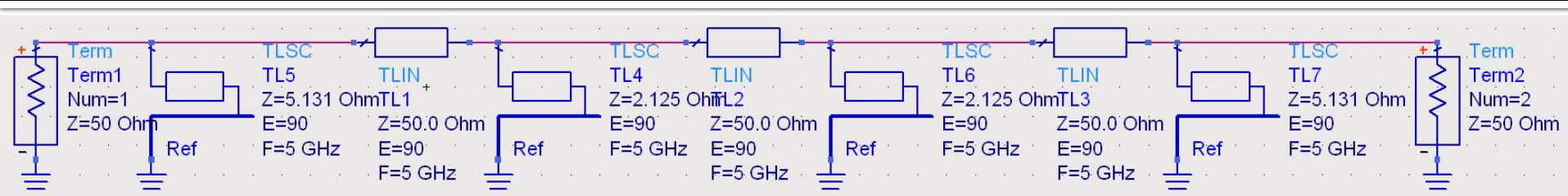
Example

- Similar to a project assignment
- Follows the amplifier designed as in L8
- 4th order bandpass filter, $f_0 = 5\text{GHz}$, fractional bandwidth of the passband 10 %
- maximally flat table or formulas for g_n :

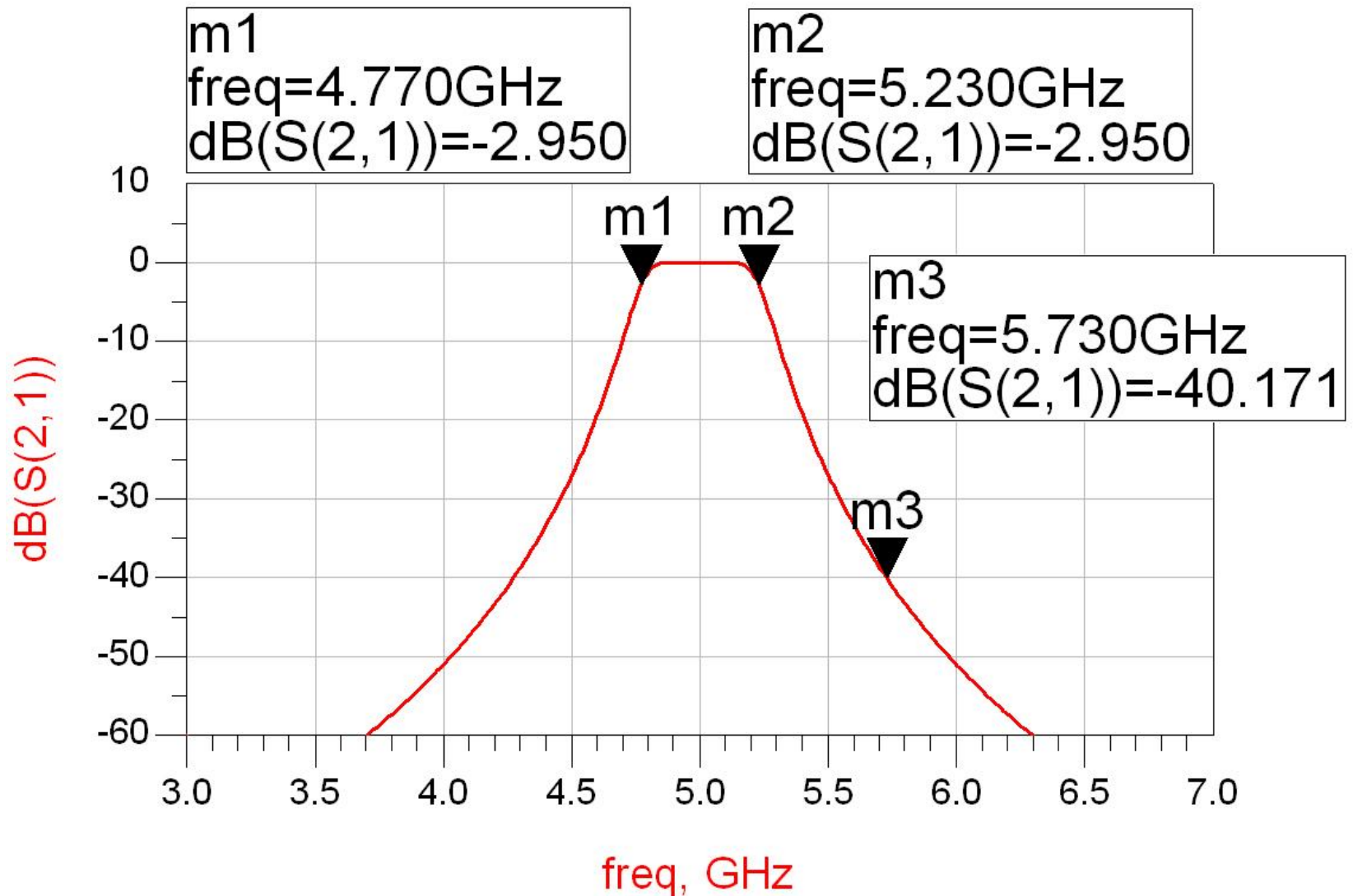
n	g_n	$Z_{0n}(\Omega)$
1	0.7654	5.131
2	1.8478	2.125
3	1.8478	2.125
4	0.7654	5.131

$$Z_{0n} \approx \frac{\pi \cdot Z_0 \cdot \Delta}{4 \cdot g_n}$$

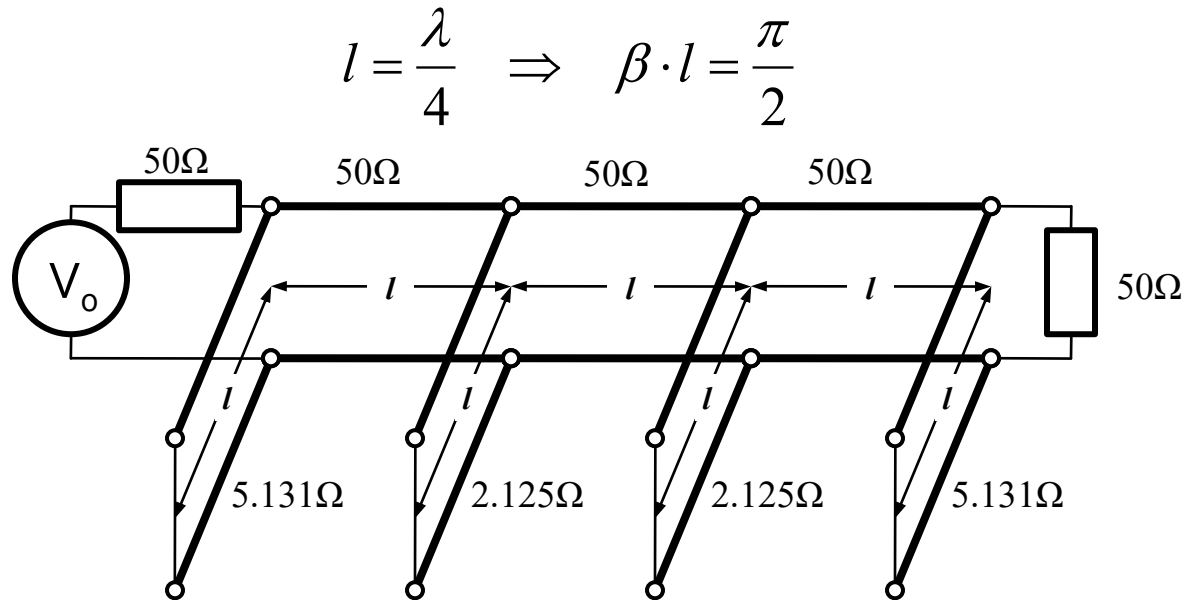
ADS – BPF



ADS – BPF



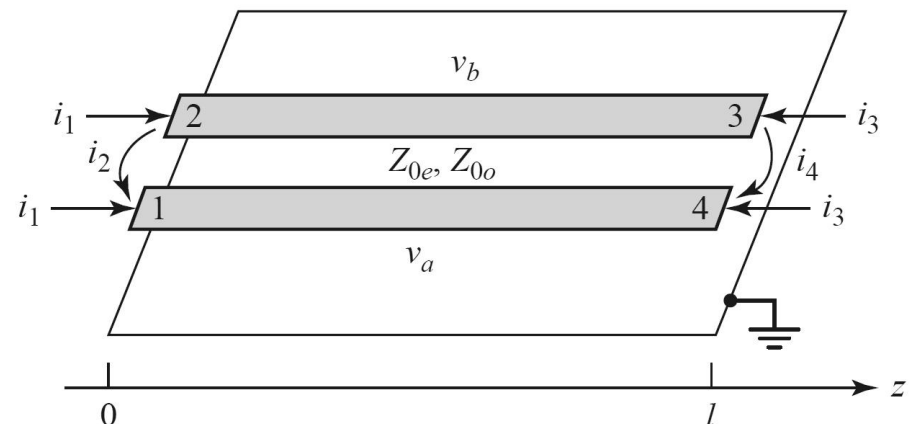
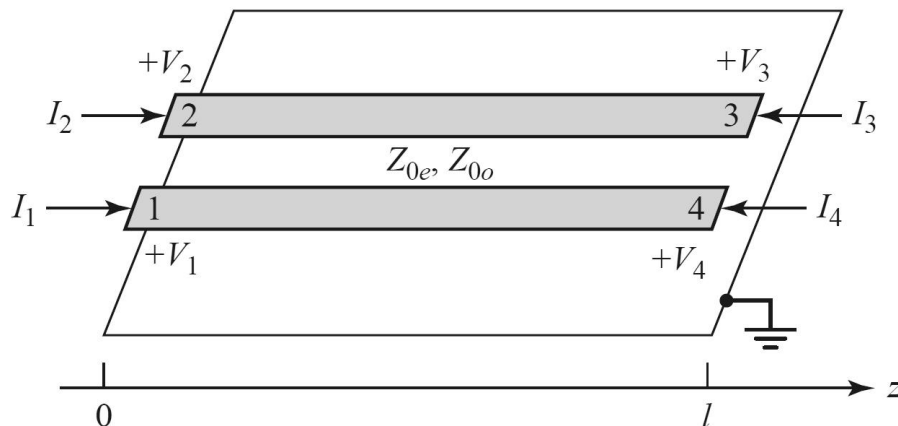
Example



- Disadvantages of the filters using impedance inverters and lines as resonators:
 - short-circuited stubs (via-hole) for BPF
 - often the **characteristic impedances** for the stubs have **values** difficult to implement (2.125Ω)

Coupled Line Filters

- A parallel coupled line section model is obtained by even/odd mode analysis
- Even and odd modes are characterized by the characteristic even/odd mode impedances whose required values will impose the lines' geometry (width / distance between lines, depending on the line technology we use)



Coupled Lines

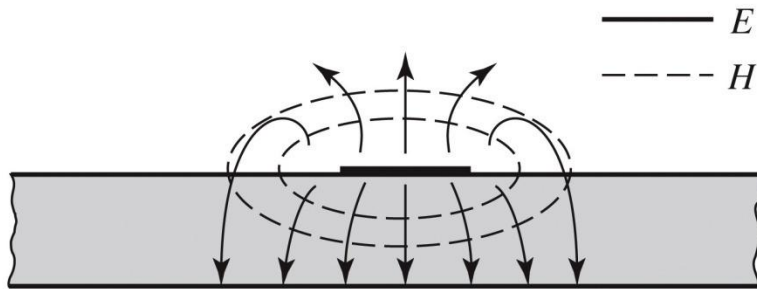
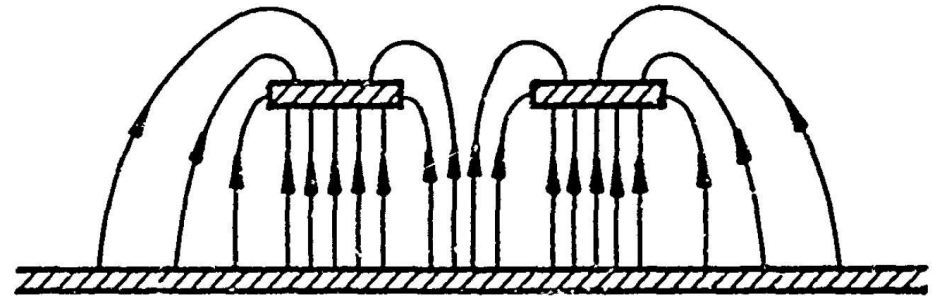
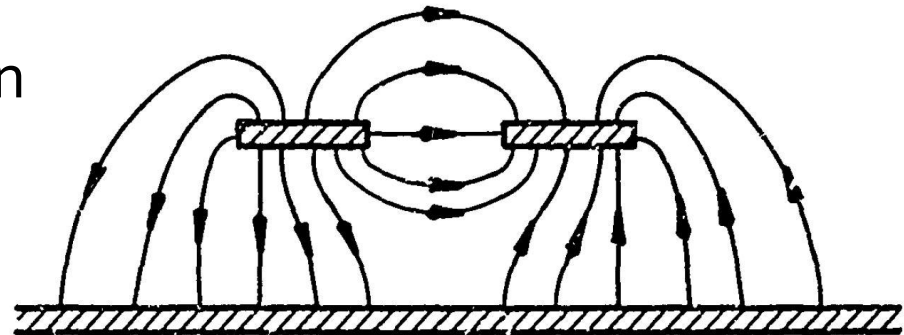


Figure 3.25b
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b) EVEN MODE ELECTRIC FIELD PATTERN (SCHEMATIC)

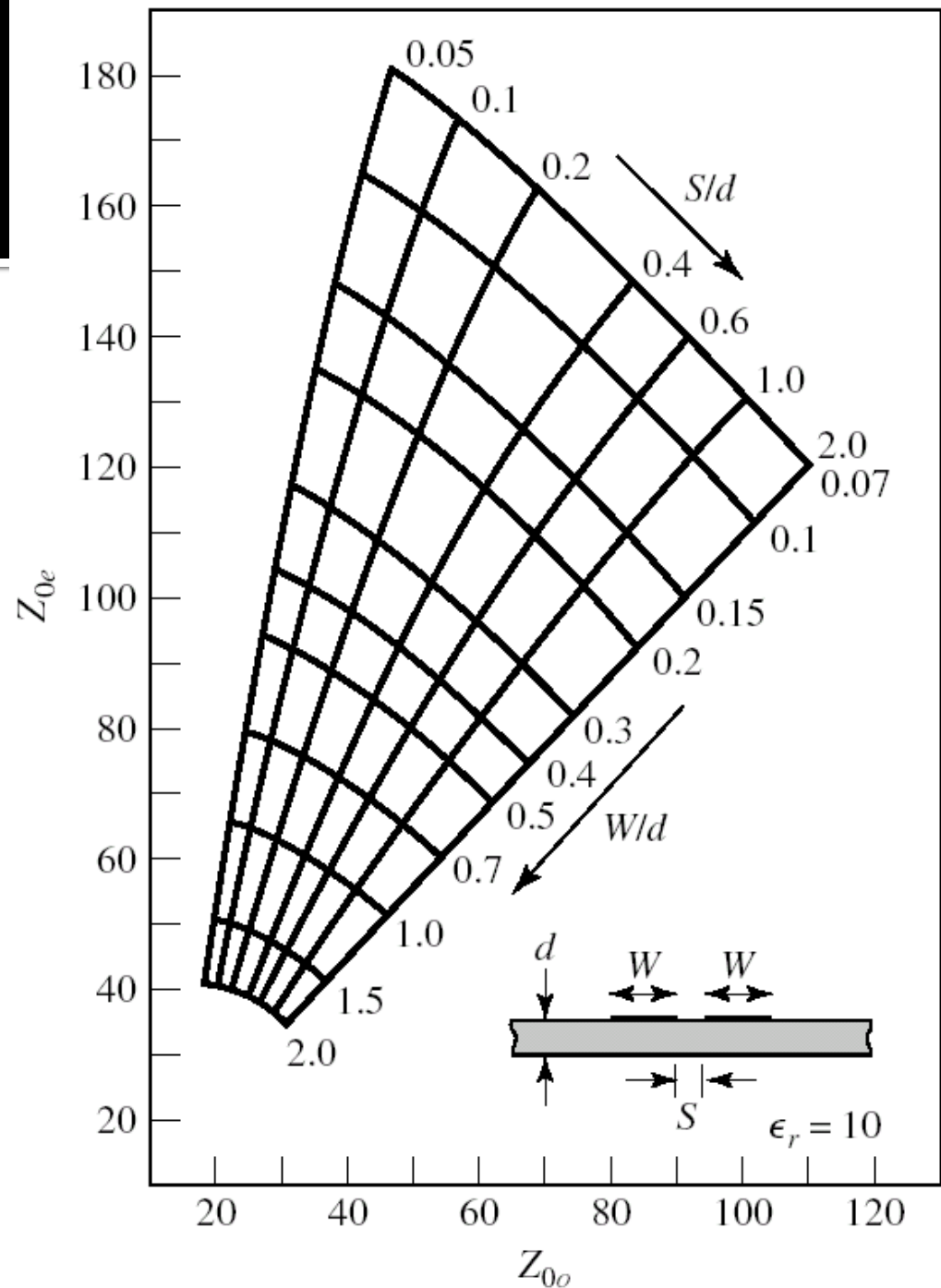


c) ODD MODE ELECTRIC FIELD PATTERN (SCHEMATIC)

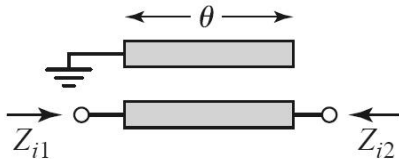
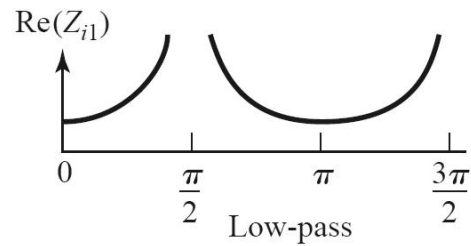
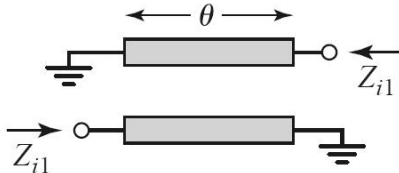
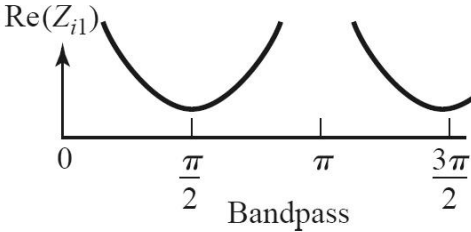
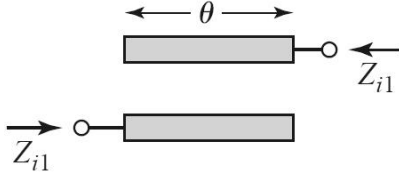
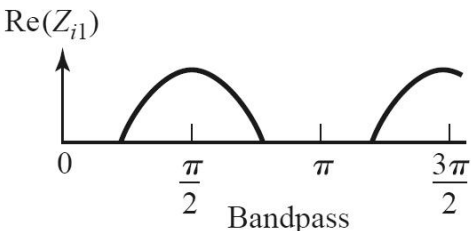
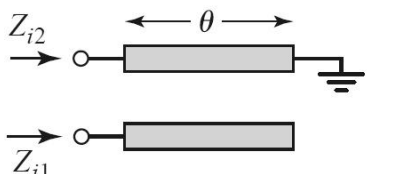
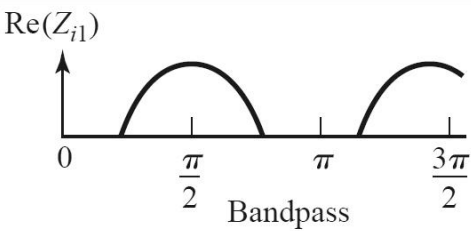
- Even mode - characterizes the common mode signal on the two lines
- Odd mode - characterizes the differential mode signal between the two lines
- Each of the two modes is characterized by **different** characteristic impedances

Even- and odd-mode characteristic impedance

- Even- and odd-mode characteristic impedance design data for coupled microstrip lines on a substrate with $\epsilon_r = 10$.



Coupled Line Filters

Circuit	Image Impedance	Response
	$Z_{i1} = \frac{2Z_{0e}Z_{0o} \cos \theta}{\sqrt{(Z_{0e} + Z_{0o})^2 \cos^2 \theta - (Z_{0e} - Z_{0o})^2}}$ $Z_{i2} = \frac{Z_{0e}Z_{0o}}{Z_{i1}}$	
	$Z_{i1} = \frac{2Z_{0e}Z_{0o} \sin \theta}{\sqrt{(Z_{0e} - Z_{0o})^2 - (Z_{0e} + Z_{0o})^2 \cos^2 \theta}}$	
	$Z_{i1} = \frac{\sqrt{(Z_{0e} - Z_{0o})^2 - (Z_{0e} + Z_{0o})^2 \cos^2 \theta}}{2 \sin \theta}$	
	$Z_{i1} = \frac{\sqrt{Z_{0e}Z_{0o}} \sqrt{(Z_{0e} - Z_{0o})^2 - (Z_{0e} + Z_{0o})^2 \cos^2 \theta}}{(Z_{0e} + Z_{0o}) \sin \theta}$ $Z_{i2} = \frac{Z_{0e}Z_{0o}}{Z_{i1}}$	

Coupled Line Filters

- Bandpass filter with resonance at $\theta = \pi/2$ ($l = \lambda/4$)

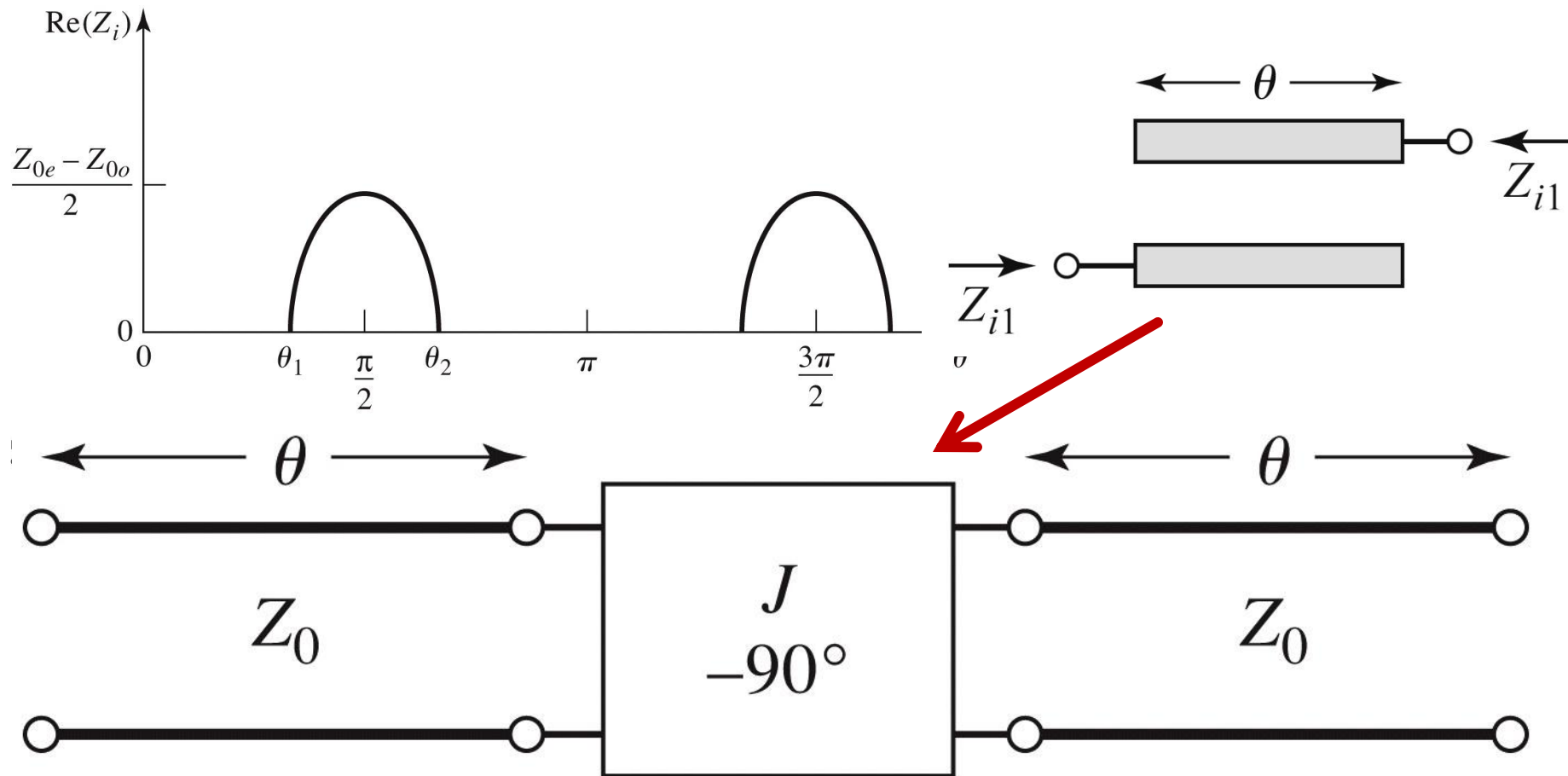
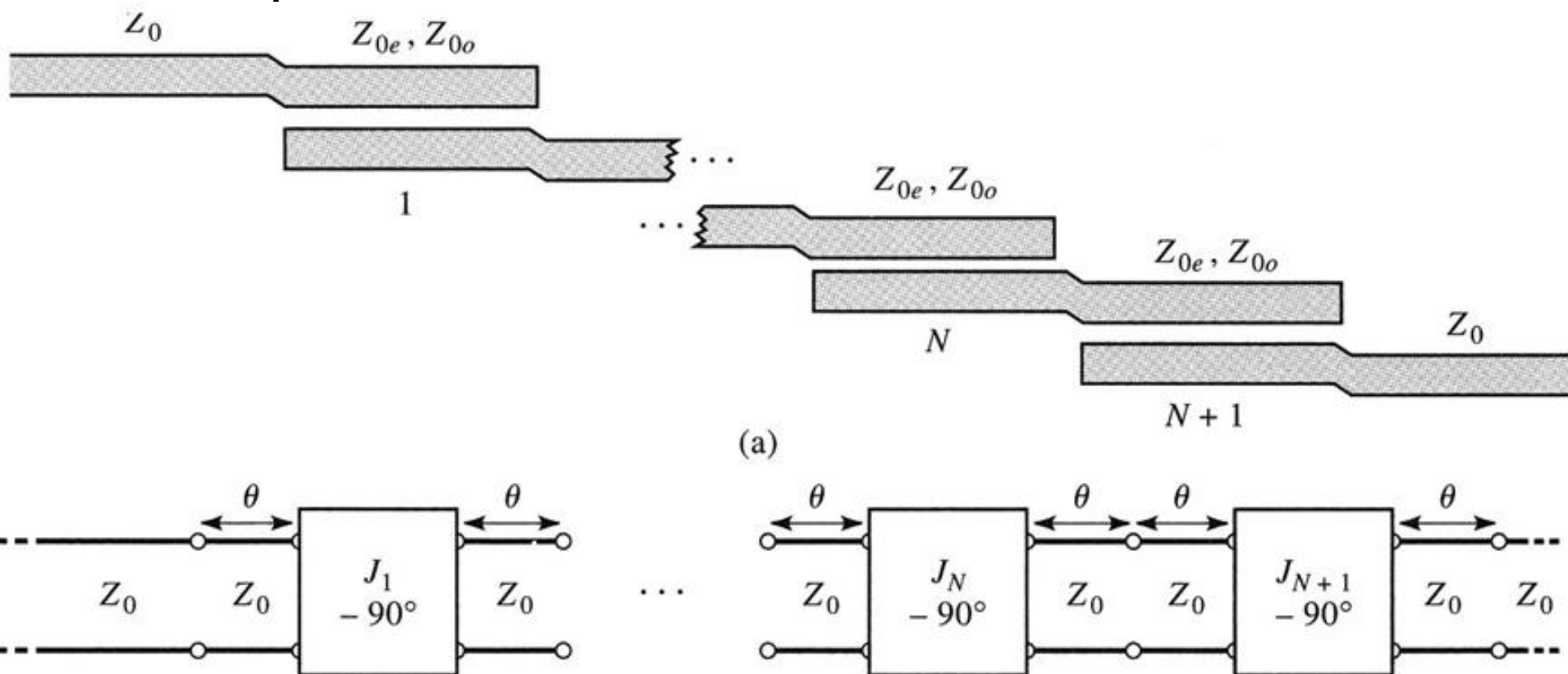


Figure 8.44

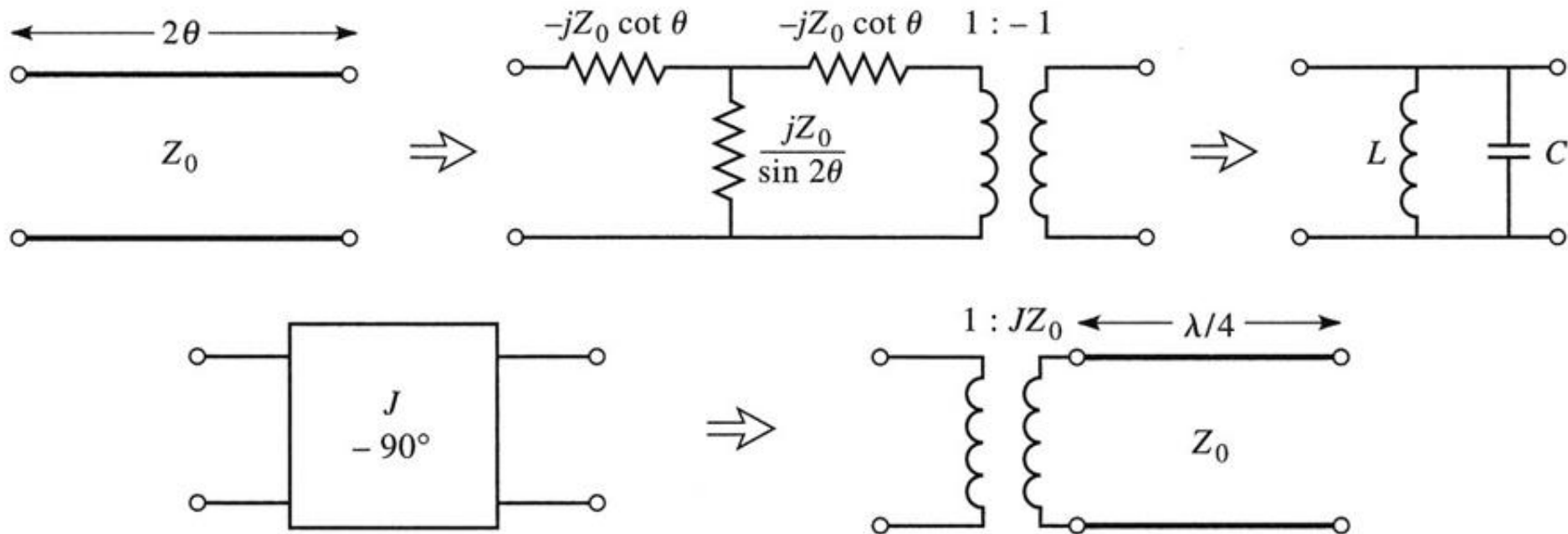
Coupled Line Filters

- We get a N^{th} order filter with $N+1$ parallel coupled line section



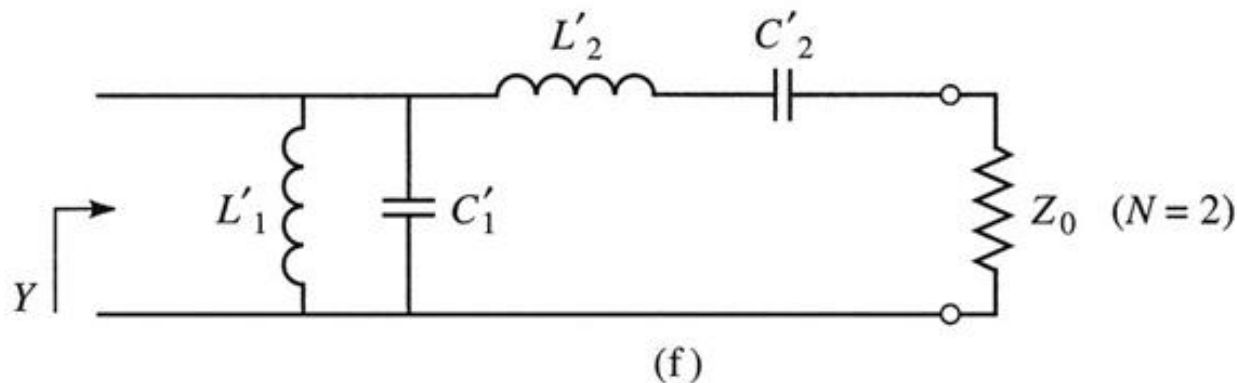
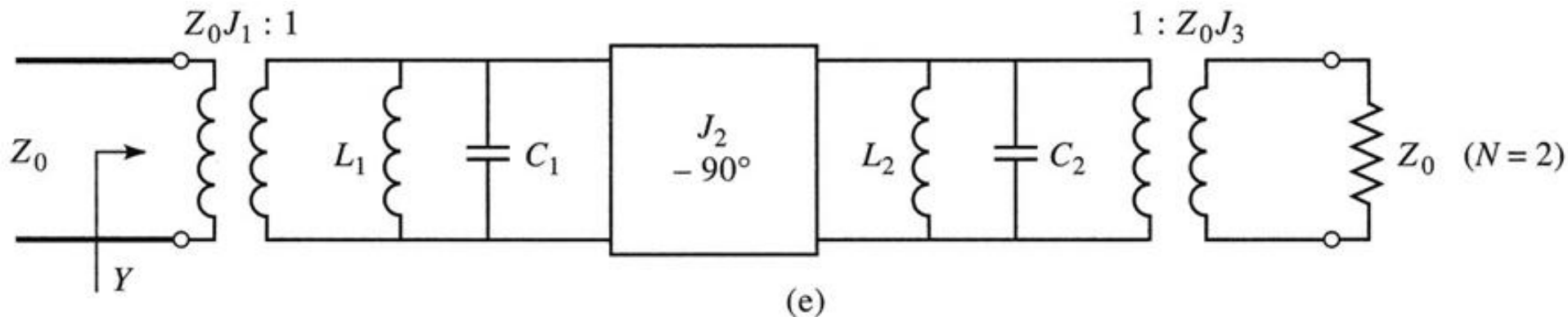
Coupled Line Filters

- Equivalent circuits for
 - transmission lines of length 2θ
 - admittance inverters



Coupled Line Filters N=2

- We get a 2nd order BPF behavior with 3 coupled lines sections



Coupled Line Filters design formulas

- Compute the inverters from prototype parameters

$$Z_0 \cdot J_1 = \sqrt{\frac{\pi \cdot \Delta}{2 \cdot g_1}} \quad Z_0 \cdot J_n = \frac{\pi \cdot \Delta}{2 \cdot \sqrt{g_{n-1} \cdot g_n}}, n = \overline{2, N} \quad Z_0 \cdot J_{N+1} = \sqrt{\frac{\pi \cdot \Delta}{2 \cdot g_N \cdot g_{N+1}}}$$

- Compute coupled line parameters Z_{oe}/Z_{oo} (all of length $l = \lambda/4$)

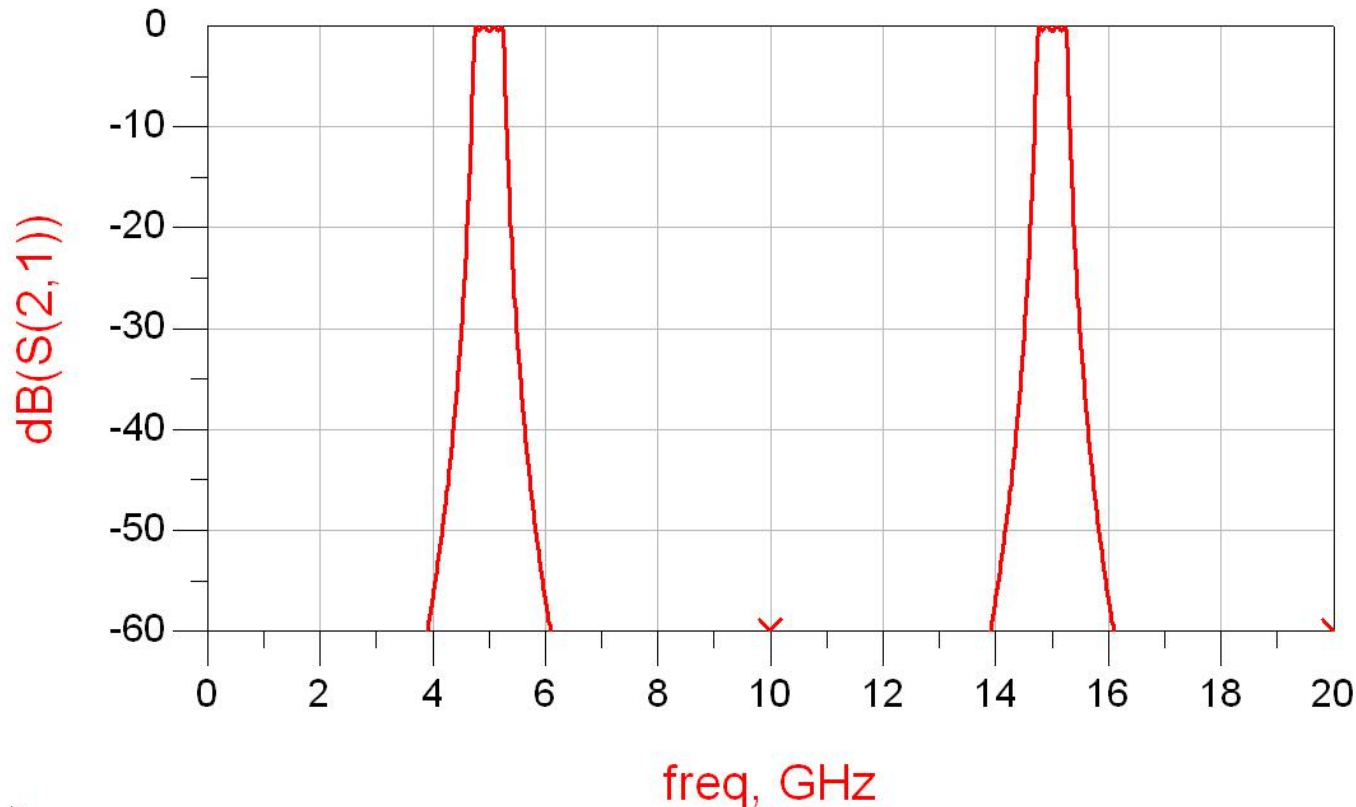
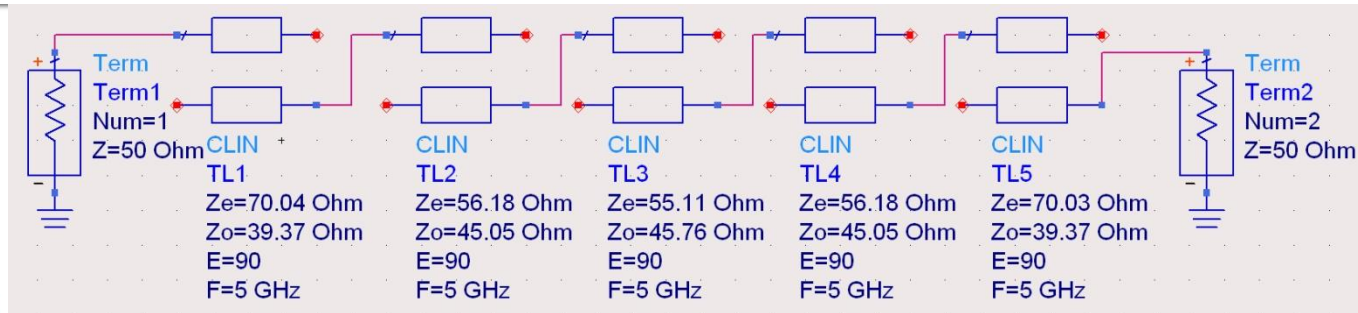
$$\begin{aligned} Z_{oe,n} &= Z_0 \cdot \left[1 + J_n \cdot Z_0 + (J_n \cdot Z_0)^2 \right] \\ Z_{oo,n} &= Z_0 \cdot \left[1 - J_n \cdot Z_0 + (J_n \cdot Z_0)^2 \right] \end{aligned} \quad n = \overline{1, N+1}$$

Example

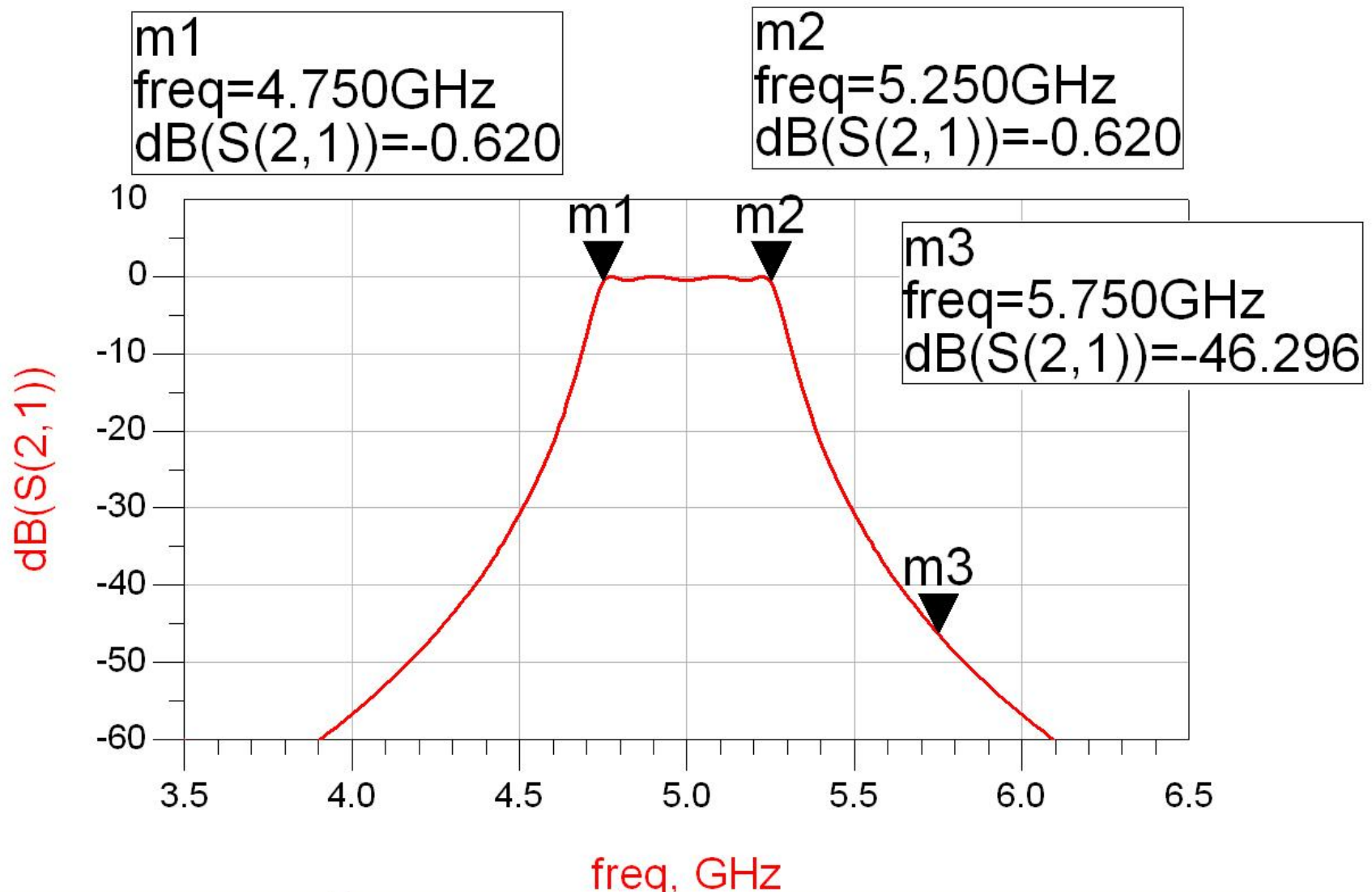
- Similar to a project assignment
- Follows the amplifier designed as in L10
- 4th order bandpass filter, $f_0 = 5\text{GHz}$, fractional bandwidth of the passband 10 %
- 0.5dB equal-ripple table for g_n followed by filter design formulas

n	g	$Z_0 J_n$	$Z_0 \epsilon$	$Z_0 \omega$
1	1.6703	0.306664	70.04	39.37
2	1.1926	0.111295	56.18	45.05
3	2.3661	0.09351	55.11	45.76
4	0.8419	0.111294	56.18	45.05
5	1.9841	0.306653	70.03	39.37

ADS – coupled line BPF



ADS – coupled line BPF



Examples

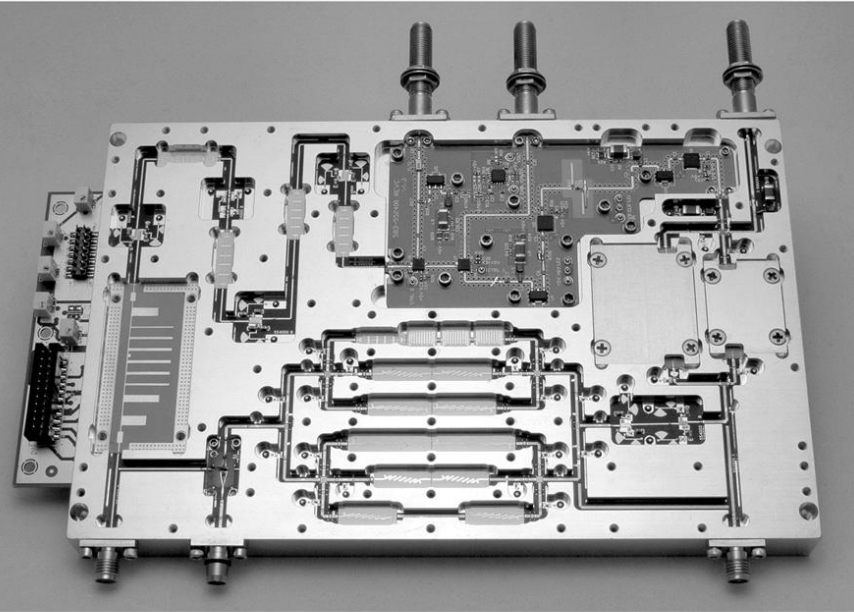
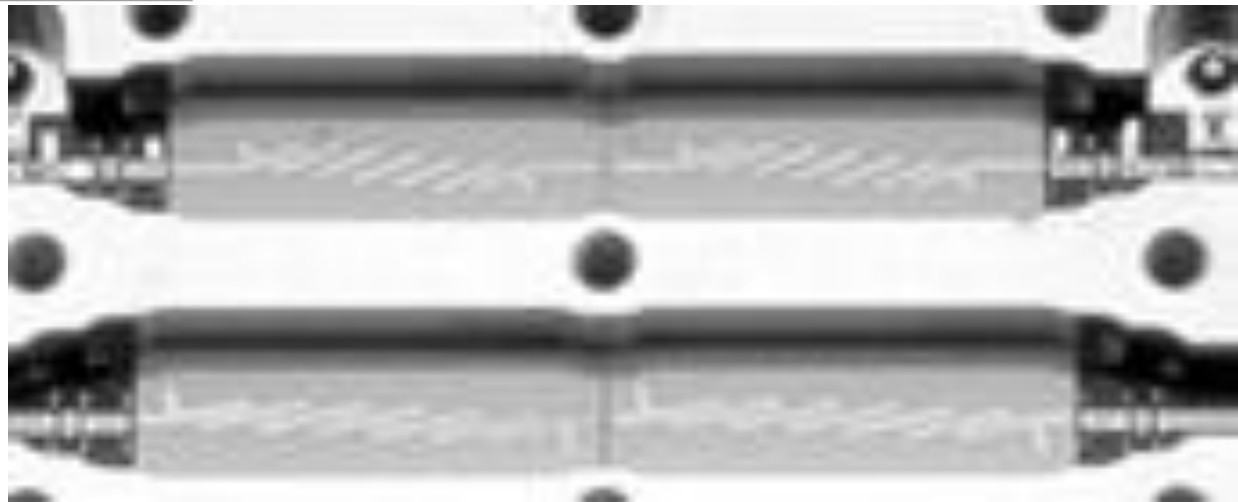
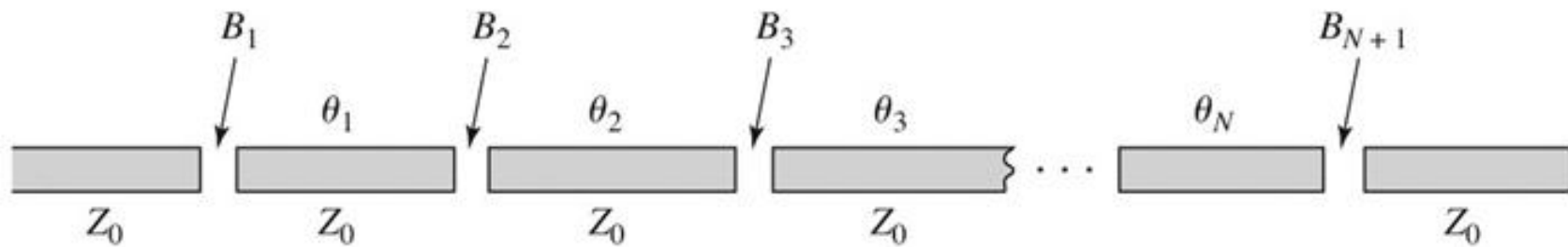


Figure 8.55
Courtesy of LNX Corporation, Salem, N.H.

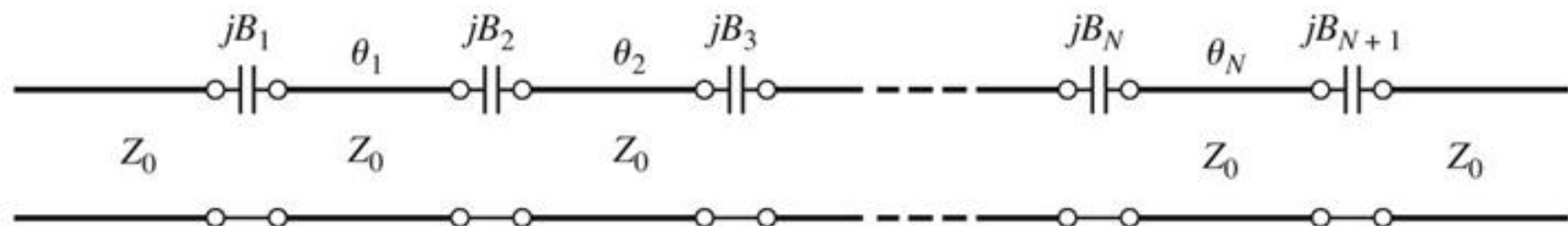


Bandpass Filters Using Capacitively Coupled Series Resonators

- The gaps between the resonators ($\sim \lambda/2$) generate a capacitive coupling between two resonators and can be approximated as series capacitors



(a)



(b)

Bandpass Filters Using Capacitively Coupled Series Resonators

- From the real physical length of the resonators, some part is used implement a admittance inverter (the remainder $\phi=\pi$, $l=\lambda/2$, resonator)

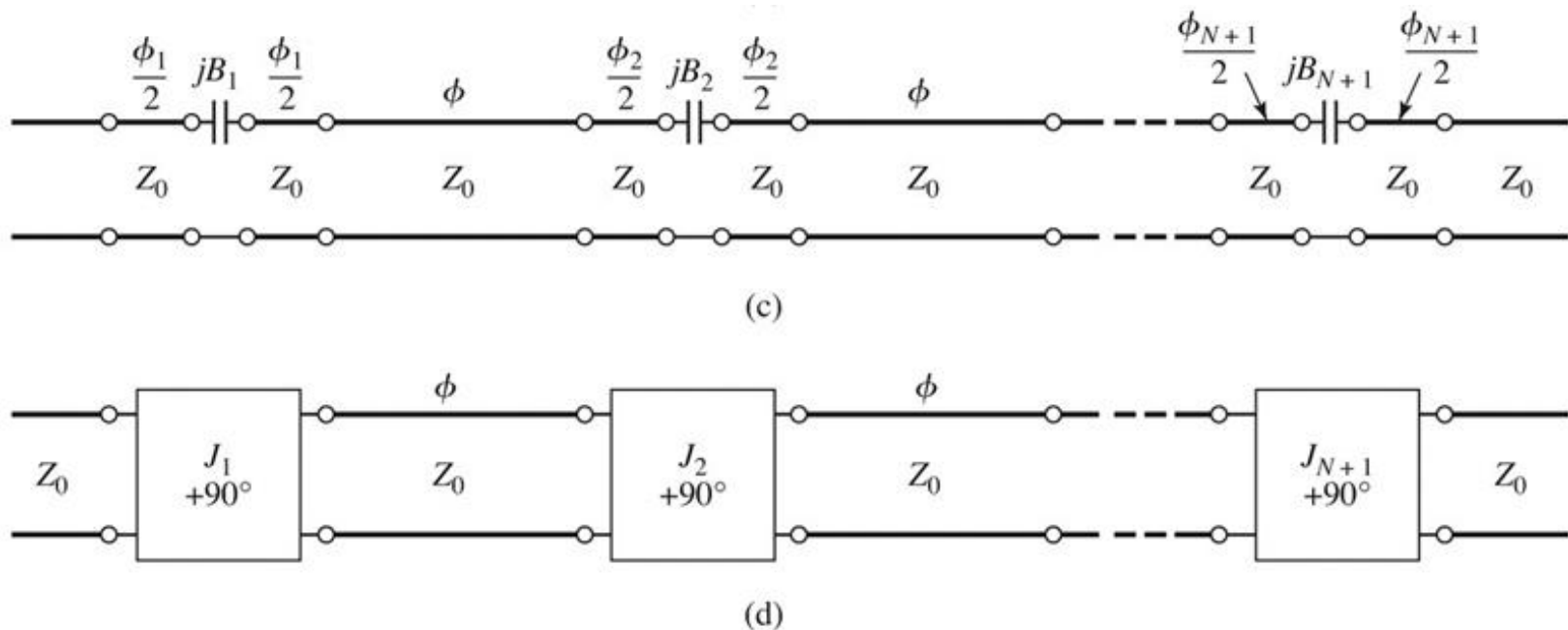


Figure 8.50

Bandpass Filters Using Capacitively Coupled Series Resonators design

- Compute the inverters (similar to coupled lines)

$$Z_0 \cdot J_1 = \sqrt{\frac{\pi \cdot \Delta}{2 \cdot g_1}} \quad Z_0 \cdot J_n = \frac{\pi \cdot \Delta}{2 \cdot \sqrt{g_{n-1} \cdot g_n}}, n = \overline{2, N} \quad Z_0 \cdot J_{N+1} = \sqrt{\frac{\pi \cdot \Delta}{2 \cdot g_N \cdot g_{N+1}}}$$

- Compute capacitive susceptances

$$B_n = \frac{J_n}{1 - (Z_0 \cdot J_n)^2}, n = \overline{1, N+1}$$

- Compute the line lengths that must be “borrowed” to implement the inverters

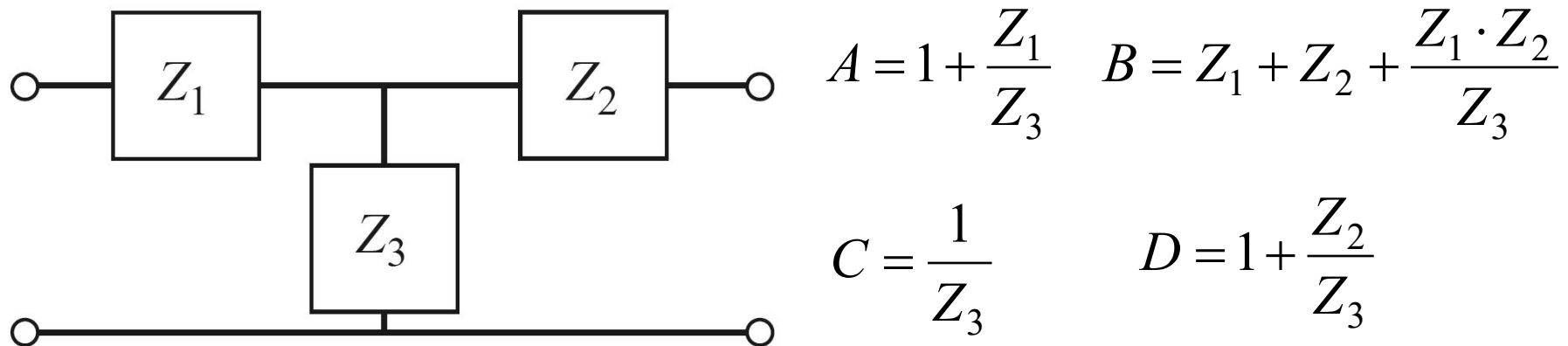
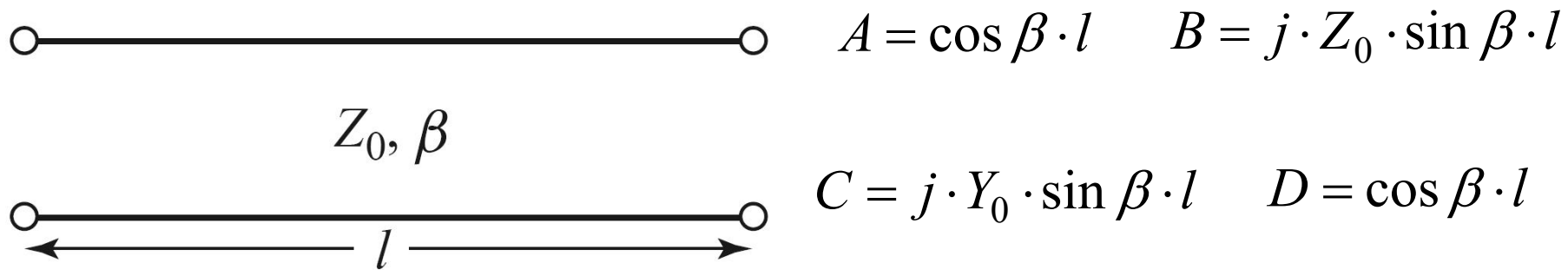
$$\phi_n = -\tan^{-1}(2 \cdot Z_0 \cdot B_n), n = \overline{1, N+1} \quad \phi_n < 0, n = \overline{1, N+1}$$

- Compute the actual length of the lines ($\lambda/2$ + borr.)

$$\theta_i = \pi + \frac{1}{2} \cdot (\phi_i + \phi_{i+1}) = \pi - \frac{1}{2} \cdot [\tan^{-1}(2 \cdot Z_0 \cdot B_i) + \tan^{-1}(2 \cdot Z_0 \cdot B_{i+1})], i = \overline{1, N}$$

Equivalent circuits for short sections of transmission lines

- ABCD matrix (L5)
- short line, model with lumped elements is valid



Equivalent circuits for short sections of transmission lines

- The shunt element is capacitive

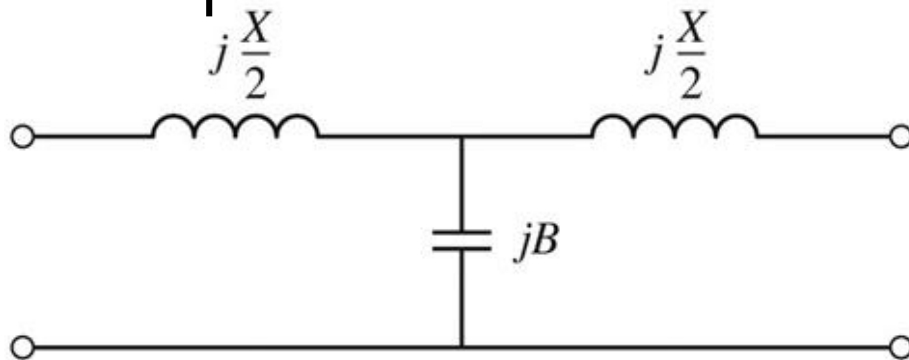
$$Z_3 = \frac{1}{j \cdot Y_0 \cdot \sin \beta \cdot l}$$

- Series elements are equal, and inductive

$$\cos \beta \cdot l = 1 + \frac{Z_1}{Z_3} = 1 + \frac{Z_2}{Z_3}$$

$$Z_1 = Z_2 = Z_3 \cdot (\cos \beta \cdot l - 1) = -j \cdot Z_0 \cdot \frac{\cos \beta \cdot l - 1}{\sin \beta \cdot l} = j \cdot Z_0 \cdot \tan \frac{\beta \cdot l}{2}$$

- Equivalent circuit

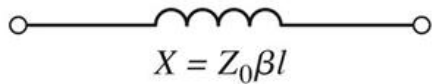


$$\frac{X}{2} = Z_0 \cdot \tan \frac{\beta \cdot l}{2}$$
$$B = \frac{1}{Z_0} \cdot \sin \beta \cdot l$$

Equivalent circuits for short sections of transmission lines

- depending on the characteristic impedance:

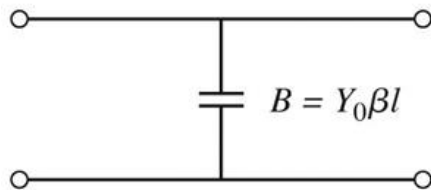
- high $Z_0 \gg$



$$X \cong Z_0 \cdot \beta \cdot l \quad \beta \cdot l < \frac{\pi}{4} \quad Z_0 = Z_h$$



- low $Z_0 \ll$



$$B \cong Y_0 \cdot \beta \cdot l \quad \beta \cdot l < \frac{\pi}{4} \quad Z_0 = Z_l$$

Stepped-impedance low-pass filter

- Series L, shunt C, we realize low-pass filters
- We use

- lines with high characteristic impedance to implement an series inductor

$$\beta \cdot l = \frac{L \cdot R_0}{Z_h}$$

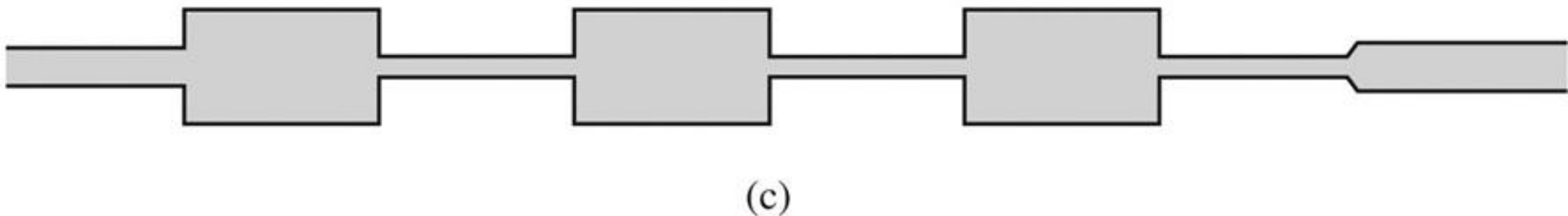
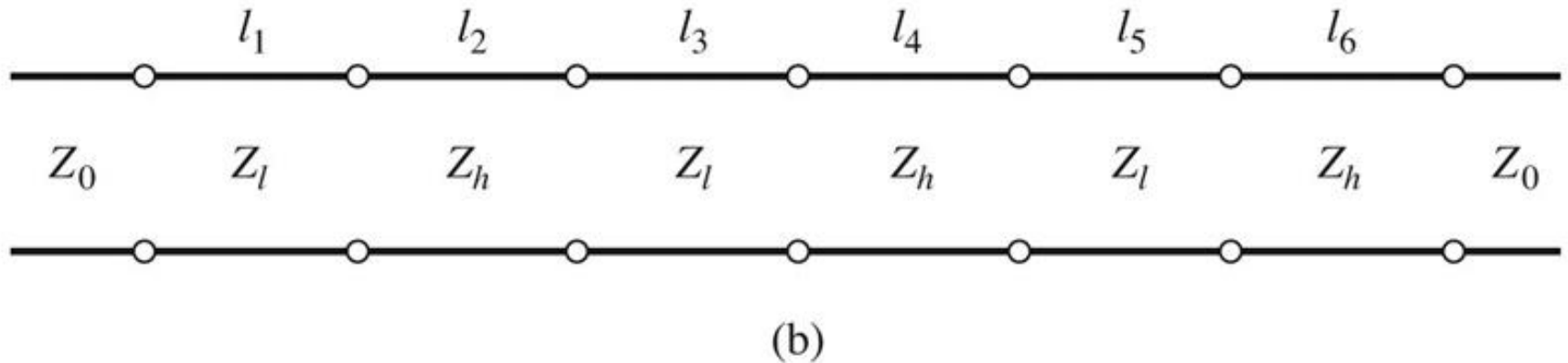
- lines with low characteristic impedance to implement a shunt capacitor

$$\beta \cdot l = \frac{C \cdot Z_l}{R_0}$$

- usually the highest and lowest characteristic impedance that can be practically fabricated

Stepped-impedance LPF

- Not all the lines will result with the same length so the filter response is not periodic in frequency

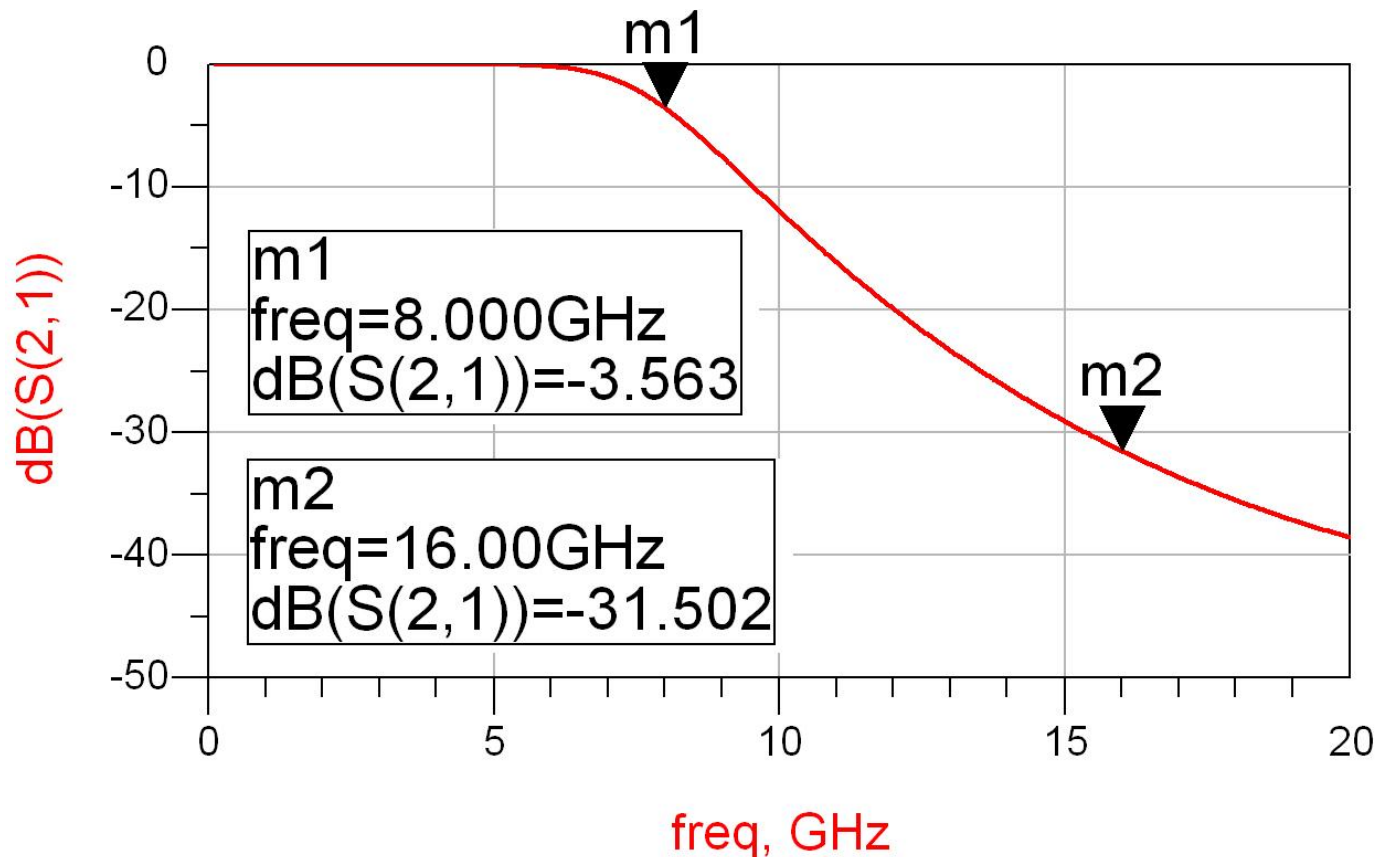
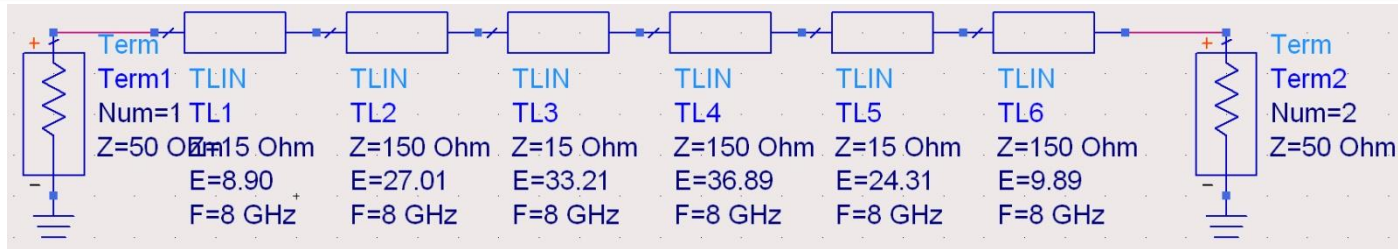


Example

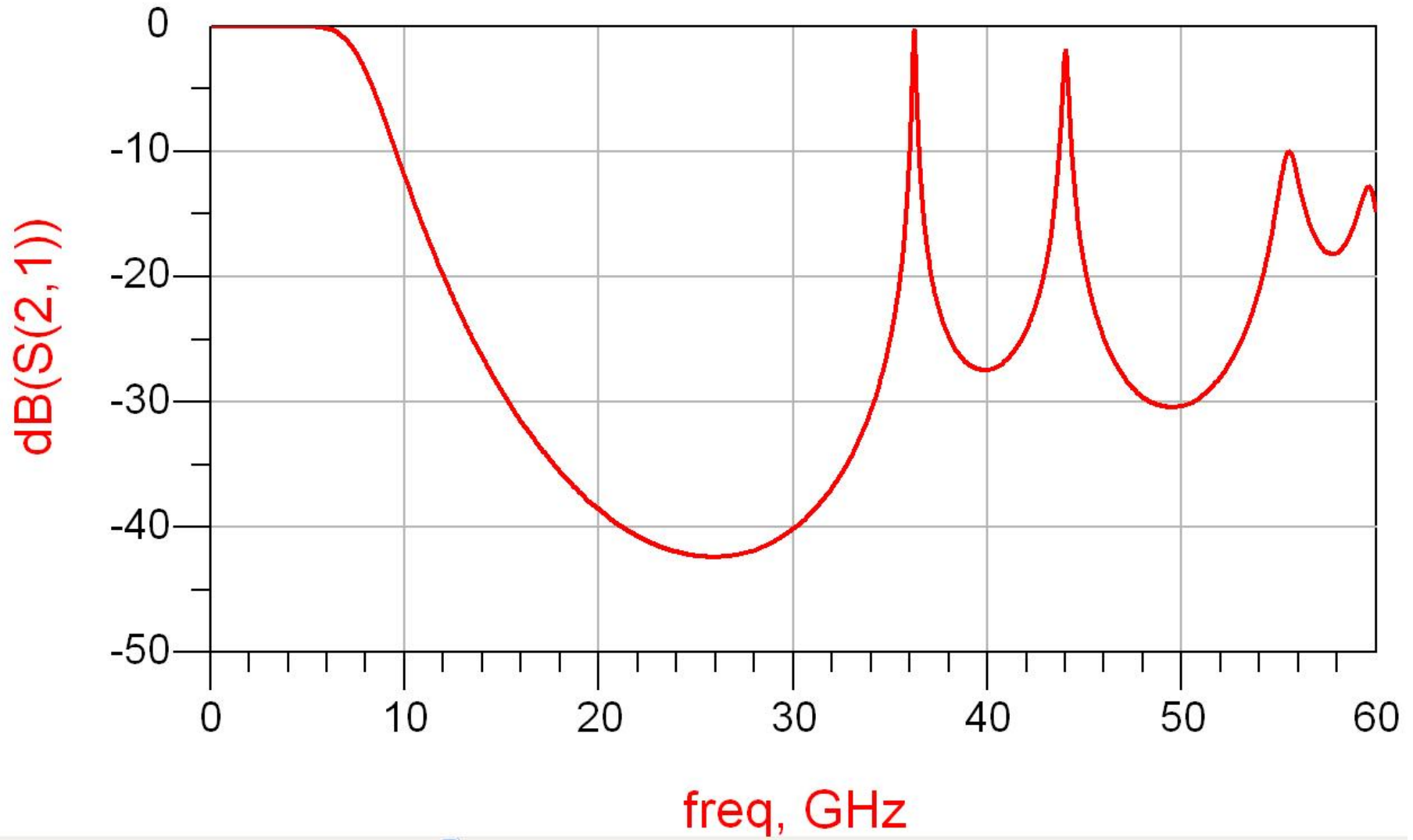
- LPF with 8GHz cutoff frequency, 6th order.
Maximum realizable impedance is 150Ω and lowest 15Ω .

n	g_n	L/C_n	Z	$\theta_n[\text{rad}]$	$\theta_n[^\circ]$
1	0.5176	0.206pF	15	0.155	8.90
2	1.4142	1.407nH	150	0.471	27.01
3	1.9318	0.769pF	15	0.580	33.21
4	1.9318	1.922nH	150	0.644	36.89
5	1.4142	0.563pF	15	0.424	24.31
6	0.5176	0.515nH	150	0.173	9.89

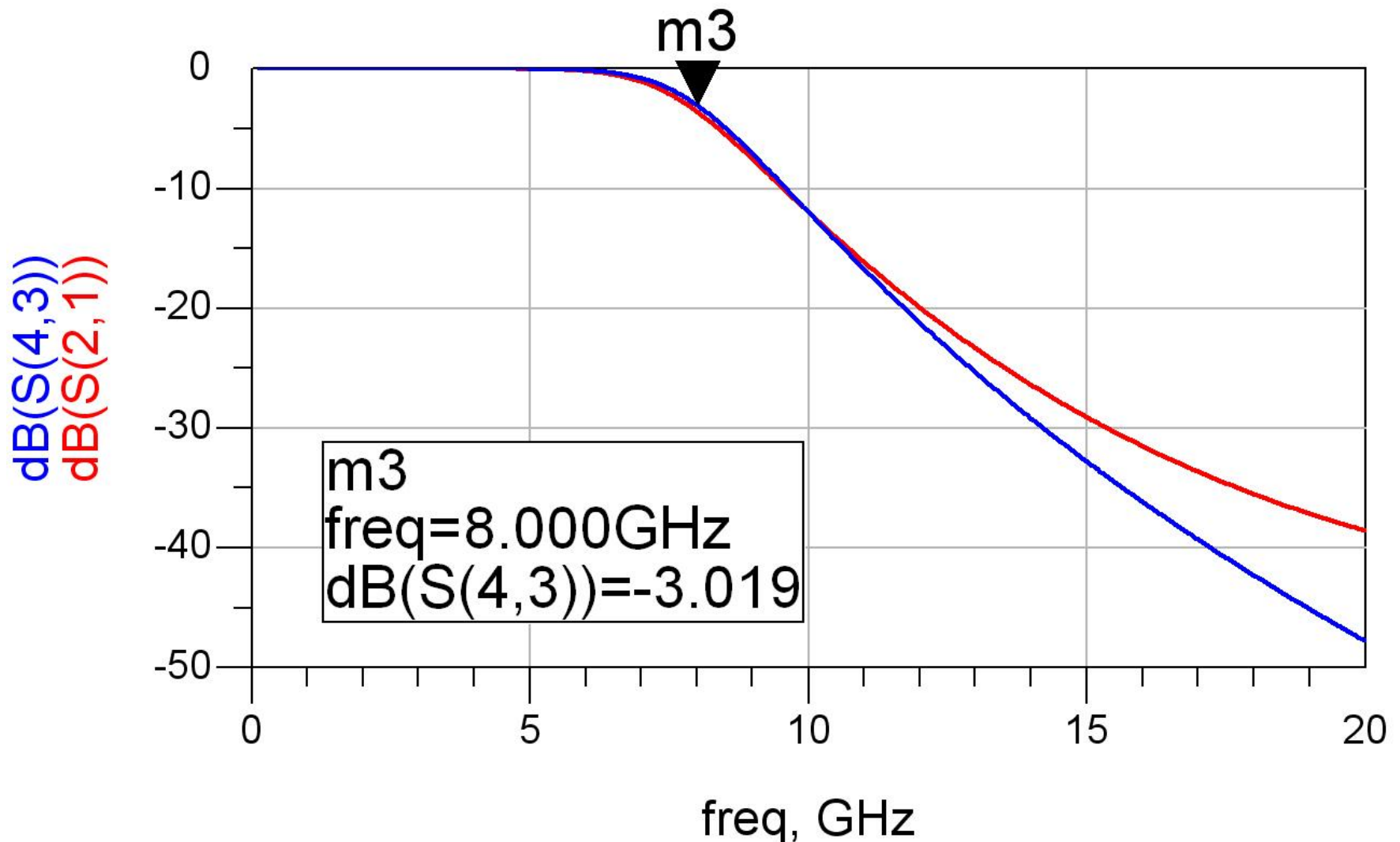
ADS – Stepped-impedance LPF



ADS – Stepped-impedance LPF



ADS – Stepped-impedance LPF – compared with lumped elements



Examples

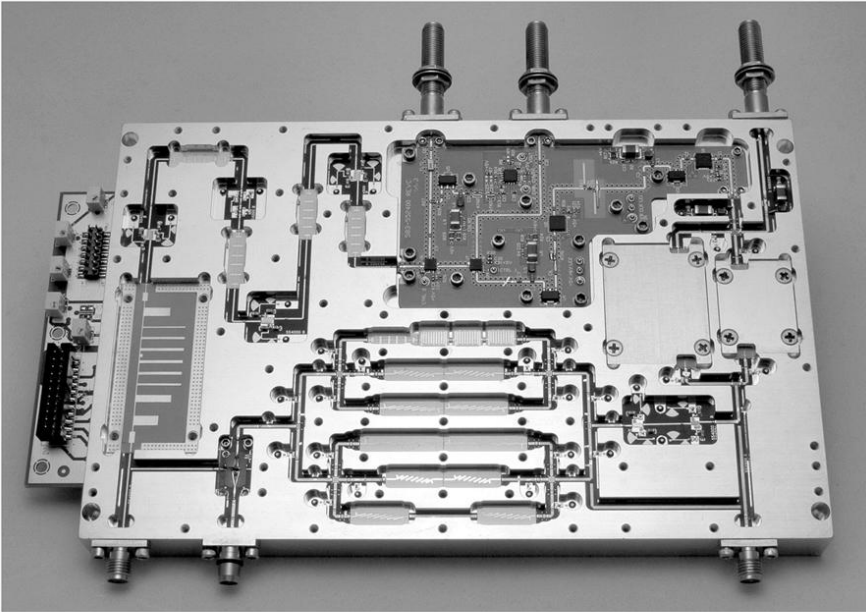
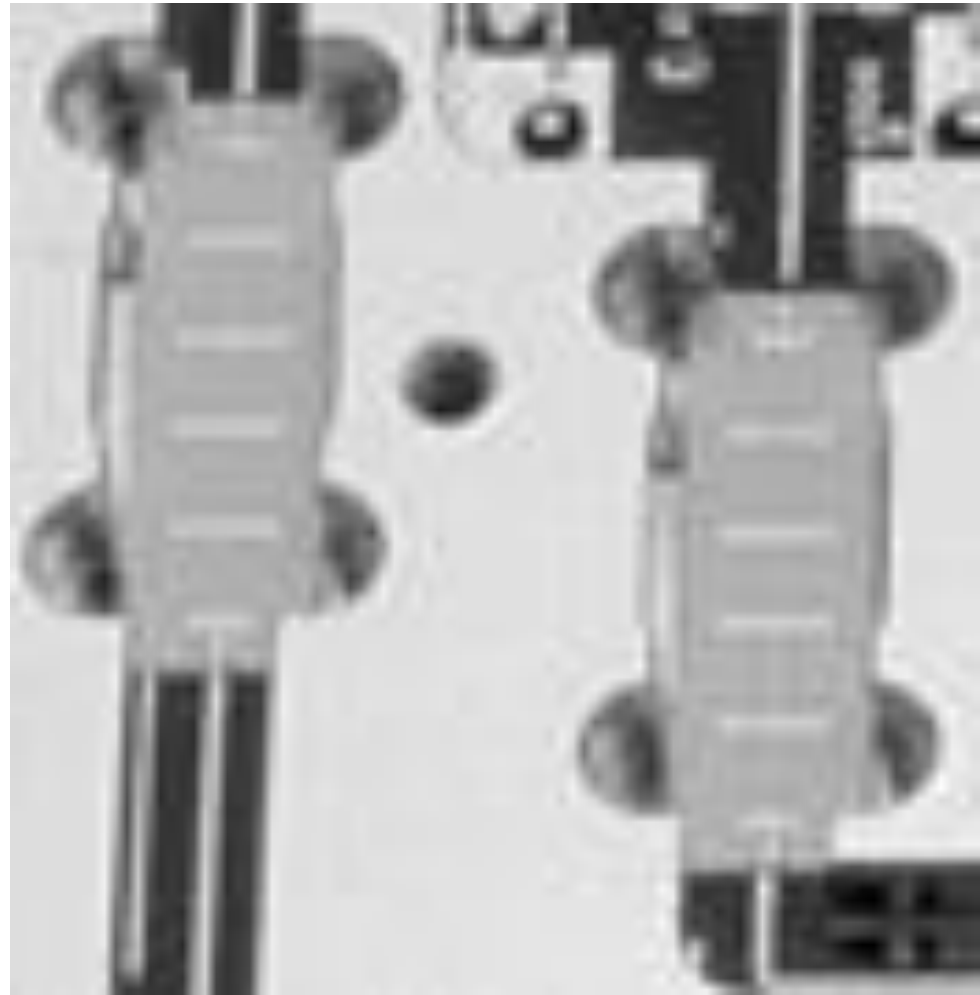


Figure 8.55
Courtesy of LNX Corporation, Salem, N.H.



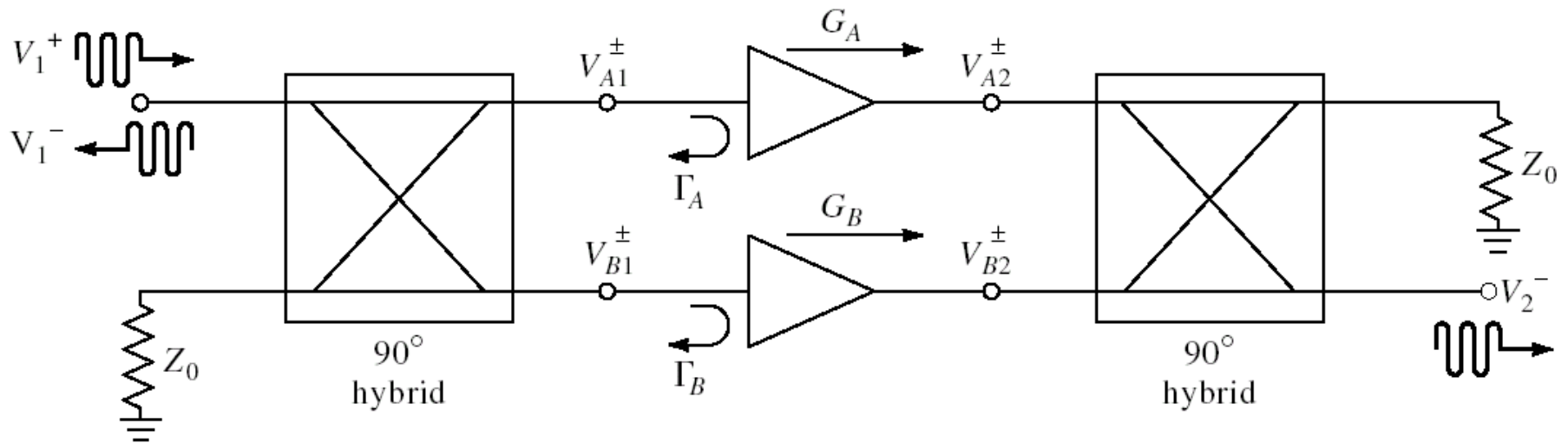
Microwave Amplifiers

Broadband amplifiers

Broadband/Wideband amplifiers

- Achieved by some design techniques (only at the expense of gain, complexity)
 1. Compensated matching networks
 2. Resistive matching networks
 3. Negative feedback
 4. Balanced amplifiers
 5. Distributed amplifiers
 6. Differential amplifiers

Balanced amplifiers



- two identical amplifiers with two hybrid couplers
3 dB / 90° to cancel input and output reflections

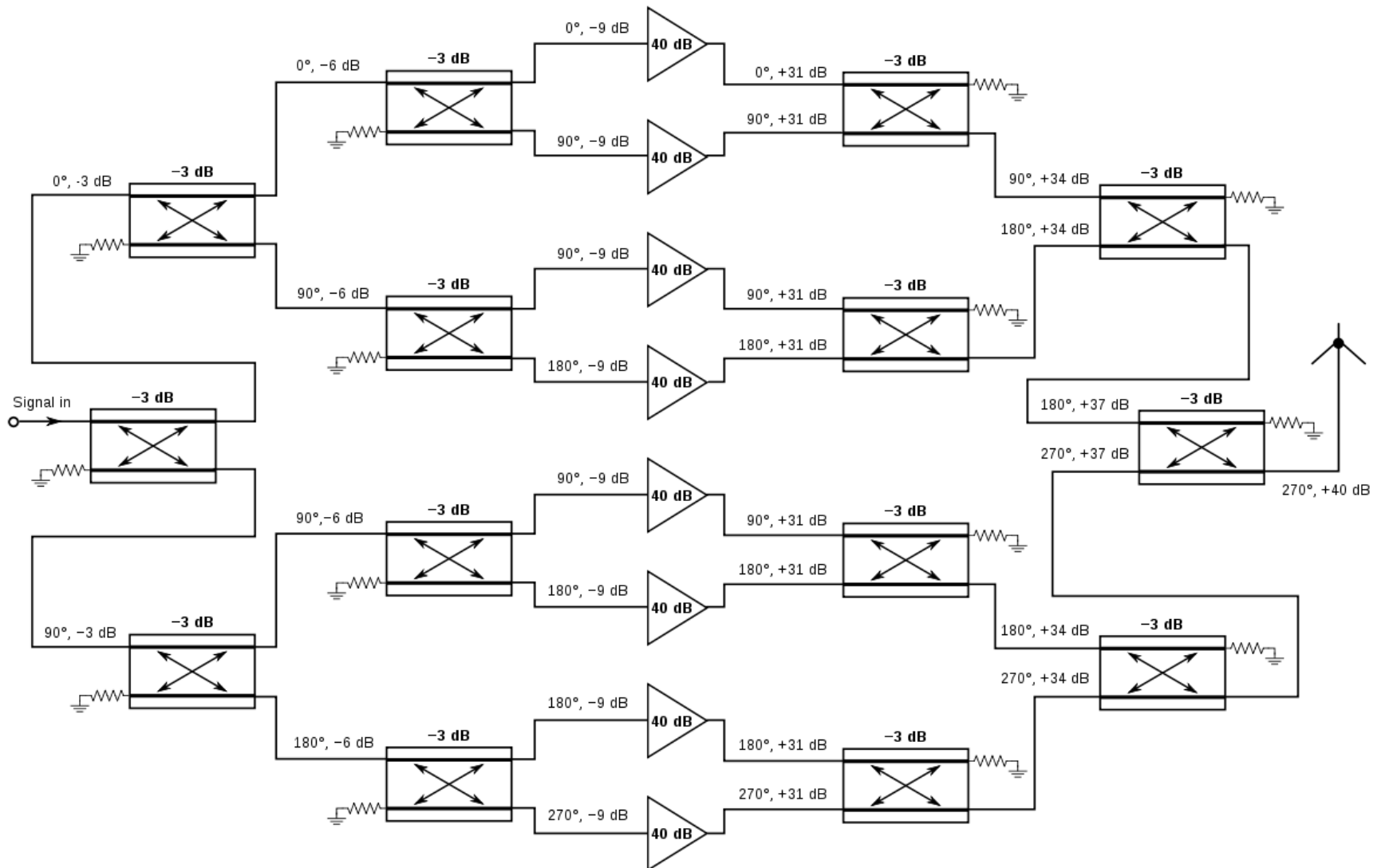
$$S_{21} = \frac{-j}{2} \cdot (G_A + G_B)$$

$$S_{21}|_{A=B} = -j \cdot G$$

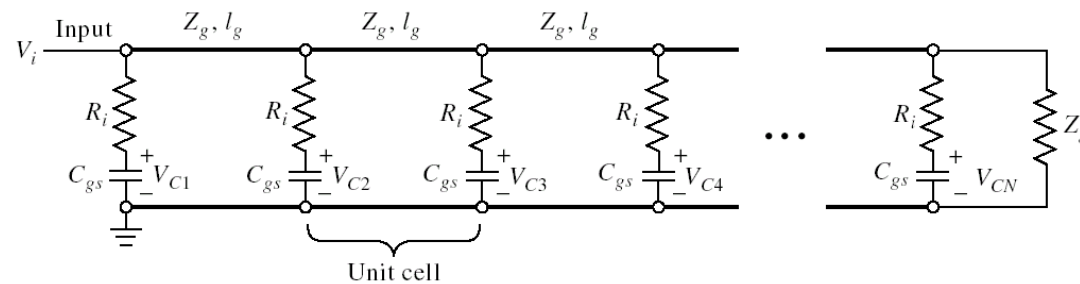
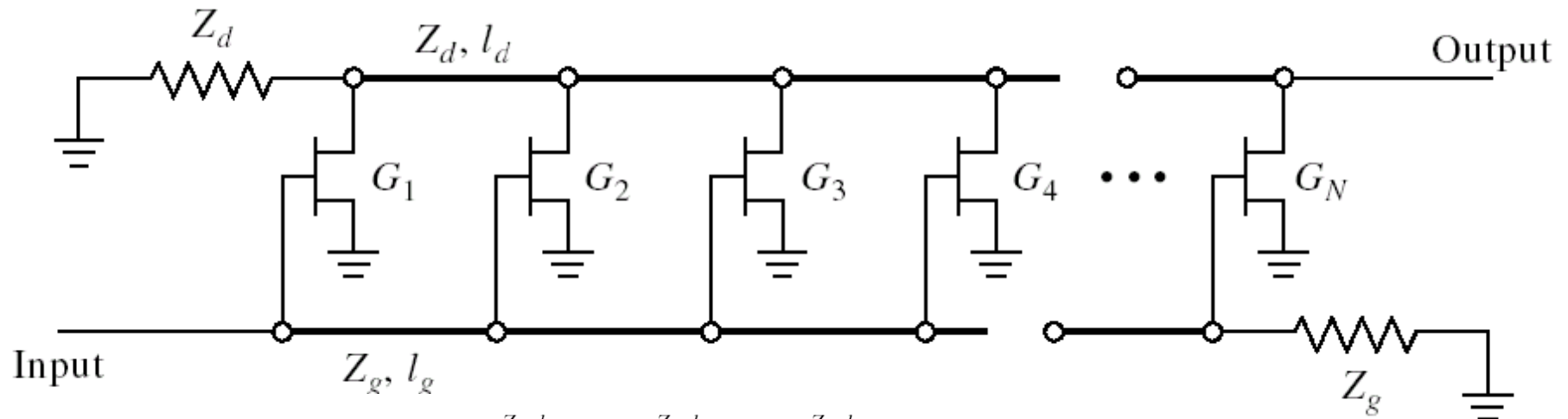
$$S_{11} = \frac{1}{2} \cdot (\Gamma_A - \Gamma_B) \quad F = \frac{1}{2} \cdot (F_A + F_B)$$

$$S_{11}|_{A=B} = 0$$

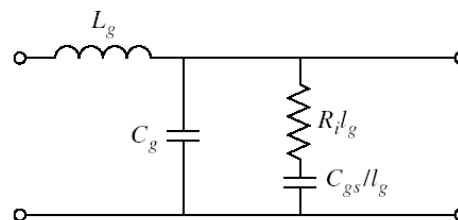
Balanced amplifiers



Distributed amplifiers



(a)



(b)

Distributed amplifiers

- the phase delays on the gate (input) and drain (output) lines are synchronized

$$\gamma_g = \alpha_g + j \cdot \beta_g \quad \gamma_d = \alpha_d + j \cdot \beta_d \quad \beta_g \cdot l_g = \beta_d \cdot l_d$$

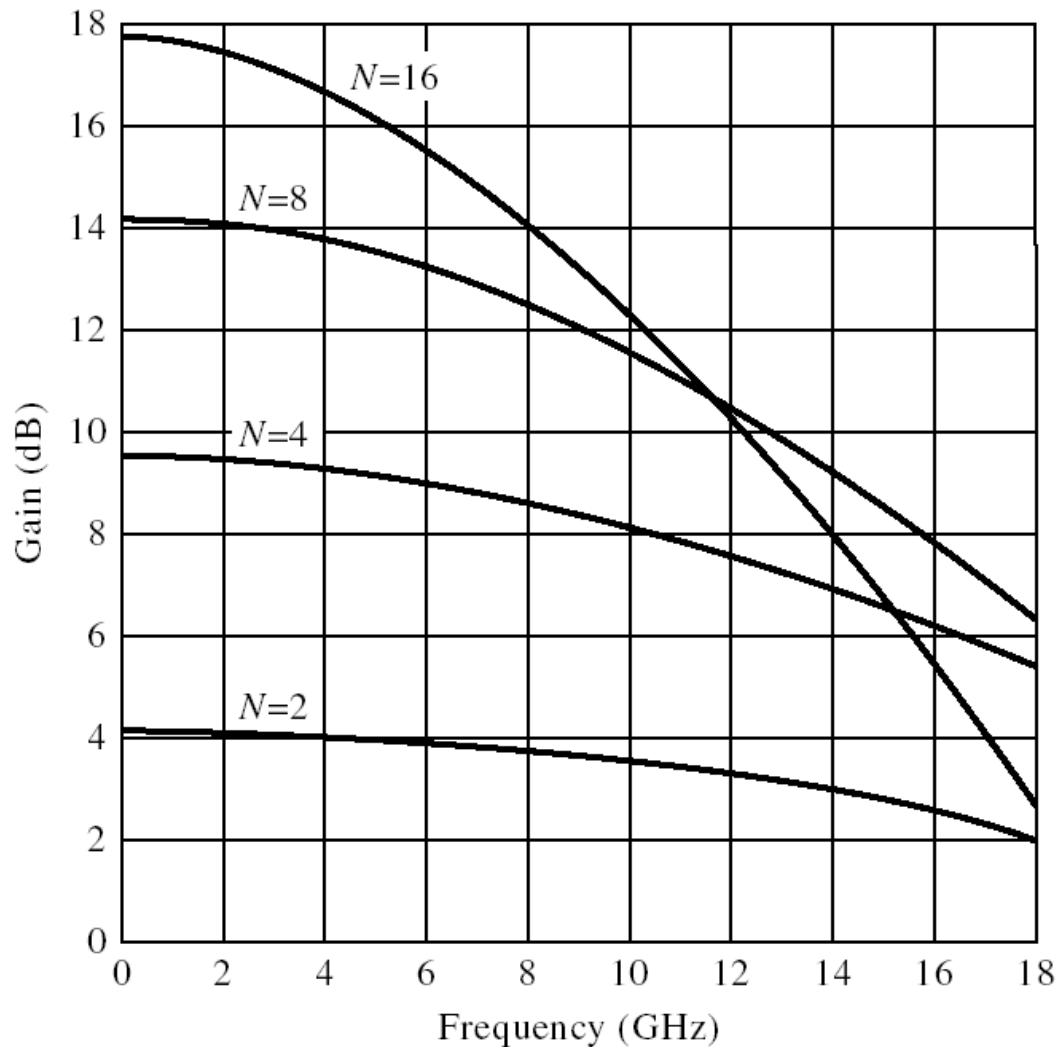
- Power gain

$$G = \frac{g_m^2 \cdot Z_d \cdot Z_g}{4} \cdot \frac{\left(e^{-N \cdot \alpha_g \cdot l_g} - e^{-N \cdot \alpha_d \cdot l_d} \right)^2}{\left(e^{-\alpha_g \cdot l_g} - e^{-\alpha_d \cdot l_d} \right)^2}$$

- Lossless power gain

$$G = \frac{g_m^2 \cdot Z_d \cdot Z_g \cdot N^2}{4}$$

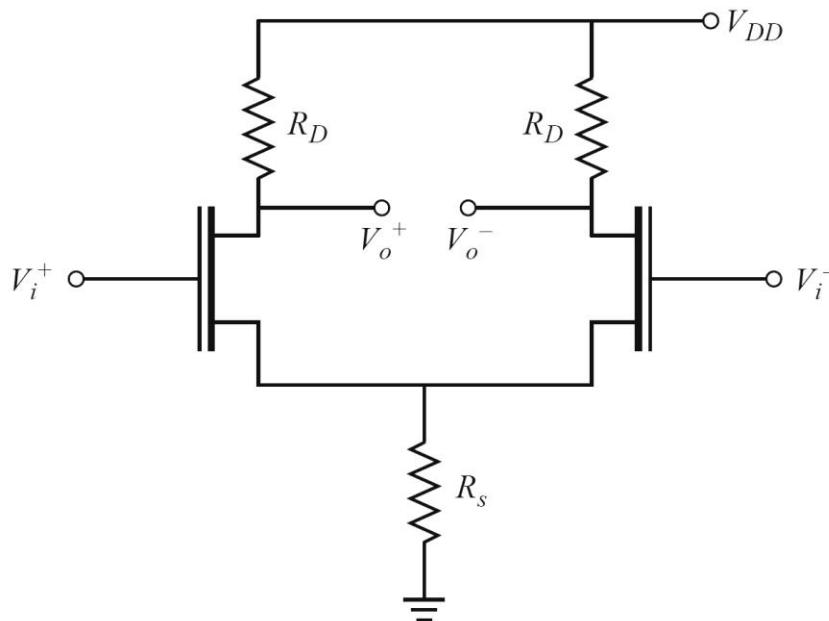
Distributed amplifiers



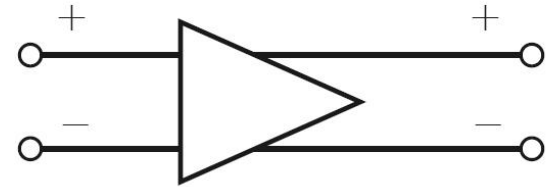
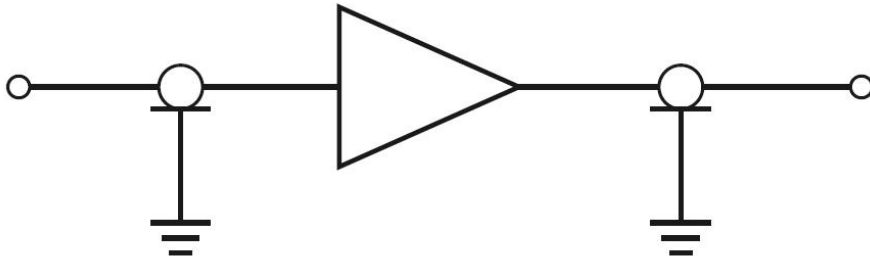
$$N_{opt} = \frac{\ln(\alpha_g \cdot l_g) - \ln(\alpha_d \cdot l_d)}{\alpha_g \cdot l_g - \alpha_d \cdot l_d}$$

Differential amplifiers

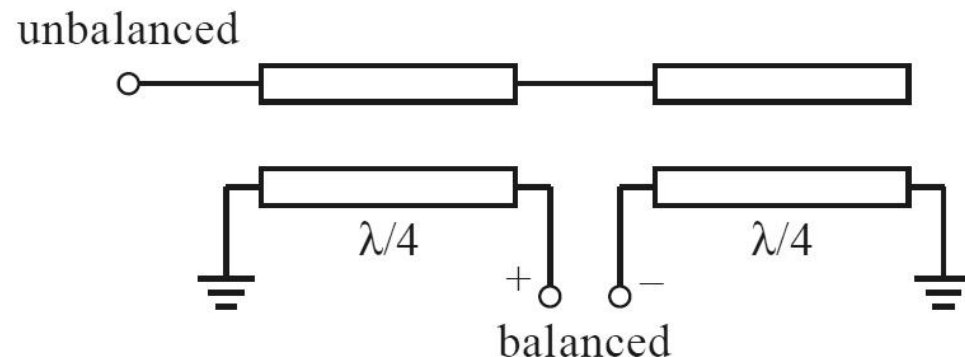
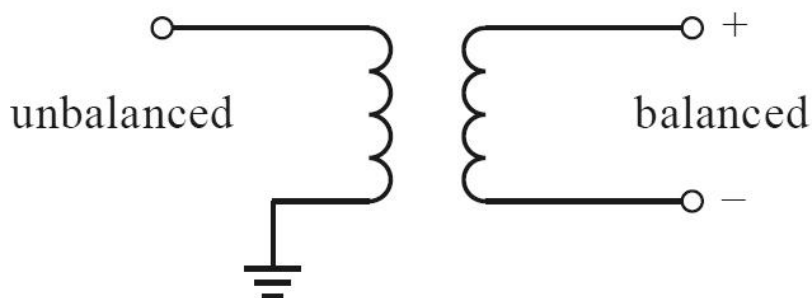
- In differential mode the input capacitances of the two transistors are connected in series
- Unity gain frequency is doubled



Differential amplifiers

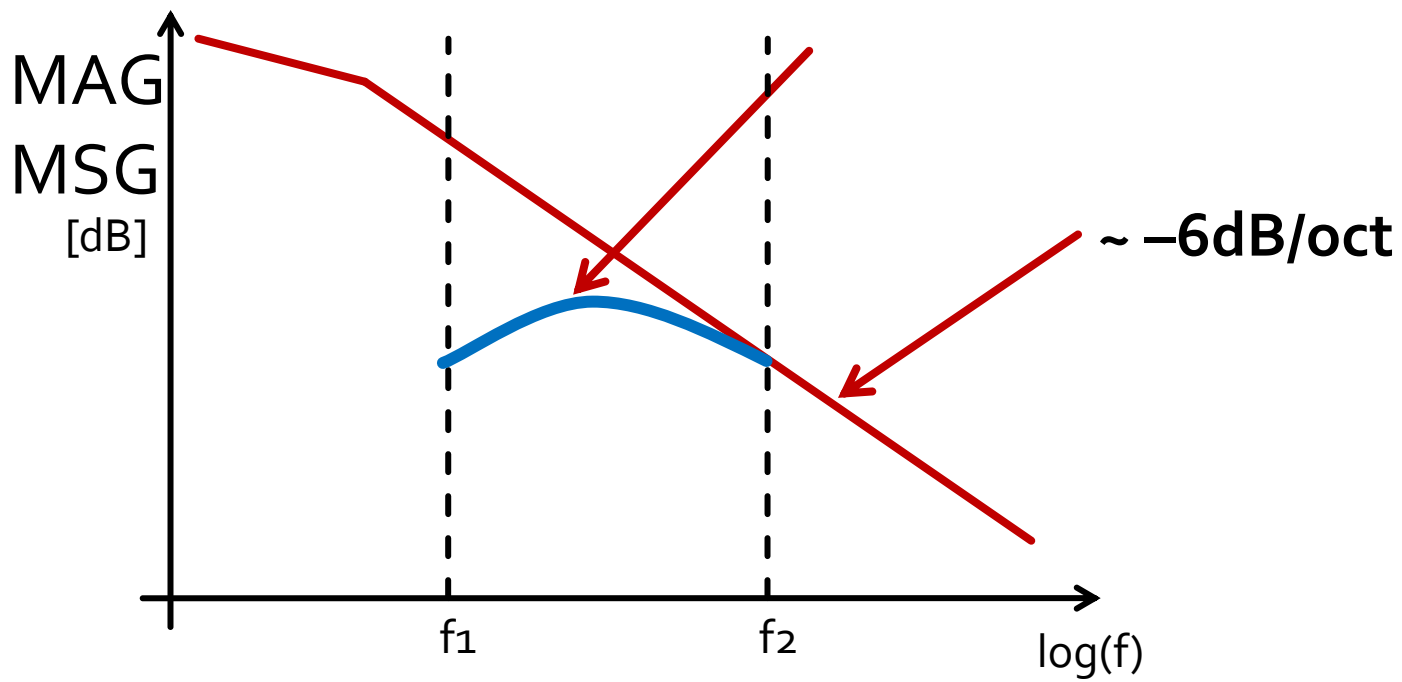


- We use circuits to transition from an unbalanced signal to a balanced signal (or vice versa)
 - hybrid couplers $3\text{dB} / 180^\circ$
 - "balun" (balanced - unbalanced)



Compensated matching networks

- Control the design of the matching networks at more (at least 2) frequencies and impose the same gain

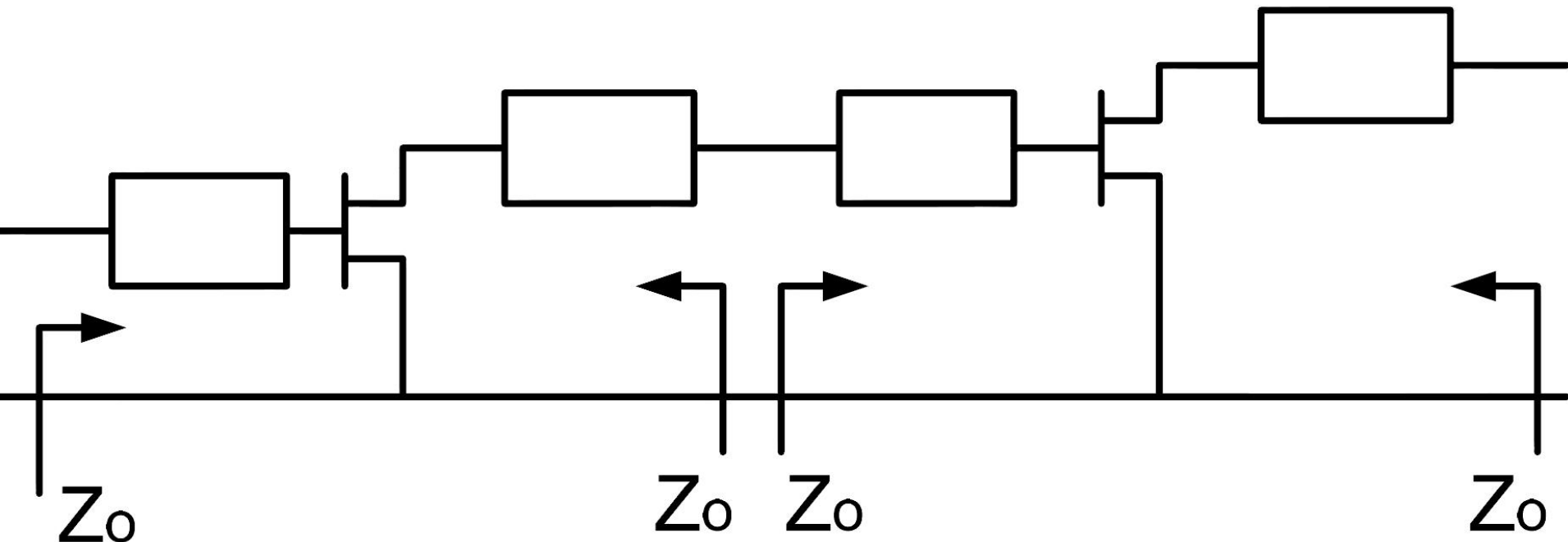


Microwave Amplifiers

Multistage Amplifier Design

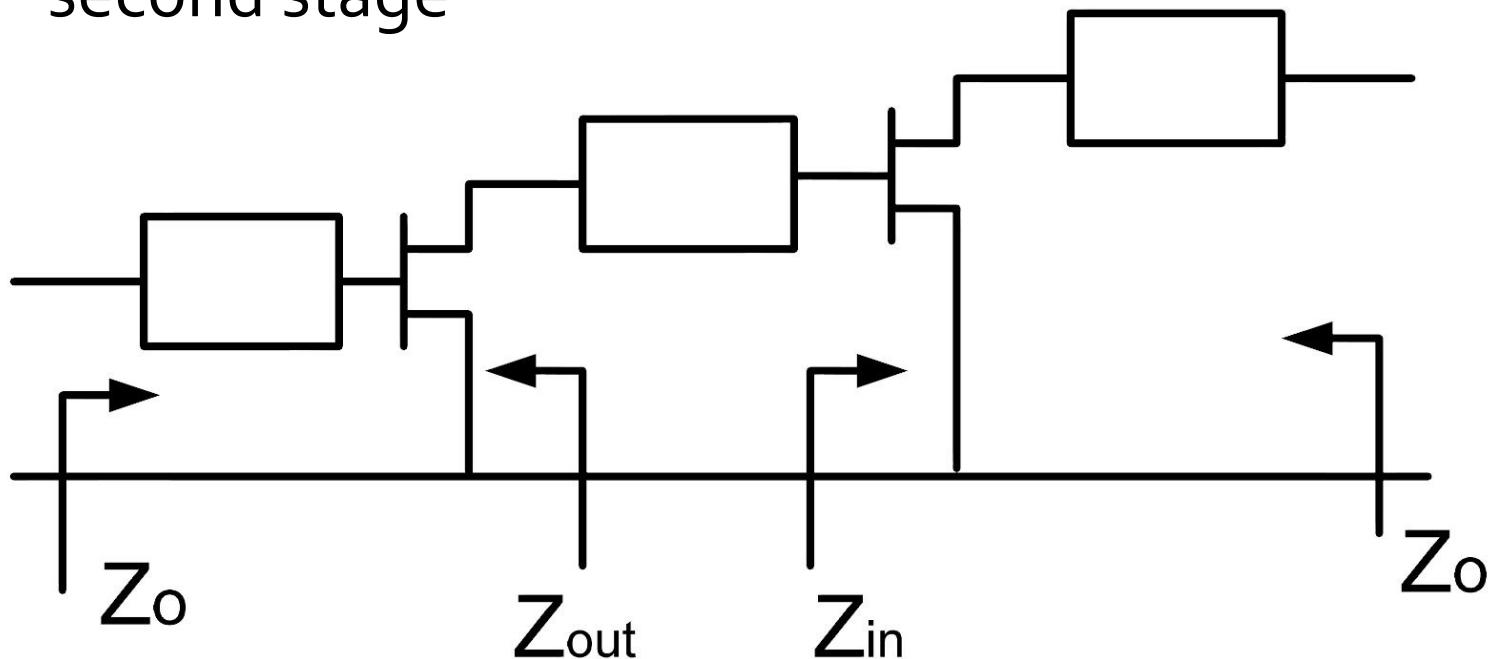
Multistage amplifiers

- Interstage matching can be designed in two modes:
 - Each stage is matched to a virtual $\Gamma = 0$



Multistage amplifiers

- Interstage matching can be designed in two modes:
 - One stage is matched to offer necessary Γ for the second stage

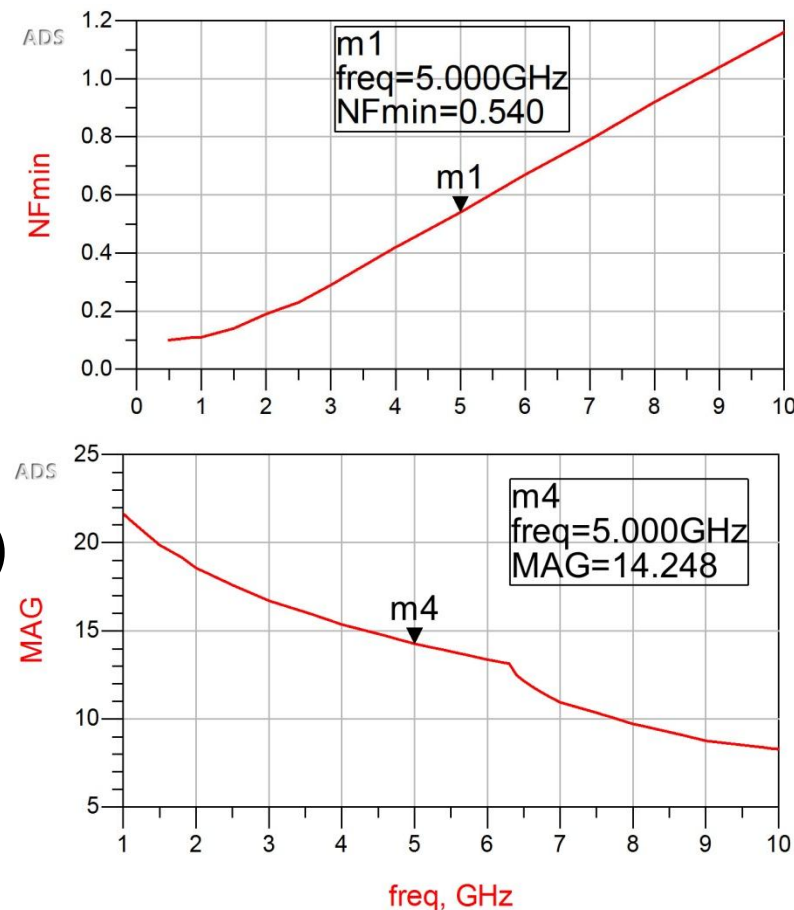


Example multistage LNA

- Similar to the project assignment
- LNA using ATF-34143 providing:
 - $G = 20\text{dB}$
 - $F = 1\text{dB}$
 - $@f = 5\text{GHz}$

Example

- ATF-34143 at $V_{ds}=3V$ $I_d=20mA$.
- @5GHz
 - $S_{11} = 0.64 \angle 139^\circ$
 - $S_{12} = 0.119 \angle -21^\circ$
 - $S_{21} = 3.165 \angle 16^\circ$
 - $S_{22} = 0.22 \angle 146^\circ$
 - $F_{min} = 0.54$ (typically[dB] !)
 - $\Gamma_{opt} = 0.45 \angle 174^\circ$
 - $r_n = 0.03$



Example, LNA @ 5 GHz

■ ATF-34143 at $V_{ds}=3V$ $I_d=20mA$.

■ @5GHz

■ $S_{11} = 0.64 \angle 139^\circ$

■ $S_{12} = 0.119 \angle -21^\circ$

■ $S_{21} = 3.165 \angle 16^\circ$

■ $S_{22} = 0.22 \angle 146^\circ$

■ $F_{min} = 0.54$ (tipic [dB])

■ $\Gamma_{opt} = 0.45 \angle 174^\circ$

■ $r_n = 0.03$

IATF-34143

IS-PARAMETERS at $V_{ds}=3V$ $I_d=20mA$. LAST UPDATED 01-29-99

ghz s ma r 50

2.0	0.75	-126	6.306	90	0.088	23	0.26	-120
2.5	0.72	-145	5.438	75	0.095	15	0.25	-140
3.0	0.69	-162	4.762	62	0.102	7	0.23	-156
4.0	0.65	166	3.806	38	0.111	-8	0.22	174
5.0	0.64	139	3.165	16	0.119	-21	0.22	146
6.0	0.65	114	2.706	-5	0.125	-35	0.23	118
7.0	0.66	89	2.326	-27	0.129	-49	0.25	91
8.0	0.69	67	2.017	-47	0.133	-62	0.29	67
9.0	0.72	48	1.758	-66	0.135	-75	0.34	46

IFREQ	Fopt	GAMMA	OPT	RN/Zo
IGHZ	dB	MAG	ANG	-

2.0	0.19	0.71	66	0.09
2.5	0.23	0.65	83	0.07
3.0	0.29	0.59	102	0.06
4.0	0.42	0.51	138	0.03
5.0	0.54	0.45	174	0.03
6.0	0.67	0.42	-151	0.05
7.0	0.79	0.42	-118	0.10
8.0	0.92	0.45	-88	0.18
9.0	1.04	0.51	-63	0.30
10.0	1.16	0.61	-43	0.46

Multistage amplifiers

- If we need more power gain than only one transistor can supply
 - design target 20dB
 - $MAG @ 5GHz = 14.248 \text{ dB} < 20\text{dB}$
- We use Friis formula to separate the target:
 - Power gain
 - Noise
- on two amplifier stages

Friis Formula (noise)

$$F_{cas} = F_1 + \frac{F_2 - 1}{G_1} + \frac{F_3 - 1}{G_1 \cdot G_2} + \frac{F_4 - 1}{G_1 \cdot G_2 \cdot G_3} + \dots$$

- Effects of Friis Formula:
 - it's essential that the first stage is as **noiseless** as possible even if that means sacrificing power
 - the second stage can be optimized for power **gain**
- Friis Formula **must** be used in **linear scale!**
- **Avago/Broadcom AppCAD**
 - AppCAD Free Design Assistant Tool for Microsoft Windows → Google

Friis Formula (noise)

$$G_{cas} = G_1 \cdot G_2$$

$$F_{cas} = F_1 + \frac{1}{G_1} (F_2 - 1)$$

- Friis formula
 - first stage: low noise factor, probably resulting in a smaller gain
 - second stage: high gain, probably resulting in higher noise factor
- It's essential to introduce a design margin (reserve: ΔF , ΔG)
 - $G = G_{\text{design}} + \Delta G$
 - $F = F_{\text{design}} - \Delta F$
- Interpretation of the design target
 - $G > G_{\text{design}}$, better, but it's not required to sacrifice other parameters to maximize the gain
 - $F < F_{\text{design}}$, better, the smaller the better, we must target **the smallest possible noise** factor as long as the other design parameters **are met**

Friis Formula (noise)

- Friis formula
 - first stage: low noise factor, probably resulting in a smaller gain
 - second stage: high gain, probably resulting in higher noise factor
- Separation of the design parameters on the 2 amplification stages (Estimated!)
 - input stage: $F_1 = 0.7 \text{ dB}$, $G_1 = 9 \text{ dB}$
 - output stage: $F_2 = 1.2 \text{ dB}$, $G_2 = 13 \text{ dB}$
- To verify the result apply Friis formula
- First transform to **linear scale !**

$$F_1 = 10^{\frac{F_1[dB]}{10}} = 10^{0.07} = 1.175$$

$$F_2 = 10^{\frac{F_2[dB]}{10}} = 10^{0.12} = 1.318$$

$$F_{cas} = F_1 + \frac{1}{G_1}(F_2 - 1) = 1.215$$

$$F_{cas} = 10 \cdot \log(1.215) = 0.846 \text{ dB}$$

$$G_1 = 10^{\frac{G_1[dB]}{10}} = 10^{0.9} = 7.943$$

$$G_2 = 10^{\frac{G_2[dB]}{10}} = 10^{1.3} = 19.953$$

$$G_{cas} = G_1 \cdot G_2 = 158.49$$

$$G_{cas} = 10 \cdot \log(158.49) = 22 \text{ dB}$$

Friis Formula (noise)

■ Avago/Broadcom AppCAD

AppCAD - [NoiseCalc]

File Calculate Application Examples Options Help

NoiseCalc Set Number of Stages = 2 Calculate [F4]

Stage Data	Units	Stage 1	Stage 2
Stage Name:		Avago Duplexer	Avago ATF-36xxx
Noise Figure	dB	0.7	1.2
Gain	dB	9	13
Output IP3	dBm	100	14.5
dNF/dTemp	dB/°C	0	0
dG/dTemp	dB/°C	0	0

Stage Analysis:

NF (Temp corr)	dB	0.70	1.20
Gain (Temp corr)	dB	9.00	13.00
Input Power	dBm	-50.00	-41.00
Output Power	dBm	-41.00	-28.00
d NF/d NF	dB/dB	0.97	0.15
d NF/d Gain	dB/dB	-0.03	0.00
d IP3/d IP3	dBm/dBm	0.00	1.00

Enter System Parameters:

Input Power	-50	dBm
Analysis Temperature	25	°C
Noise BW	1	MHz
Ref Temperature	25	°C
S/N (for sensitivity)	10	dB
Noise Source (Ref)	290	°K

System Analysis:

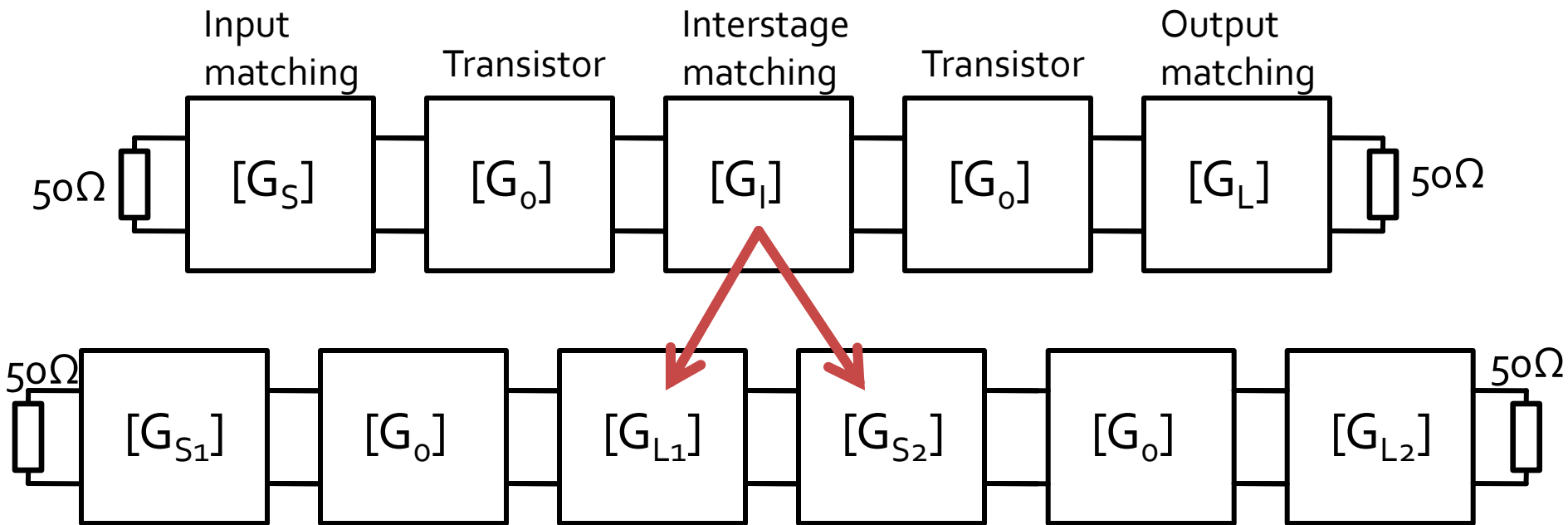
Gain	22.00	dB
Noise Figure	0.85	dB
Noise Temp	82.34	°K
SNR	63.13	dB
MDS	-113.13	dBm
Sensitivity	-103.13	dBm
Noise Floor	-173.13	dBm/Hz

Input IP3	-7.50	dBm
Output IP3	14.50	dBm
Input IM level	-135.00	dBm
Input IM level	-85.00	dbc
Output IM level	-113.00	dBm
Output IM level	-85.00	dbc
SFDR	70.42	dB

Multistage amplifier design

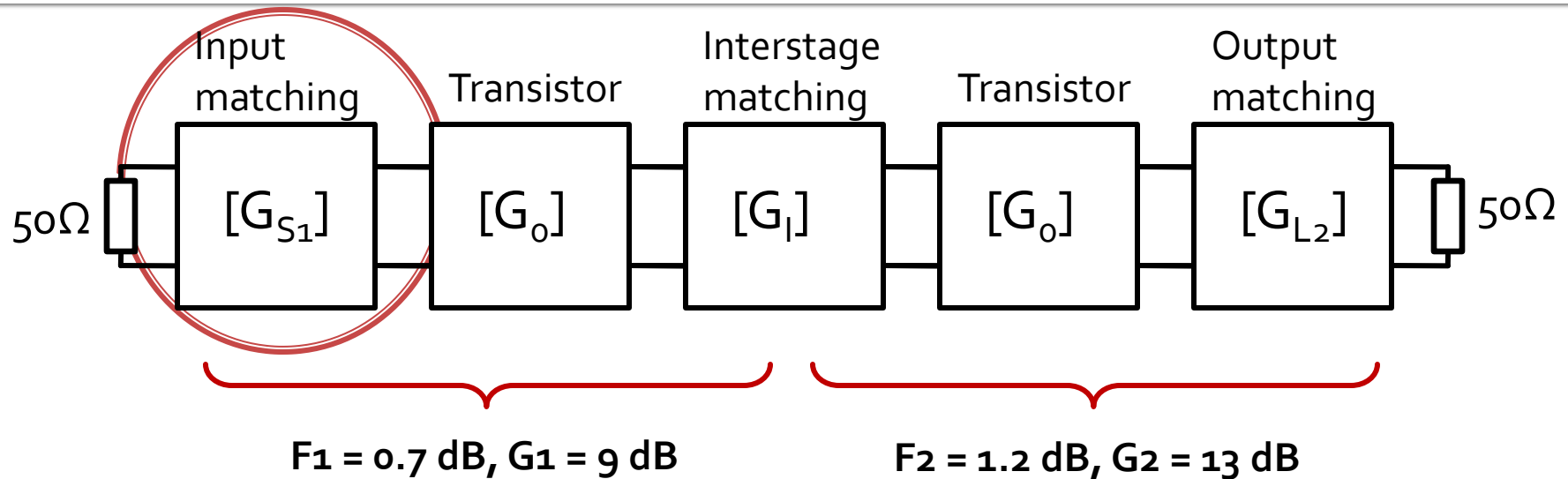
- Separation of the design parameters on the 2 amplification stages (Estimated!)
 - input stage: $F_1 = 0.7$ dB, $G_1 = 9$ dB
 - output stage: $F_2 = 1.2$ dB, $G_2 = 13$ dB
 - total: $F = 0.85$ dB, $G = 22$ dB
- Meets design specifications (with design margin)
- We can reuse some of the results in the single stage LNA design (Lecture 10)
 - input matching can be used for the input of the first stage – very low noise, good enough power gain
 - output matching was designed for maximum gain, can be used for the output of the second stage
 - input and output matching were designed for 50Ω source and load, similar to current conditions

Multistage amplifier design



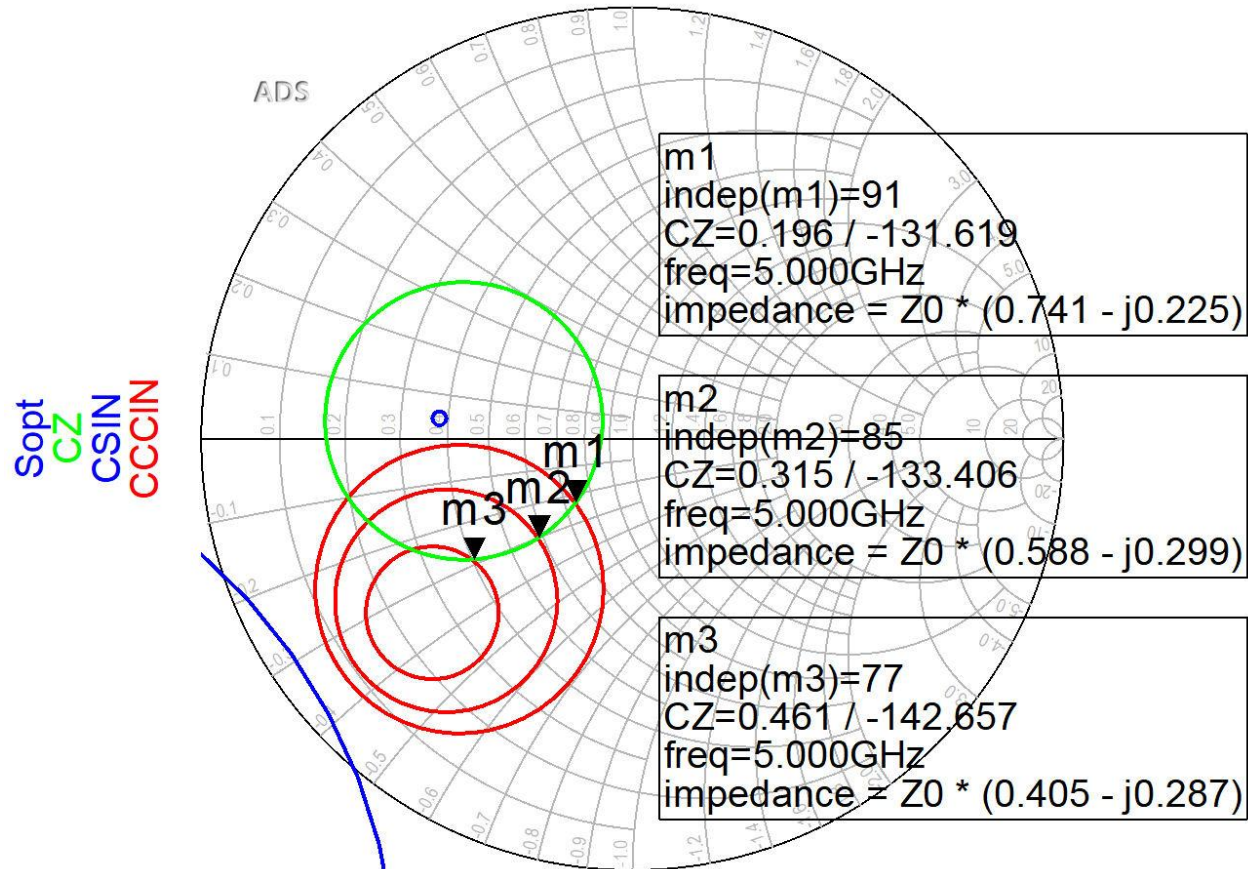
- Gain computation
 - Interstage matching can supplement the gain for both amplifier stages
 - The design for input and output matching must be achieved on a single transistor schematic (recommended: easier)

Input matching stage 1 (S1)



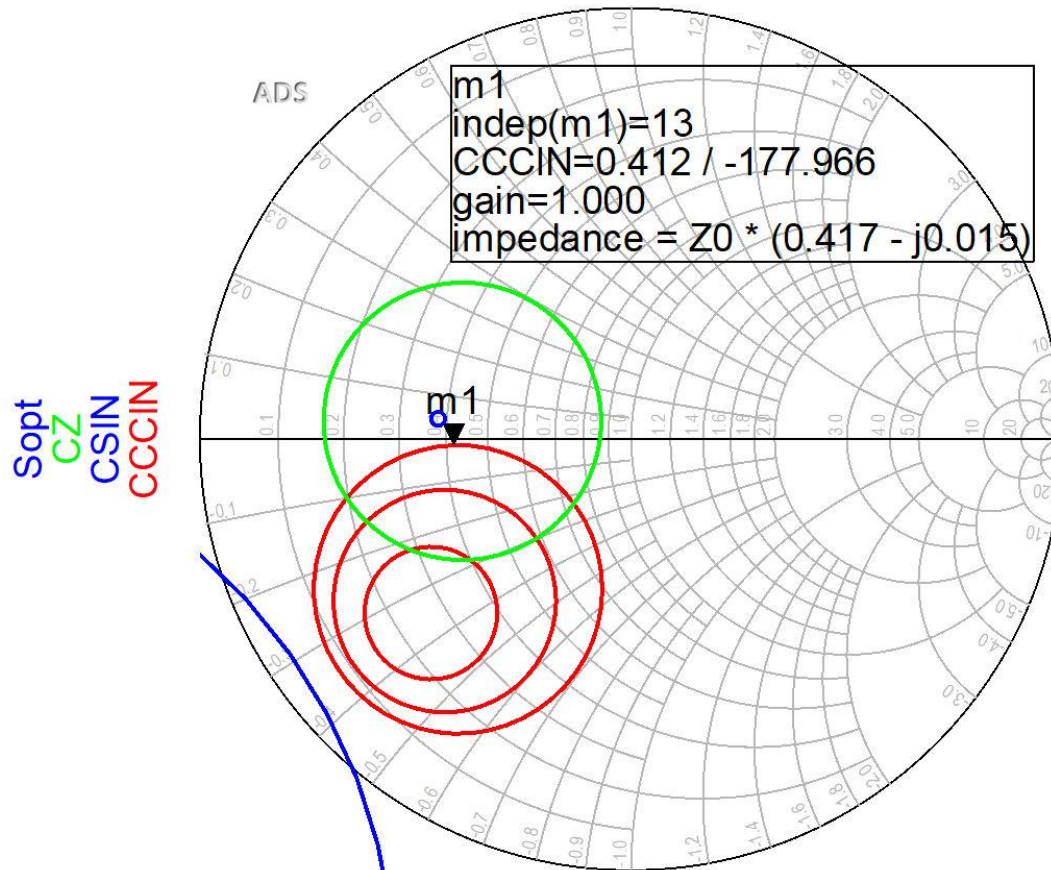
- We favor optimization for **noise** (low/minimum)
- Also considered
 - Power gain (can be lower, but not too much)
 - Bandwidth (through Q , quality factor)
 - Stability

Input matching stage 1 (S₁)



- For the input matching circuit
 - noise circle CZ: 0.75dB
 - input constant gain circles CCCIN: 1dB, 1.5dB, 2 dB
- We choose (small Q → wide bandwidth) position m1

Input matching stage 1 (S₁)



- If we can afford a 1.2dB decrease of the input gain for better NF, Q (Gs = 1 dB), position m1 above is better
- We favor **better** (smaller) **NF**

Input matching stage 1 (S1)

- G_{S1} : Position m1 in complex plane, **1dB**

$$\Gamma_S = 0.412 \angle -178^\circ$$

$$|\Gamma_S| = 0.412; \quad \varphi = -178^\circ$$

$$\cos(\varphi + 2\theta) = -|\Gamma_S|$$

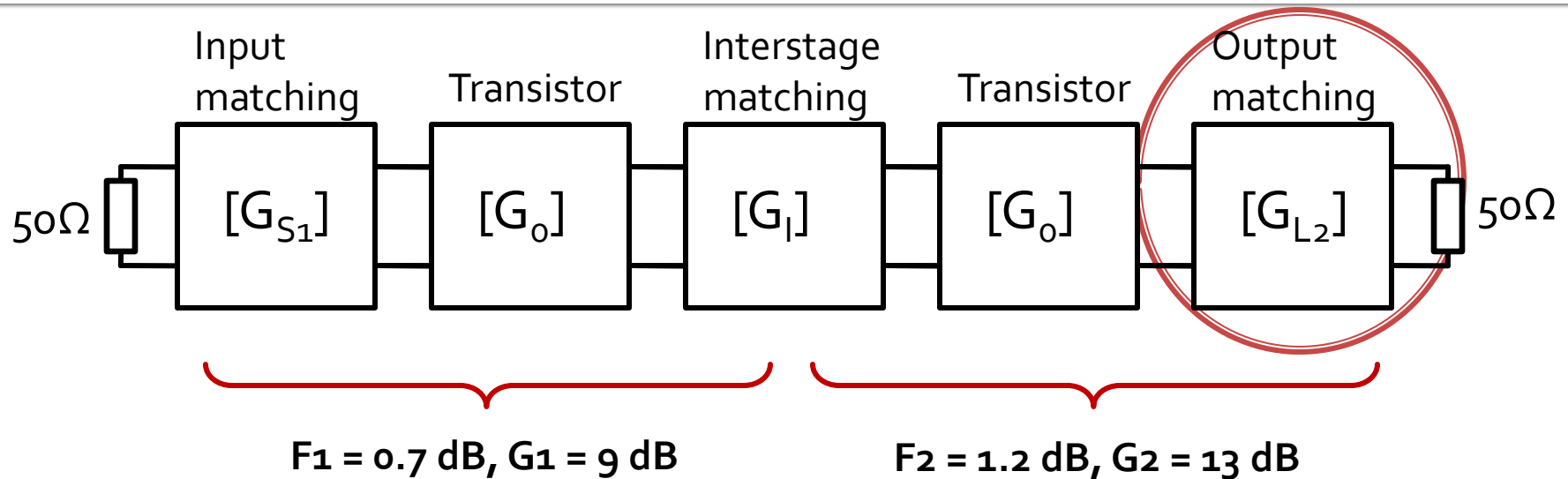
$$\text{Im}[y_S(\theta)] = \frac{\mp 2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}}$$

$$\cos(\varphi + 2\theta) = -0.412 \Rightarrow (\varphi + 2\theta) = \pm 114.33^\circ$$

$$\theta_{sp} = \tan^{-1}(\text{Im}[y_S(\theta)]) = \tan^{-1}\left(\frac{\mp 2 \cdot |\Gamma_S|}{\sqrt{1 - |\Gamma_S|^2}}\right)$$

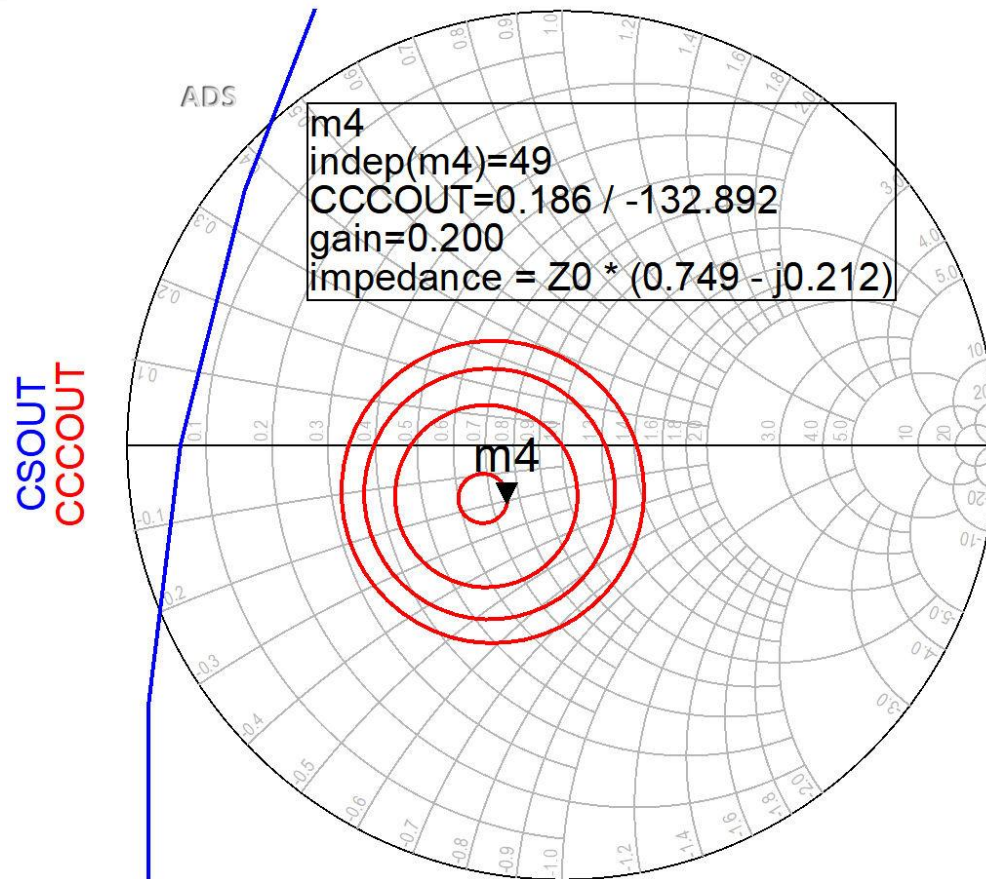
$$(\varphi + 2\theta) = \begin{cases} +114.33^\circ \\ -114.33^\circ \end{cases} \quad \theta = \begin{cases} 146.2^\circ \\ 31.8^\circ \end{cases} \quad \text{Im}[y_S(\theta)] = \begin{cases} -0.904 \\ +0.904 \end{cases} \quad \theta_{sp} = \begin{cases} 137.9^\circ \\ 42.1^\circ \end{cases}$$

Output matching stage 2 (L2)



- We favor optimization for **gain** (high/maximum)
- Also considered
 - Bandwidth (through Q , quality factor)
 - Stability
- noise is **not** an issue, output matching doesn't influence noise factor

Output matching stage 2 (L2)



- output constant gain circles CCCOUT: -0.4dB, -0.2dB, 0dB, +0.2dB
- The lack of noise restrictions allows optimization for better gain (close to maximum – position m4)

Output matching stage 2 (L2)

- $\mathbf{G_{L2}}$: Position m_4 in complex plane, **0.2dB**

$$\Gamma_L = 0.186 \angle -132.9^\circ$$

$$|\Gamma_L| = 0.186; \quad \varphi = -132.9^\circ$$

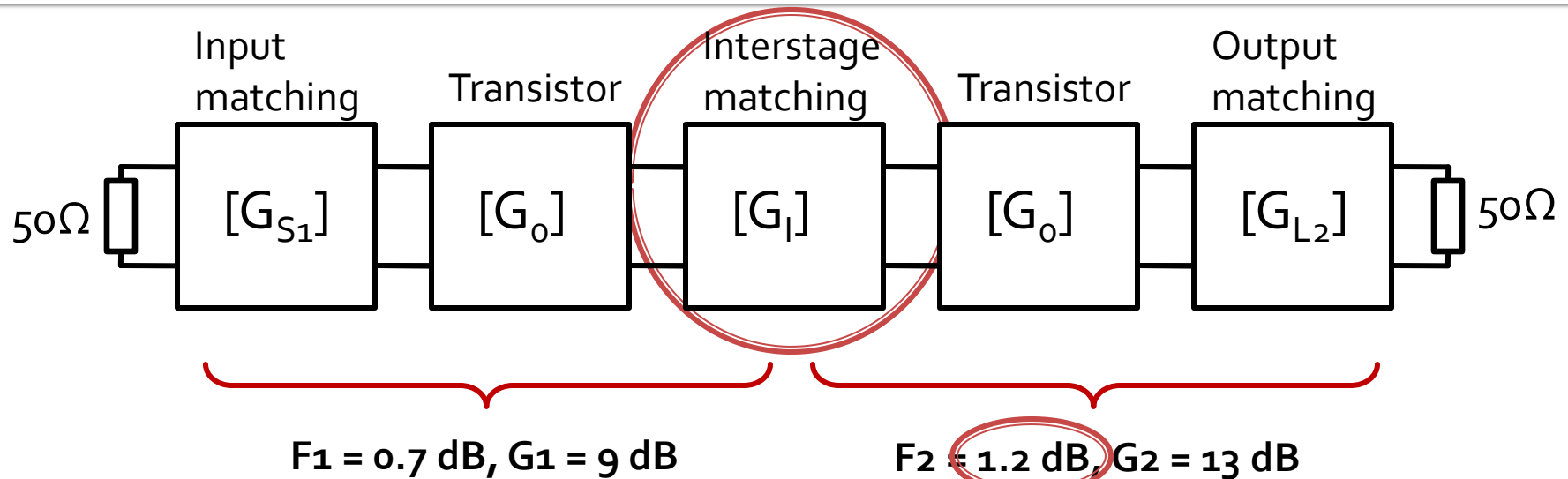
$$\cos(\varphi + 2\theta) = -|\Gamma_L| \qquad \text{Im}[y_L(\theta)] = \frac{-2 \cdot |\Gamma_L|}{\sqrt{1 - |\Gamma_L|^2}} = -0.379$$

$$\cos(\varphi + 2\theta) = -0.186 \Rightarrow (\varphi + 2\theta) = \pm 100.72^\circ$$

$$\theta_{sp} = \tan^{-1}(\text{Im}[y_L(\theta)]) = \tan^{-1}\left(\frac{\mp 2 \cdot |\Gamma_L|}{\sqrt{1 - |\Gamma_L|^2}}\right)$$

$$(\varphi + 2\theta) = \begin{cases} +100.72^\circ \\ -100.72^\circ \end{cases} \quad \theta = \begin{cases} 116.8^\circ \\ 16.1^\circ \end{cases} \quad \text{Im}[y_L(\theta)] = \begin{cases} -0.379 \\ +0.379 \end{cases} \quad \theta_{sp} = \begin{cases} 159.3^\circ \\ 20.7^\circ \end{cases}$$

Interstage matching (I)



- We take into account **gain** (high) but also **noise**
- Also considered
 - Bandwidth (through Q, quality factor)
 - Stability
- We influence the noise factor of the second stage, the noise must be considered but with less restrictive conditions (Friis shows that higher noise is acceptable).

Multistage amplifier

- Power gain

$$G_T[dB] = G_{S1}[dB] + G_0[dB] + G_I[dB] + G_0[dB] + G_{L2}[dB]$$

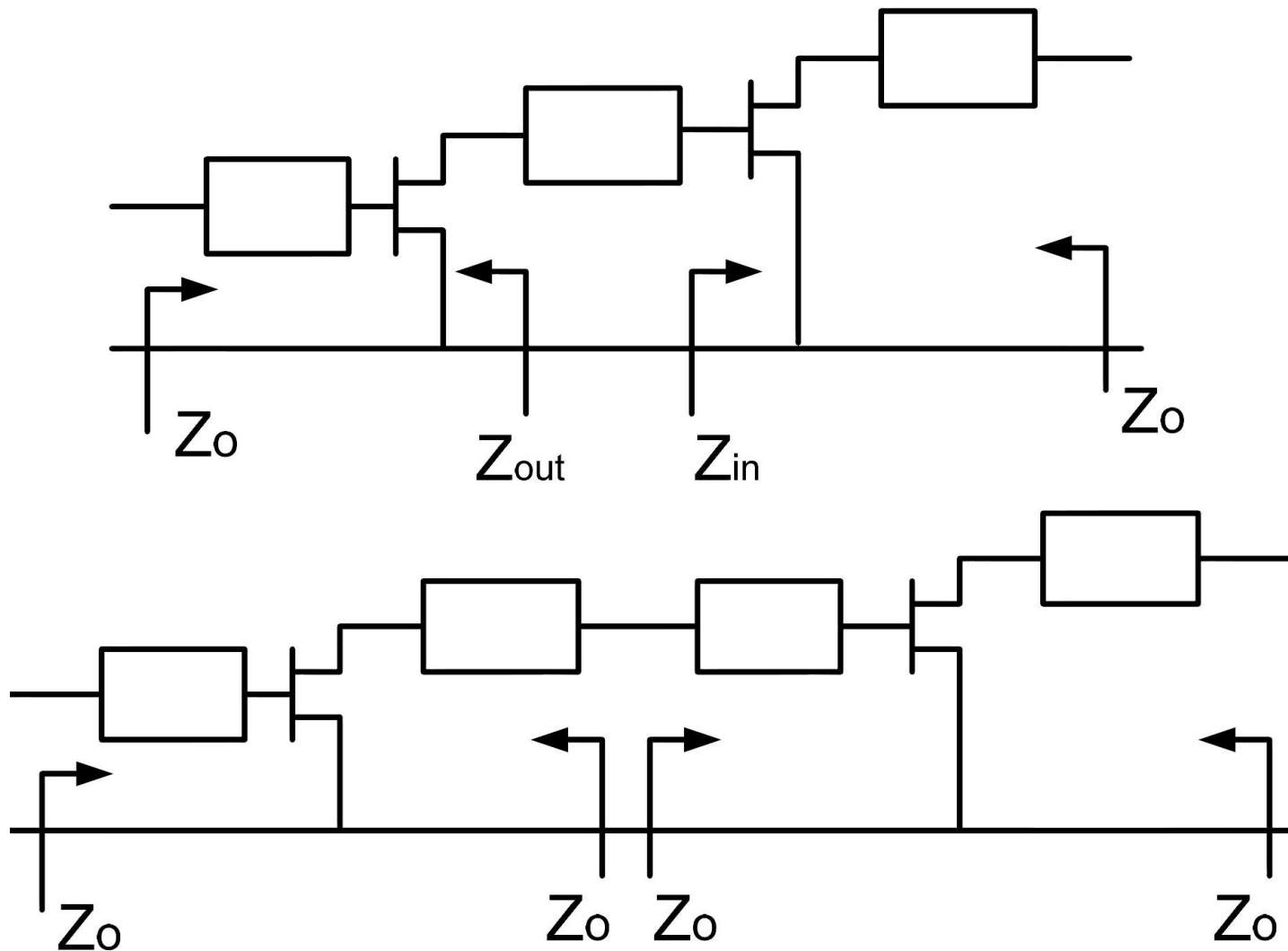
$$G_0 = |S_{21}|^2 = 10.017 = 10.007 \text{ dB}$$

$$G_T[dB] = 1 \text{ dB} + 10 \text{ dB} + G_I[dB] + 10 \text{ dB} + 0.2 \text{ dB}$$

$$G_T[dB] = 21.2 \text{ dB} + G_I[dB]$$

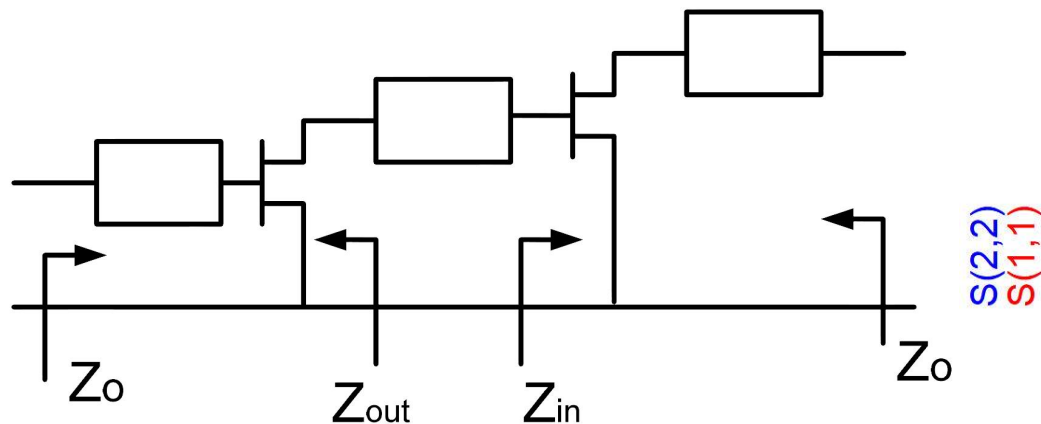
- Interstage match design must provide at least 0.8dB gain to meet specifications, by better match for the output of the first transistor and for the input of the second transistor

Interstage matching 1/2



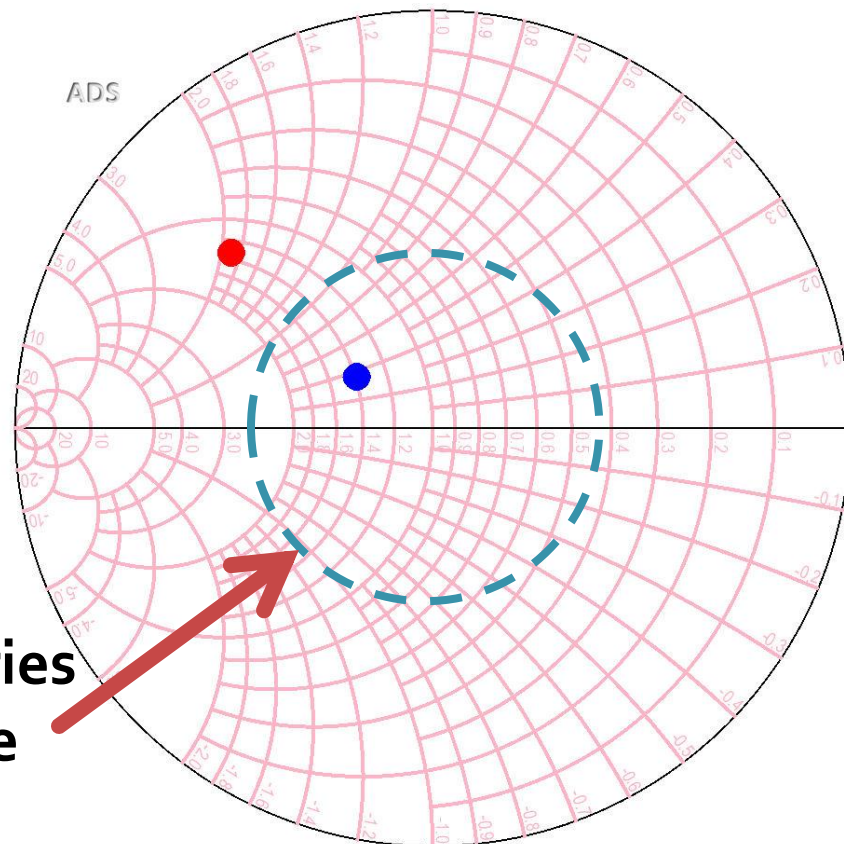
Interstage matching 1

- A single transmission line keeps constant the magnitude of the reflection coefficient
 - a circle around the Smith Chart center



$s(2,2)$
 $s(1,1)$

series
line

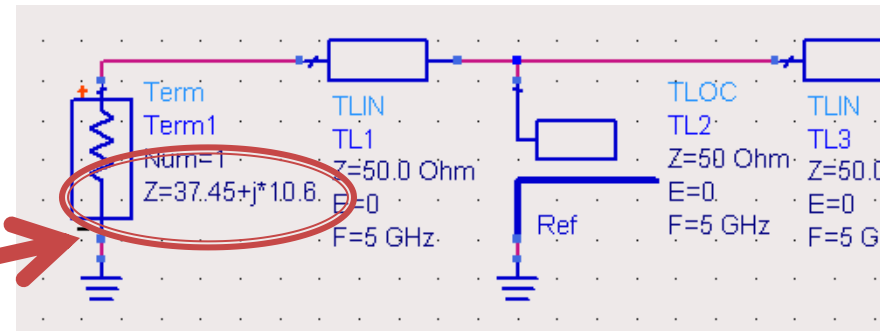
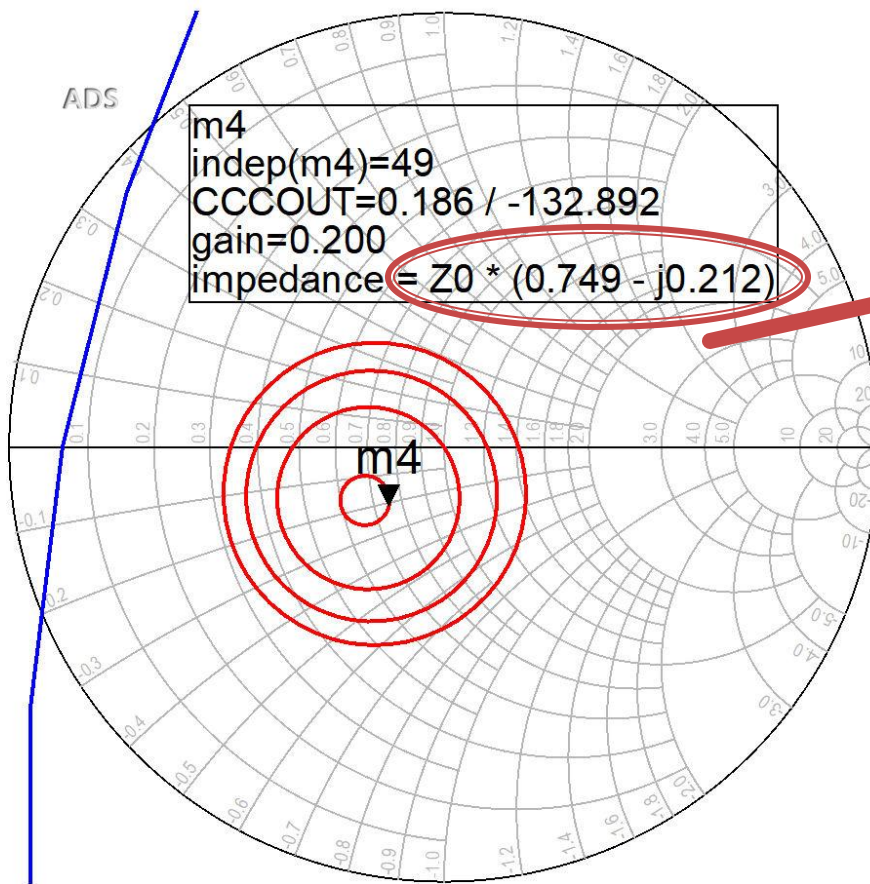


Interstage matching 1

- Can be designed in two ways:
 - starting from the output of the first stage (reflection coefficient S_{22}^*) towards the circles (drawn for the second stage):
 - stability
 - gain
 - noise
 - starting from the input of the second stage (reflection coefficient S_{11}^*) towards the circles (drawn for the first stage):
 - stability
 - gain
- First design direction has the advantage to offer control over the noise introduced by the second stage

Interstage matching 1

- Starting point – complex conjugate



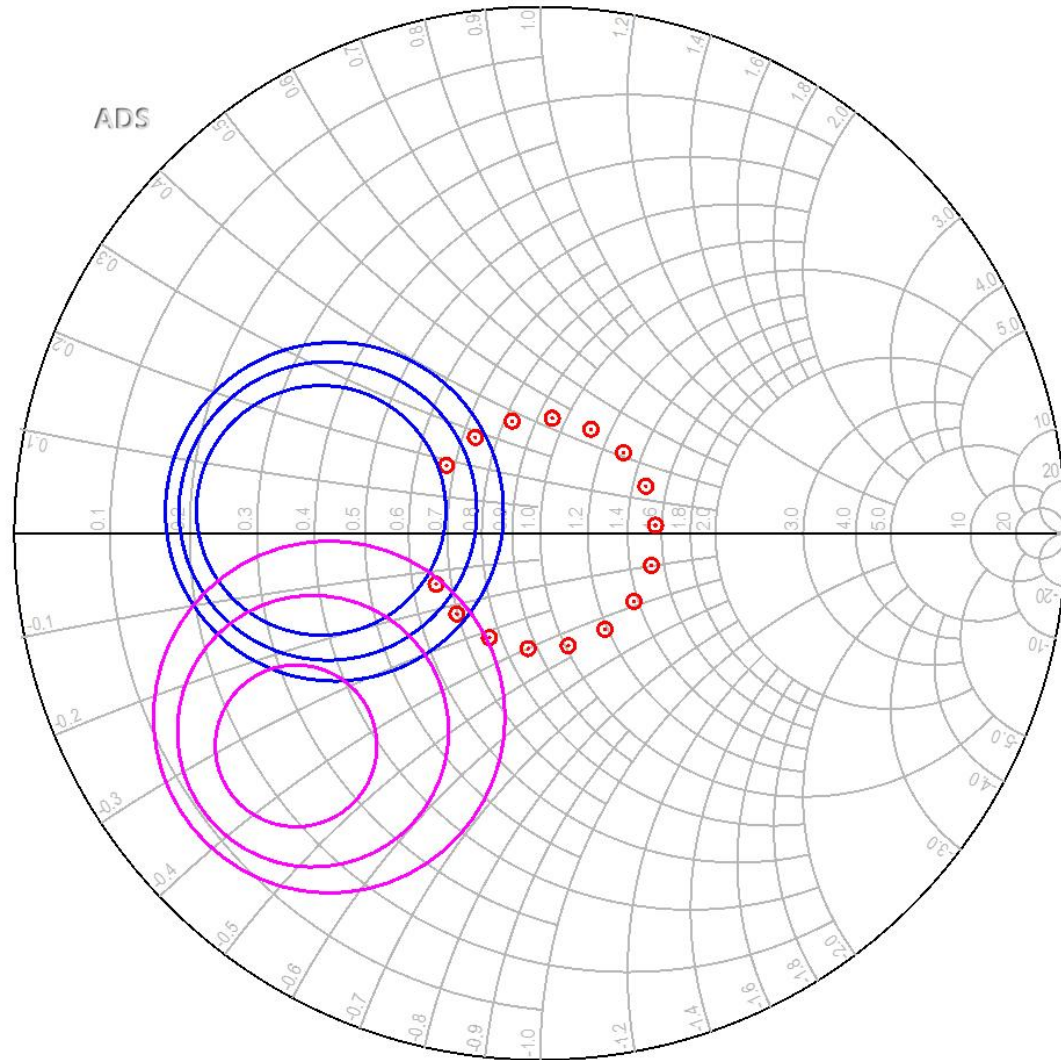
$$Z = 50\Omega \cdot (0.749 - j \cdot 0.212)$$

$$Z = 37.45\Omega - j \cdot 10.6\Omega$$

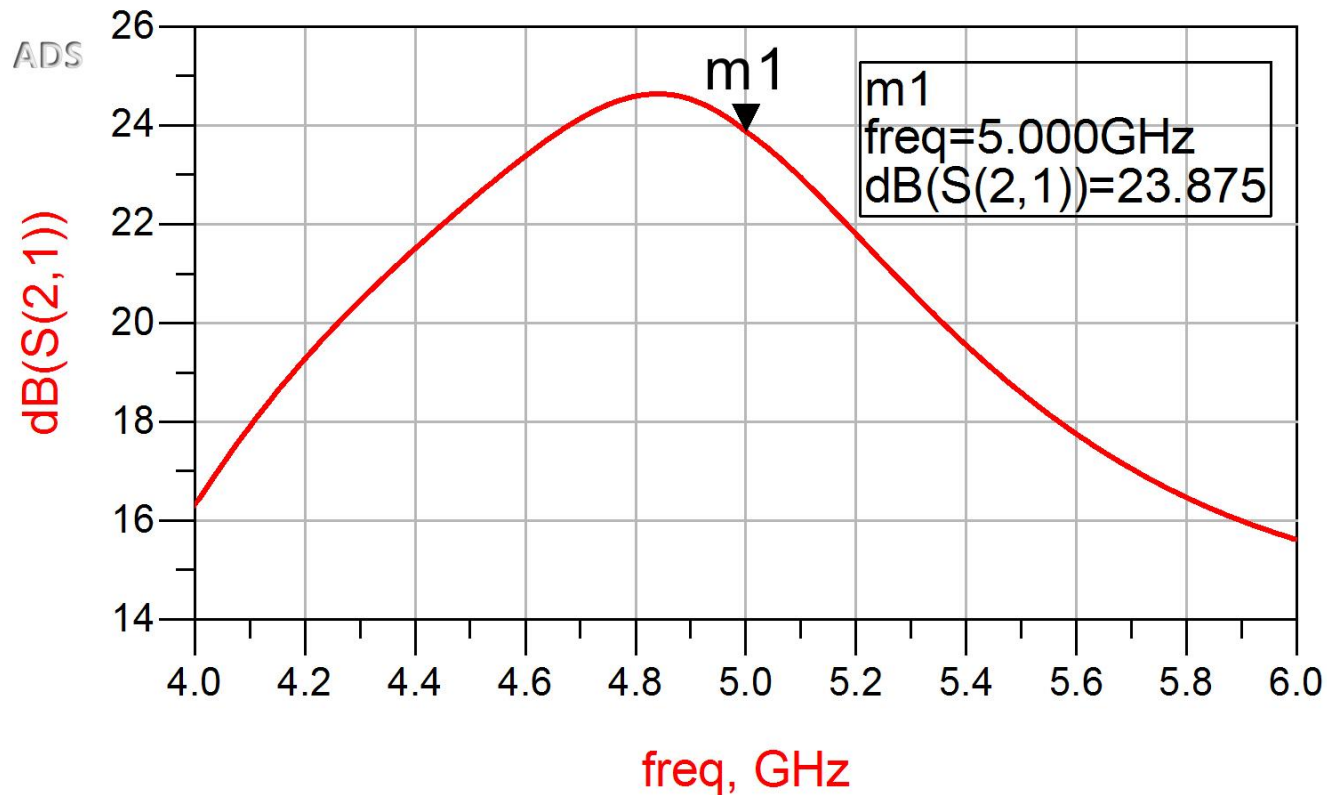
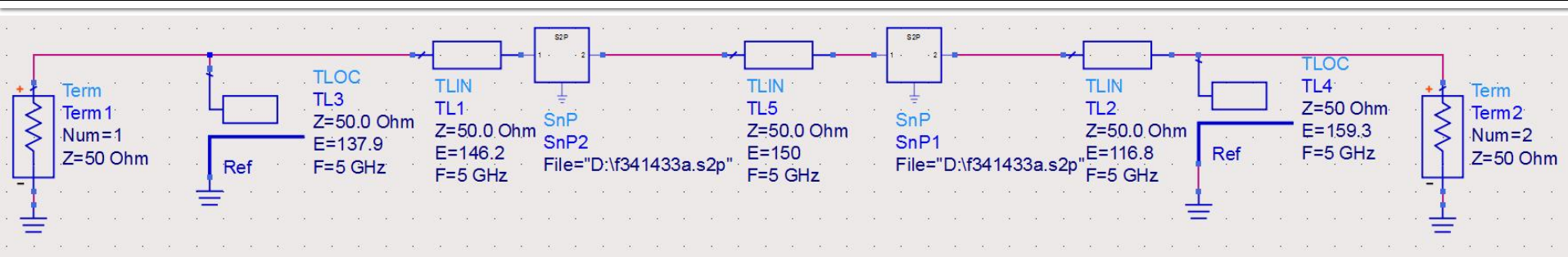
$$Z^* = 37.45\Omega + j \cdot 10.6\Omega$$

Interstage matching 1

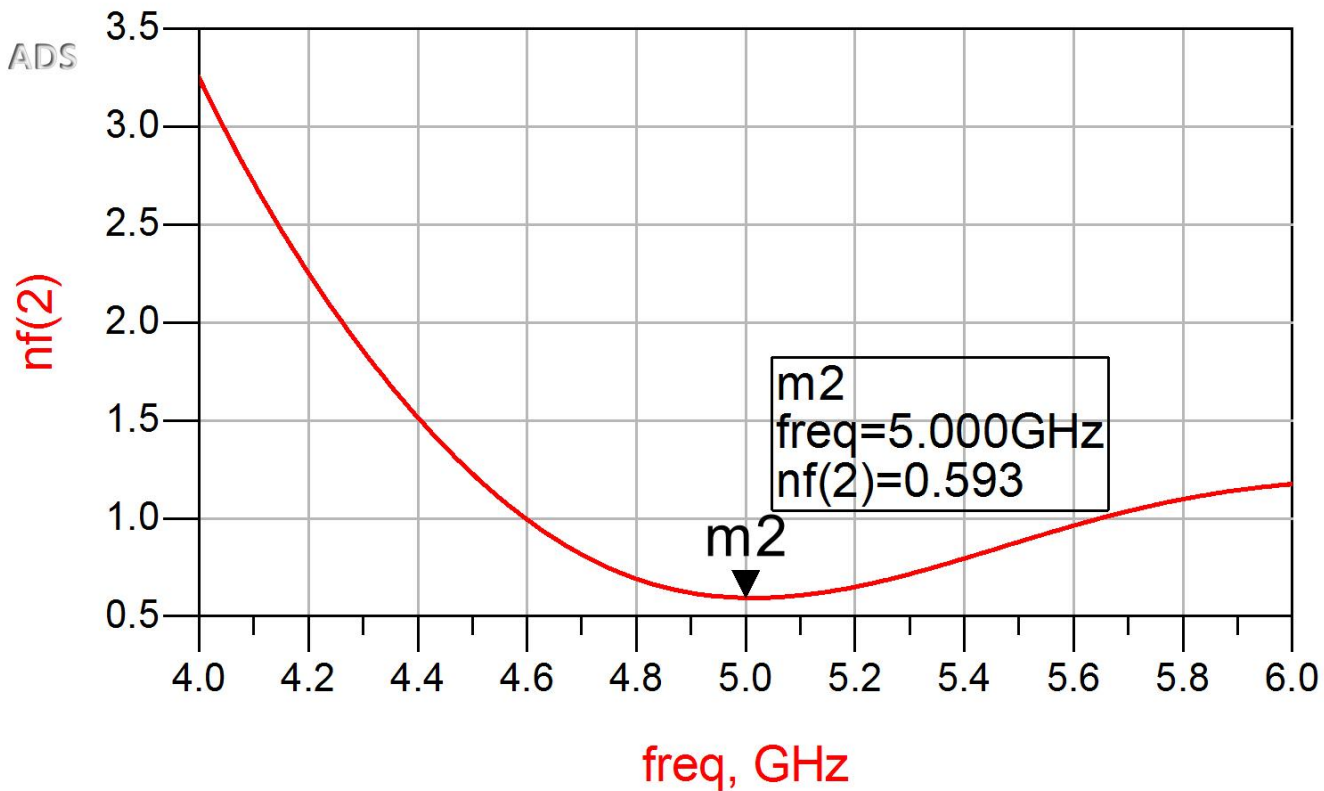
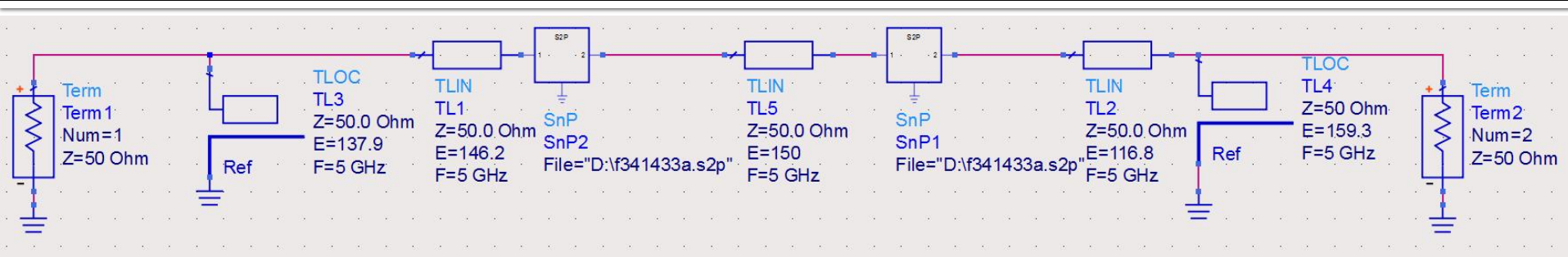
- A **single** transmission line allows reaching a point that cannot be optimized
 - $G_{L_1} = 0.2 \text{ dB}$
 - $G_{S_2} = 1 \text{ dB}$
 - $F_2 = 0.7 \text{ dB}$
- Only one parameter is available for wide band performance tuning



ADS

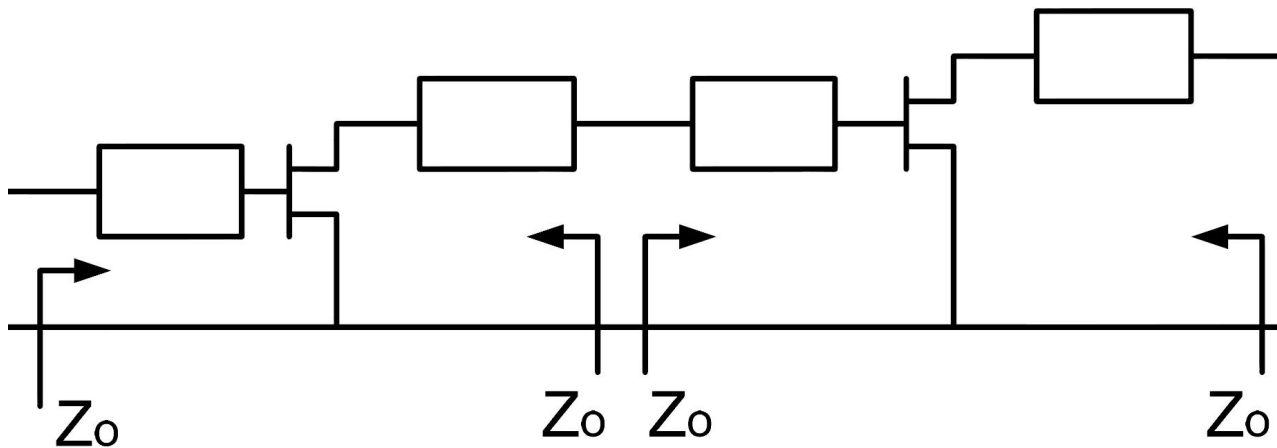


ADS

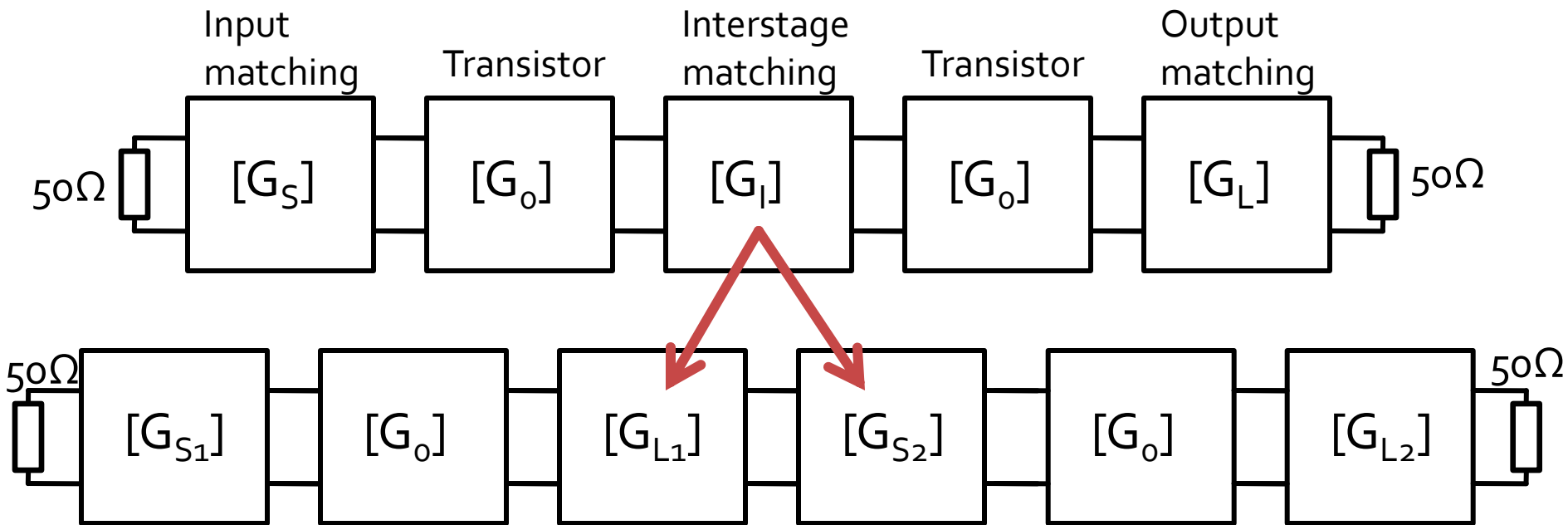


Interstage matching 2

- Using multiple transmission lines for matching each stage to a intermediate $\Gamma=0$ (virtual) allows detailed control over final reflection coefficient (and thus gain/noise)



Interstage matching 2



- Instead of a single match design we have to design two matching networks
- However both matching networks are anchored to a fixed point (50Ω , $\Gamma=0$) so we can use design **formulas** (Impedance Matching with Stubs)
- Also, due to the presence of multiple networks, we can target **precise** positions (reflection coefficients) on both stages

Multistage amplifier

- Power gain

$$G_T[dB] = G_{S1}[dB] + G_0[dB] + G_{L1}[dB] + G_{S2}[dB] + G_0[dB] + G_{L2}[dB]$$

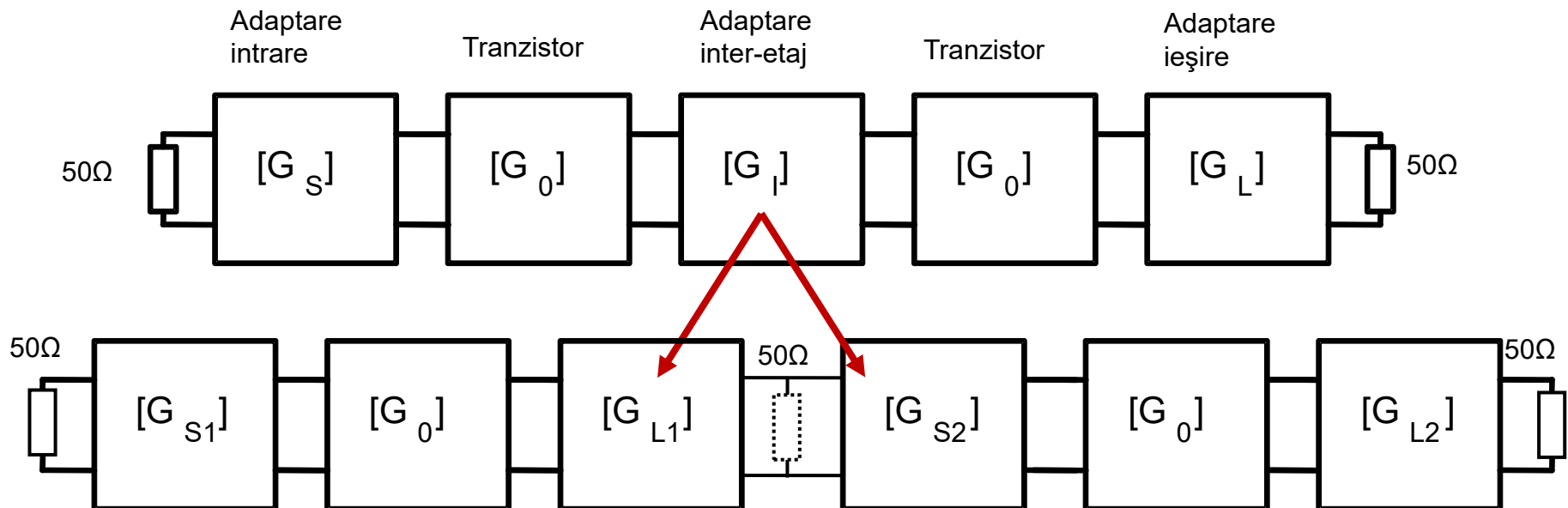
$$G_T[dB] = 1\text{ dB} + 10\text{ dB} + G_{L1}[dB] + G_{S2}[dB] + 10\text{ dB} + 0.2\text{ dB}$$

$$G_T[dB] = 21.2\text{ dB} + \underbrace{G_{L1}[dB] + G_{S2}[dB]}$$

- Interstage match design must provide at least 0.8dB **in total** gain to meet specifications, by separately better matching the output of the first transistor and for the input of the second transistor

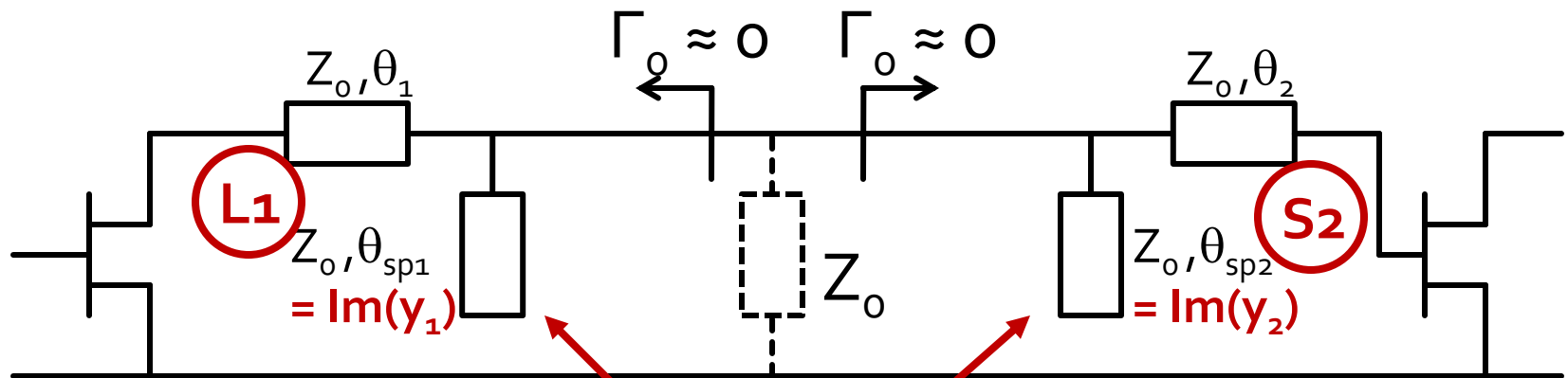
Interstage matching 2

- Using multiple transmission lines for matching each stage to a intermediate $\Gamma=0$ (virtual) allows detailed control over reflection coefficient on both stages



Interstage matching 2

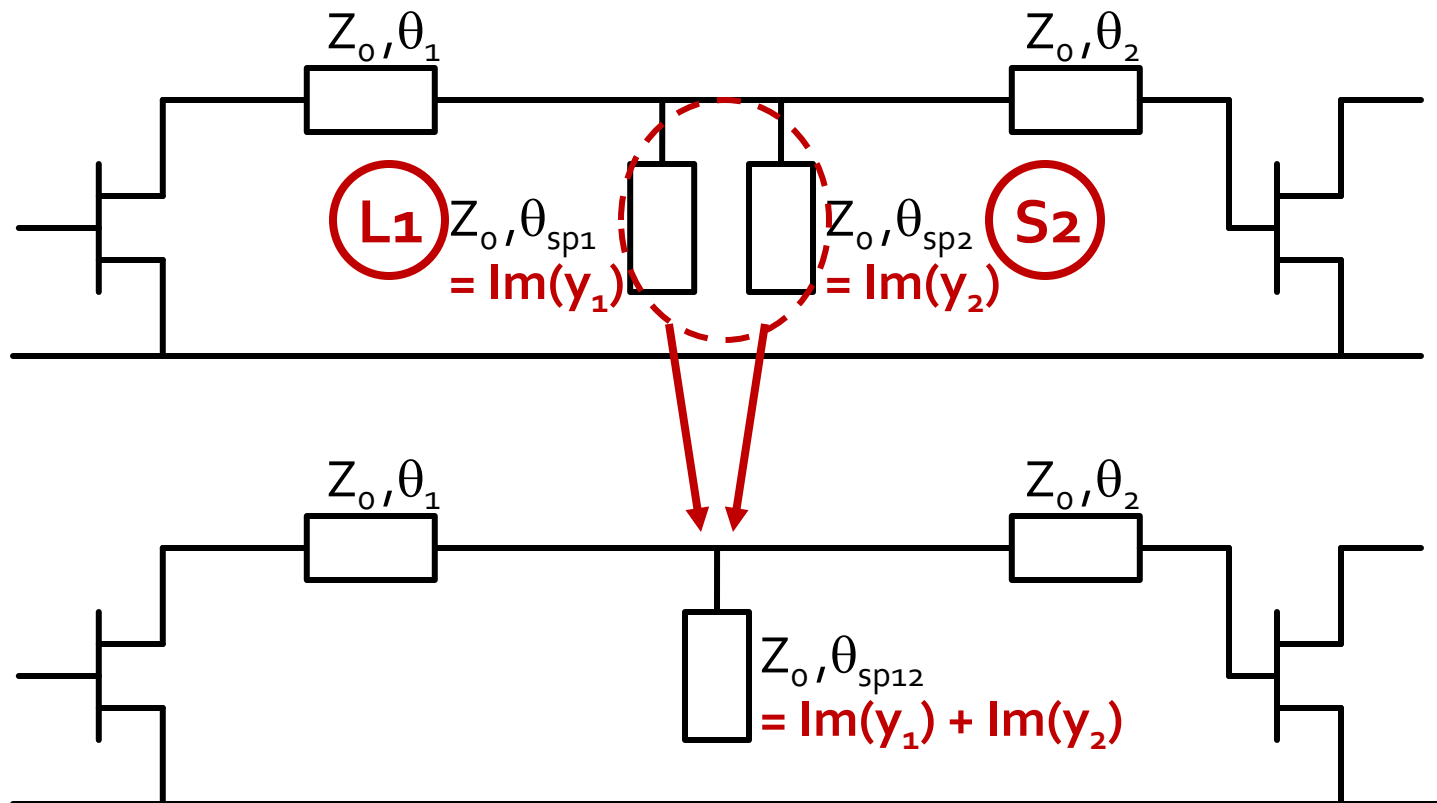
- One of the stages **creates** through its matching network a reflection coefficient $\Gamma=0$ towards which the other stage is matched



The two shunt stubs combine into a single one

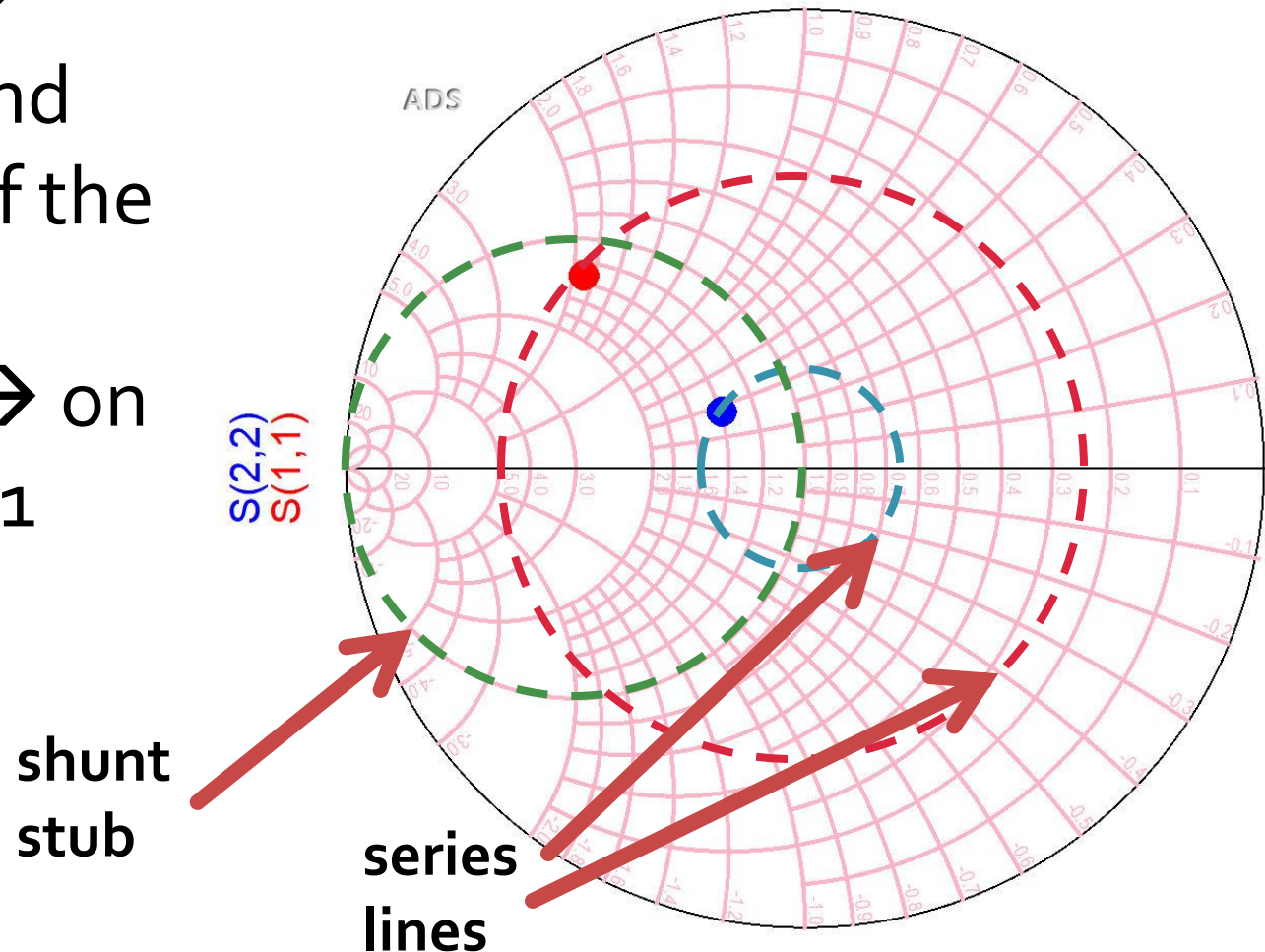
Interstage matching 2

- The two shunt stubs combine into a single one



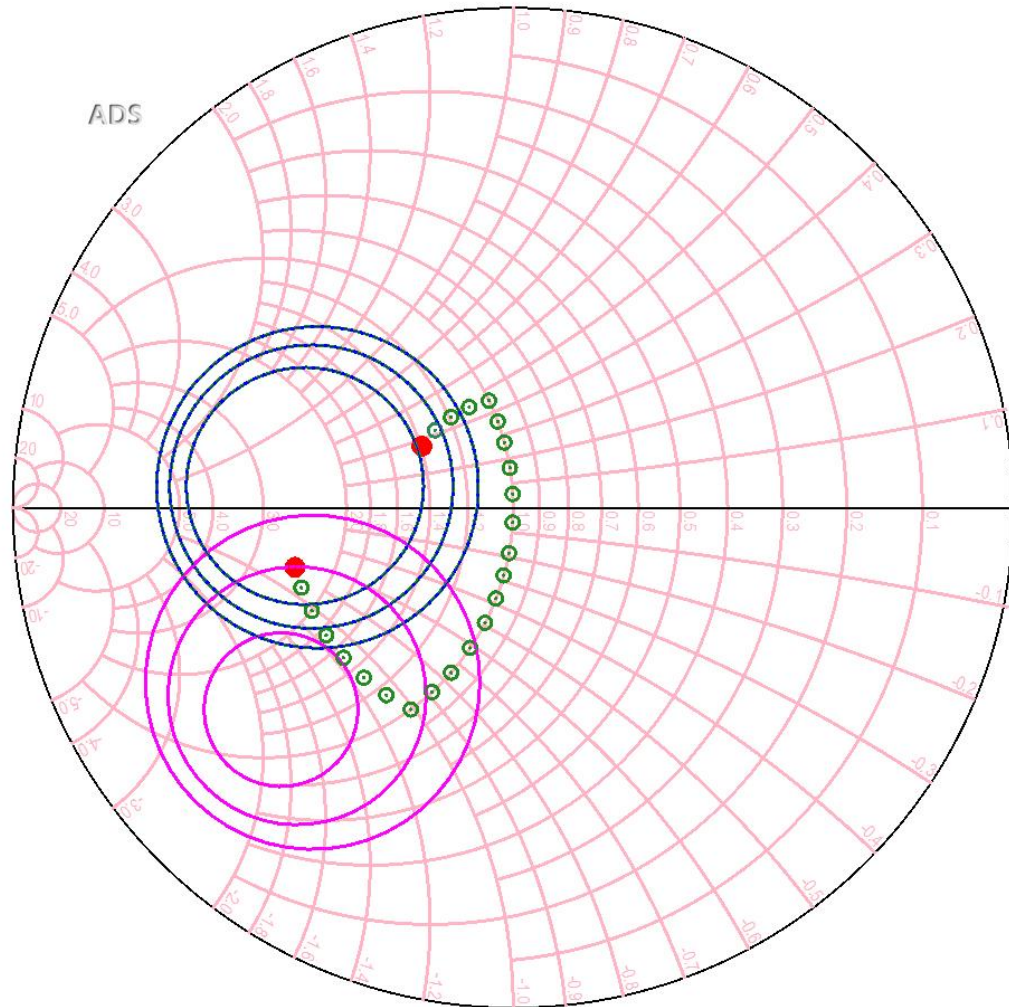
Interstage matching 2

- series line $\rightarrow$ moves around the center of the SC
- shunt stub $\rightarrow$ on the circle $g=1$



Interstage matching 2

- For every stage we use a series line and a shunt stub
 - the series line moves the reflection coefficient from the desired starting point on the unity conductance circle $g=1$
 - the shunt stub moves the point to the center of the Smith Chart (Z_0 match)
- The two shunt stubs will then combine into one



Output matching stage 1 (L1)

- G_{L1} (we use the same point <- output L2), **0.2dB**

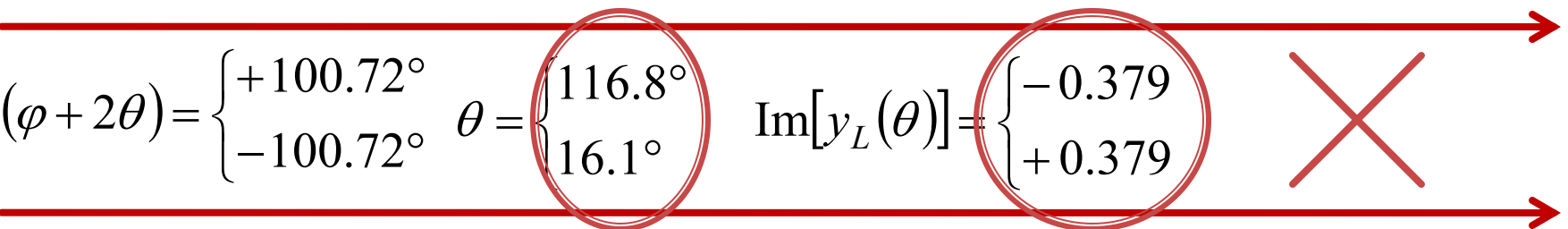
$$\Gamma_L = 0.186 \angle -132.9^\circ$$

$$|\Gamma_L| = 0.186; \quad \varphi = -132.9^\circ$$

$$\cos(\varphi + 2\theta) = -|\Gamma_L| \quad \text{Im}[y_L(\theta)] = \frac{-2 \cdot |\Gamma_L|}{\sqrt{1 - |\Gamma_L|^2}} = -0.379$$

$$\cos(\varphi + 2\theta) = -0.186 \Rightarrow (\varphi + 2\theta) = \pm 100.72^\circ$$

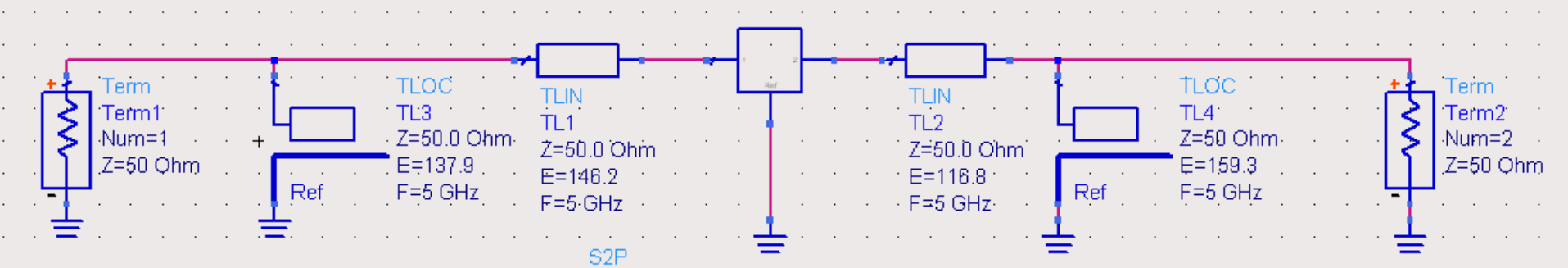
- the length of the shunt stub θ_{sp} is not calculated because it is **not** needed


$$(\varphi + 2\theta) = \begin{cases} +100.72^\circ \\ -100.72^\circ \end{cases} \quad \theta = \begin{cases} 116.8^\circ \\ 16.1^\circ \end{cases} \quad \text{Im}[y_L(\theta)] = \begin{cases} -0.379 \\ +0.379 \end{cases}$$

Output matching stage 1 (L1)

Equation	Solution L1A	Solution L1B
$\Phi+2\theta$	$+100.72^\circ$	-100.72°
θ	116.8°	16.1°
$\text{Im}[y(\theta)]$	-0.379	$+0.379$

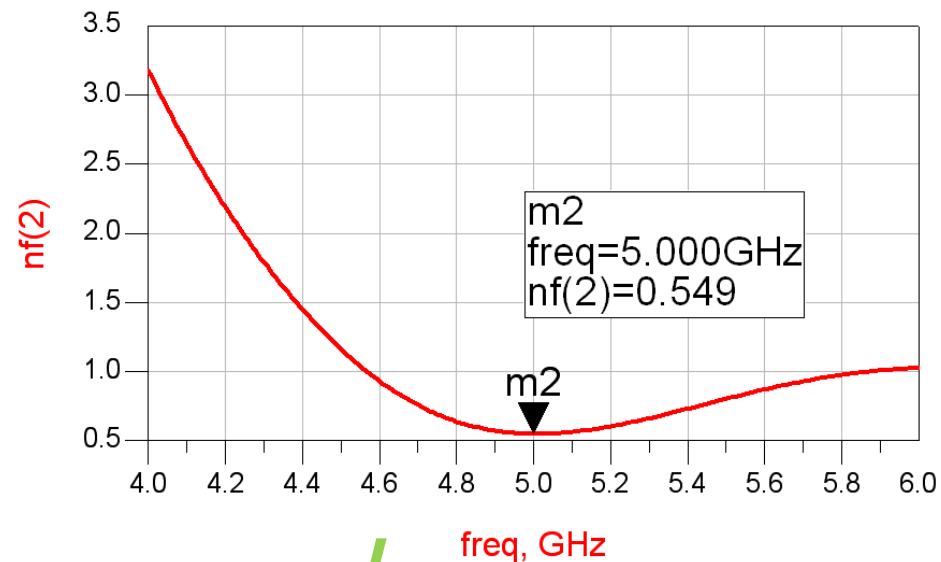
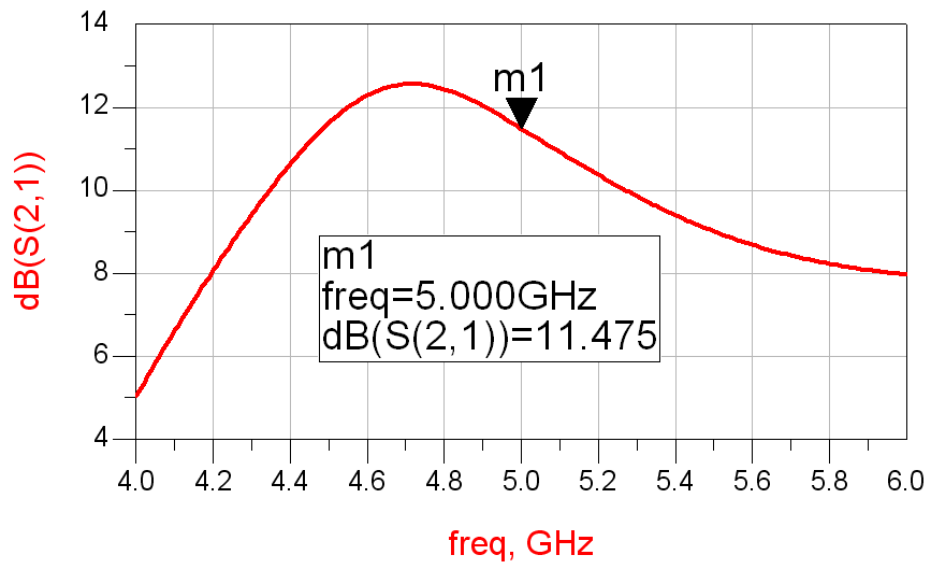
Verify stage 1



G_{S1}

G_0

G_{L1}

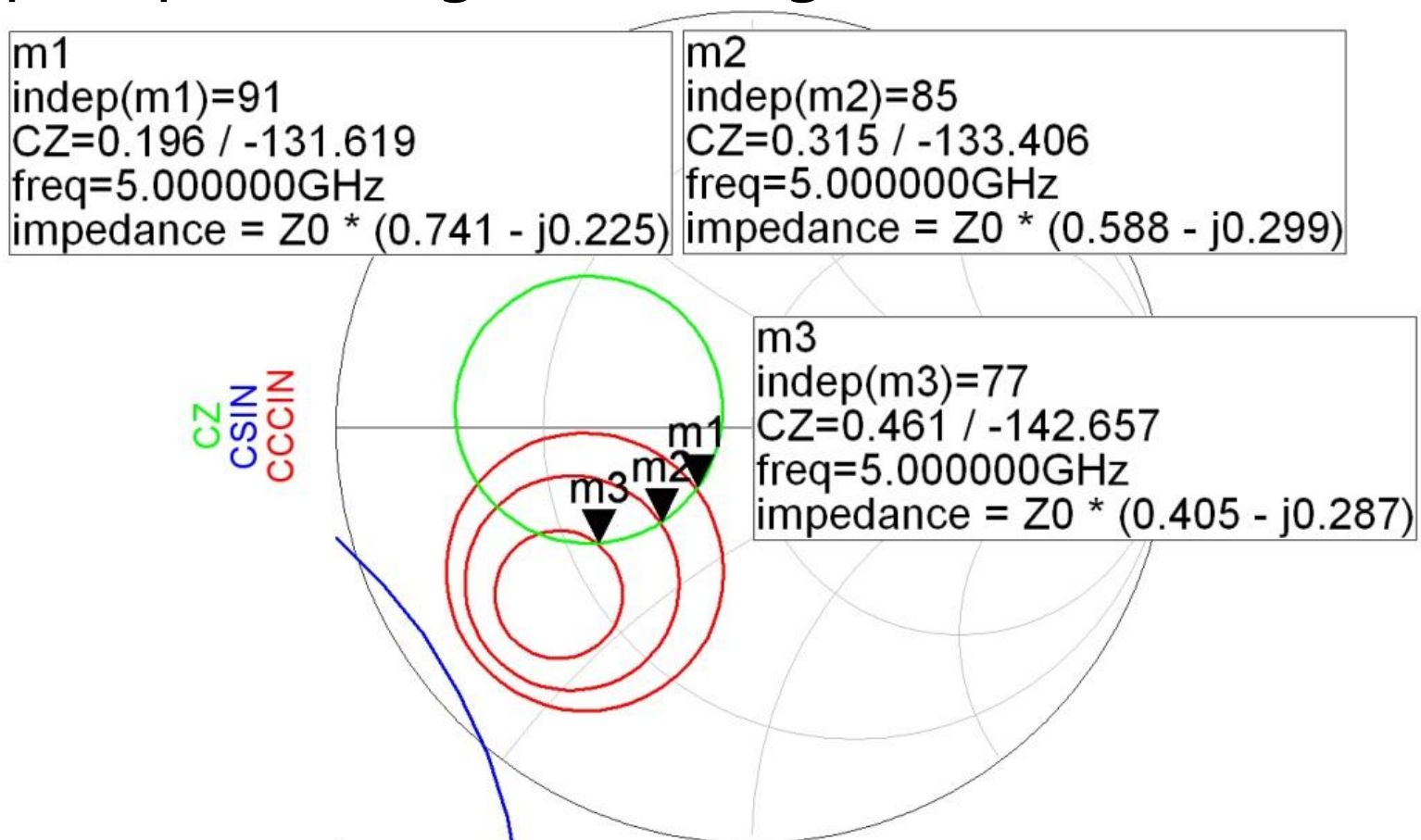


$F_1 < 0.7 \text{ dB}, G_1 > 9 \text{ dB}$



Input matching stage 2 (S2)

- G_{S_2} (moving from Γ_{S_2} we choose towards complex plane origin – **m3** – gain 2dB)



Input matching stage 2 (S2)

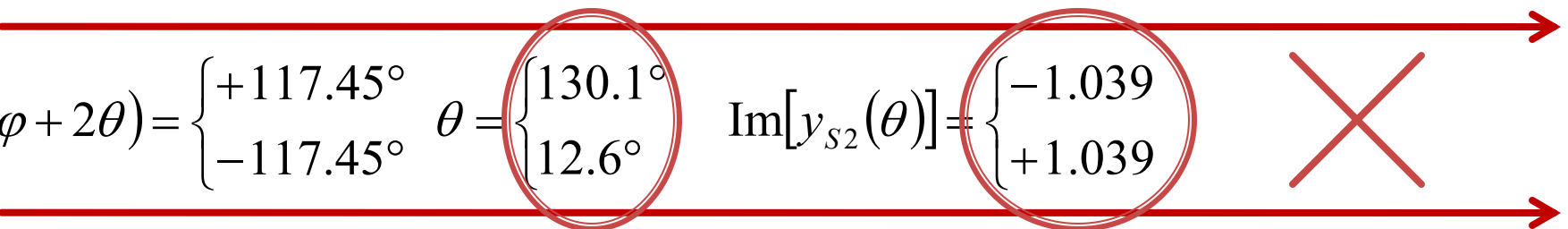
- G_{S2} (going from m3 towards origin), **2dB**

$$\Gamma_{S2} = 0.461 \angle -142.66^\circ \quad |\Gamma_{S2}| = 0.461; \quad \varphi = -142.66^\circ$$

$$\cos(\varphi + 2\theta) = -|\Gamma_{S2}| \quad \text{Im}[y_{S2}(\theta)] = \frac{\mp 2 \cdot |\Gamma_{S2}|}{\sqrt{1 - |\Gamma_{S2}|^2}}$$

$$\cos(\varphi + 2\theta) = -0.461 \Rightarrow (\varphi + 2\theta) = \pm 117.45^\circ$$

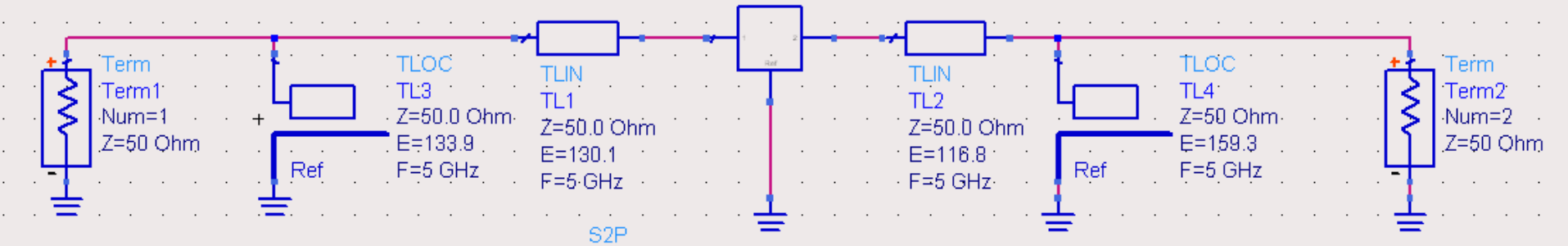
- the length of the shunt stub θ_{sp} is not calculated because it is **not** needed


$$(\varphi + 2\theta) = \begin{cases} +117.45^\circ \\ -117.45^\circ \end{cases} \quad \theta = \begin{cases} 130.1^\circ \\ 12.6^\circ \end{cases} \quad \text{Im}[y_{S2}(\theta)] = \begin{cases} -1.039 \\ +1.039 \end{cases}$$

Input matching stage 2 (S2)

Equation	Solution S2A	Solution S2B
$\Phi+2\theta$	$+117.45^\circ$	-117.45°
θ	130.1°	12.6°
$\text{Im}[y(\theta)]$	-1.039	$+1.039$

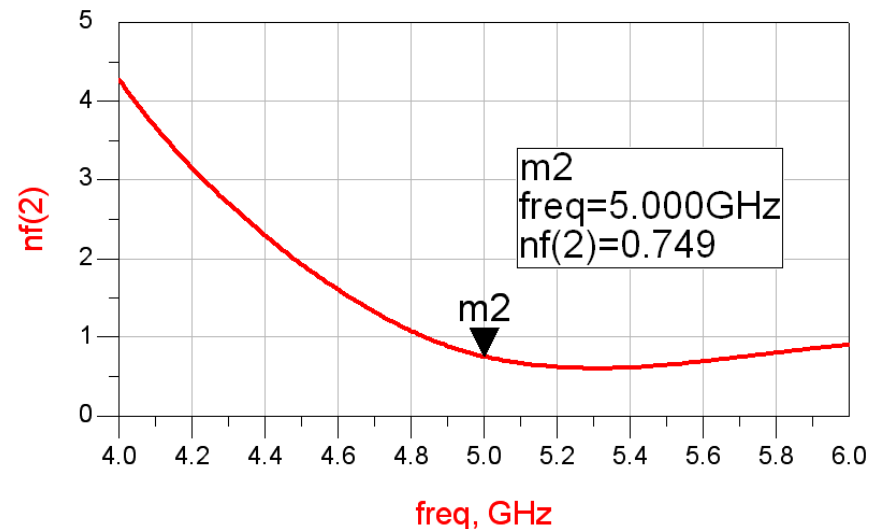
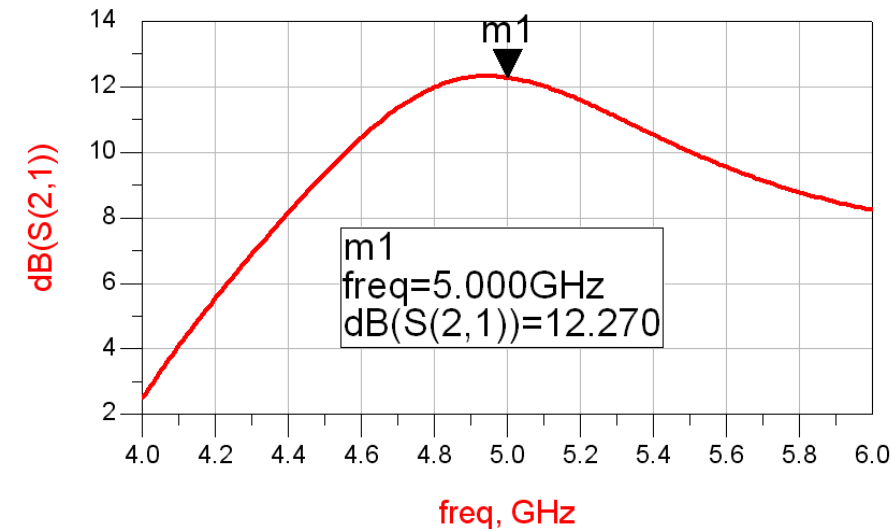
Verify stage 2



G_{S1}

G_0

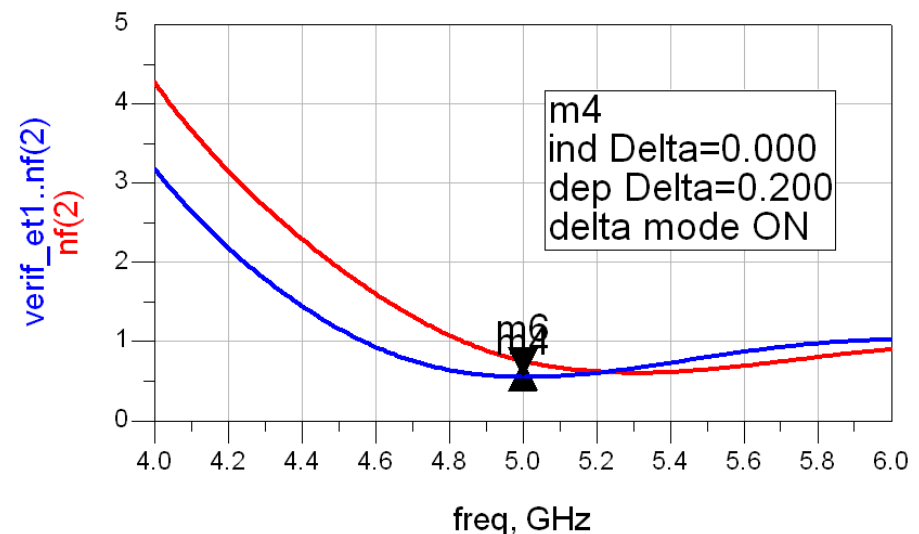
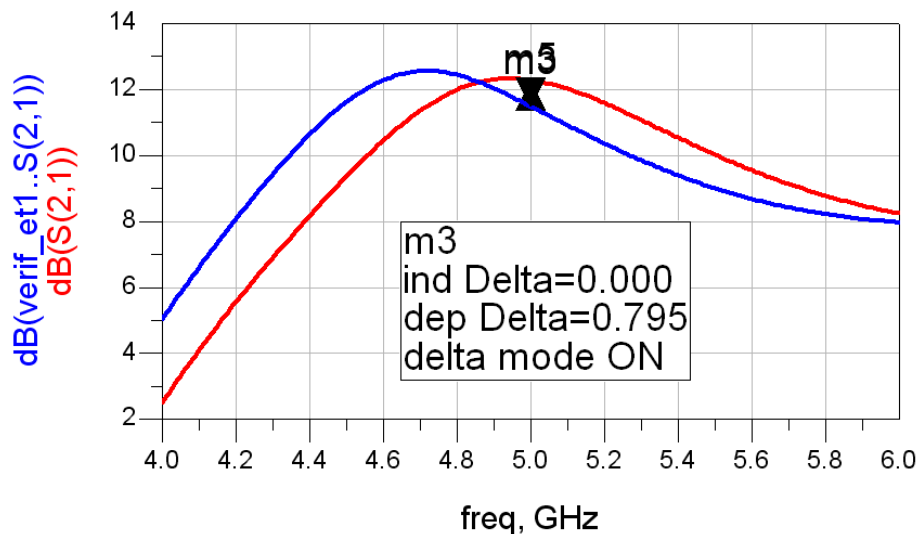
G_{L1}



$F_2 < 1.2\text{ dB}$, $G_2 < 13\text{ dB}$ **X** $G_1 = 11.5\text{ dB}$, $G_2 = 12.3\text{ dB}$, $G_1 + G_2 > 22\text{ dB}$ **✓**

Stage 1/2

- According to the conclusions of the Friis formula, the second stage obtains a higher gain because a higher noise is acceptable.



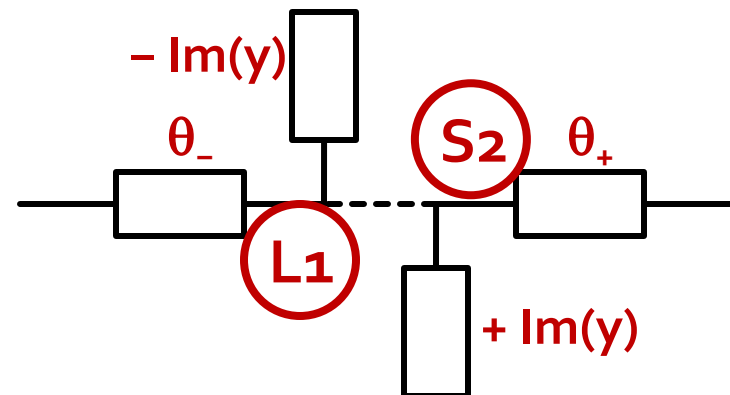
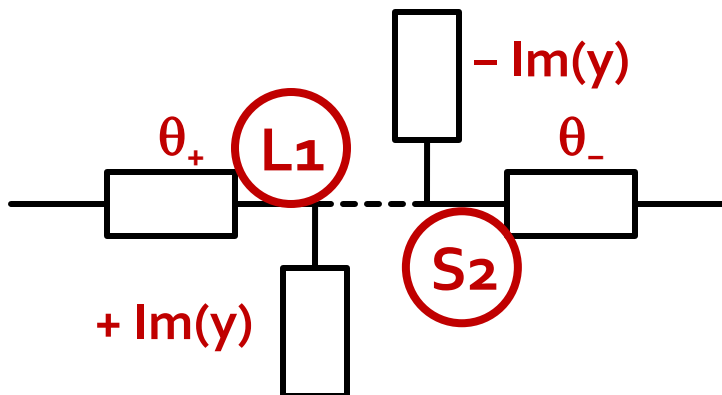
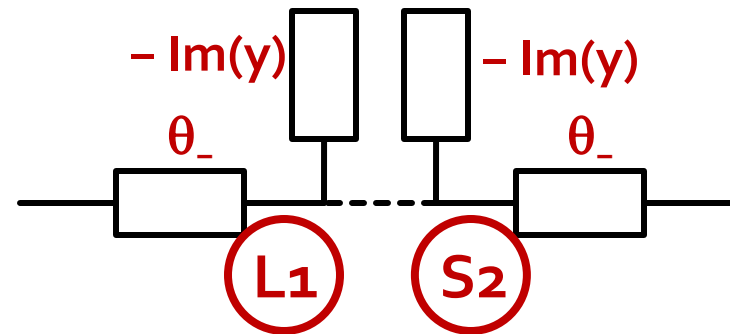
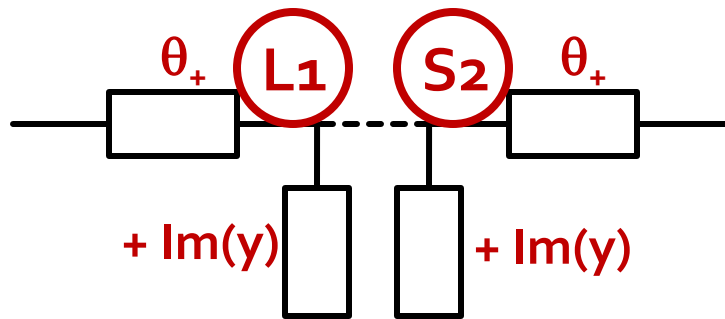
Merging the two shunt stubs

- **The two shunt stubs merge into a single one**
- There are **4 possible combinations** depending on how we chose the electrical length for the two series lines
 - for each chosen electric length (θ) the corresponding $\text{Im}[y(\theta)]$ must be used
- Ex:

$$\theta_{L1} = 116.8^\circ \quad \theta_{S2} = 130.1^\circ \quad \text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = -1.418$$
$$\theta_{sp} = \tan^{-1}(\text{Im}[y_{sp}]) \quad \theta_{sp} = 125.2^\circ$$

Merging the two shunt stubs

- 4 possible combinations
 - the **admittances** are in parallel and **add** up, not the electrical lengths



$$Im[y_{sp}] = Im[y_{L1}(\theta)] + Im[y_{S2}(\theta)]$$

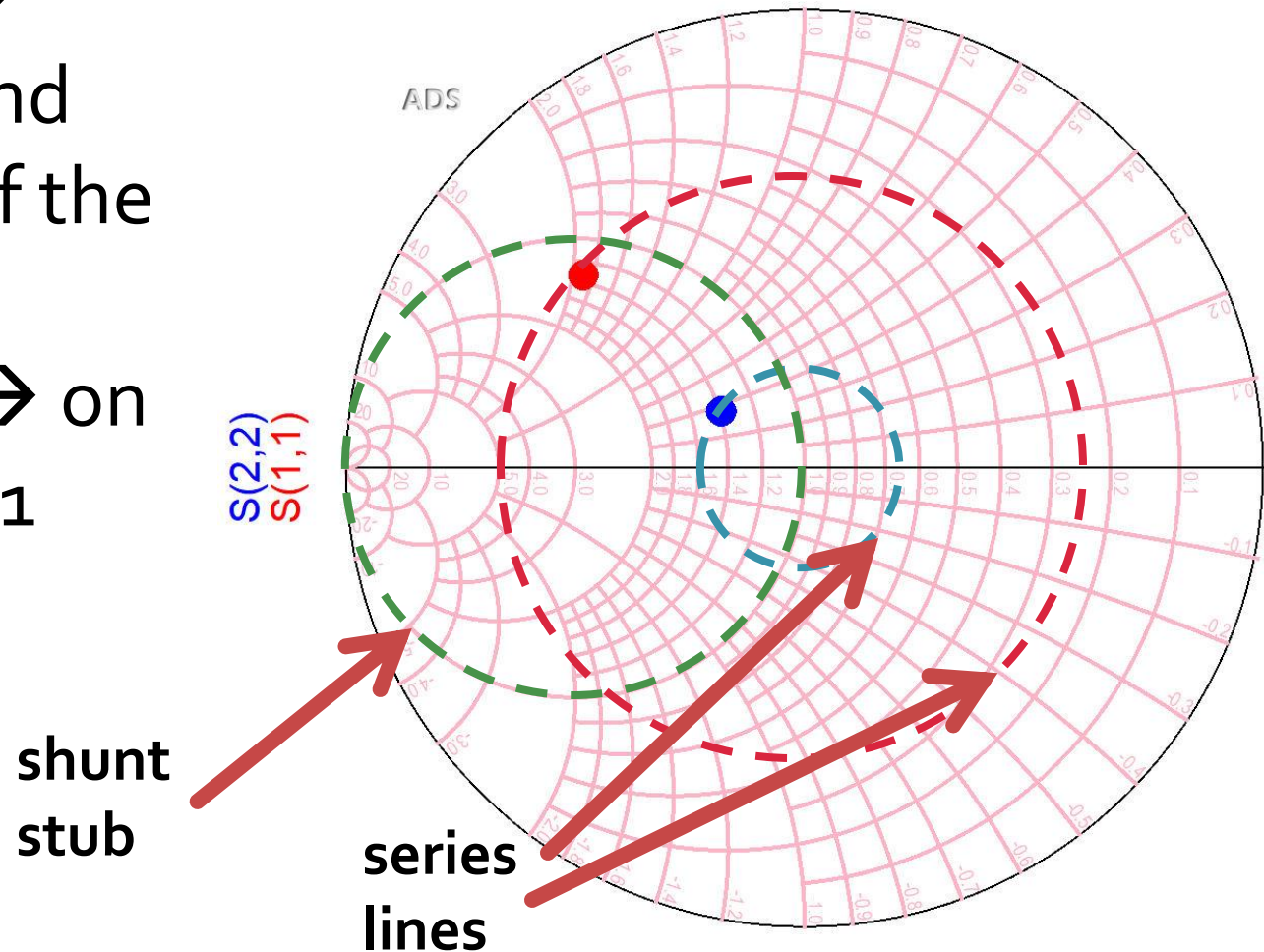
$$\theta_{sp} = \tan^{-1}(Im[y_{sp}])$$

Merging the two shunt stubs

		Solution S2A	Solution S2B
		$\theta = 130.1^\circ$ $\text{Im}[y(\theta)] = -1.039$	$\theta = 12.6^\circ$ $\text{Im}[y(\theta)] = +1.039$
Solution L1A	$\theta = 116.8^\circ$ $\text{Im}[y(\theta)] = -0.379$	$\theta_{L1} = 116.8^\circ$ $\text{Im}[y(\theta)] = -1.418$ $\theta_p = 125.2^\circ$ $\theta_{S2} = 130.1^\circ$	$\theta_{L1} = 116.8^\circ$ $\text{Im}[y(\theta)] = +0.66$ $\theta_p = 33.4^\circ$ $\theta_{S2} = 12.6^\circ$
Solution L1B	$\theta = 16.1^\circ$ $\text{Im}[y(\theta)] = +0.379$	$\theta_{L1} = 16.1^\circ$ $\text{Im}[y(\theta)] = -0.66$ $\theta_p = 146.6^\circ$ $\theta_{S2} = 130.1^\circ$	$\theta_{L1} = 16.1^\circ$ $\text{Im}[y(\theta)] = 1.418$ $\theta_p = 54.8^\circ$ $\theta_{S2} = 12.6^\circ$

Smith Chart

- series line $\rightarrow$ moves around the center of the SC
- shunt stub $\rightarrow$ on the circle $g=1$



Merge 1, Smith Chart

$$\theta_{L1} = 116.8^\circ \quad \theta_{S2} = 130.1^\circ$$

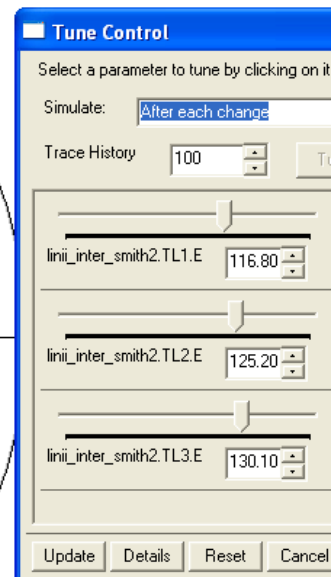
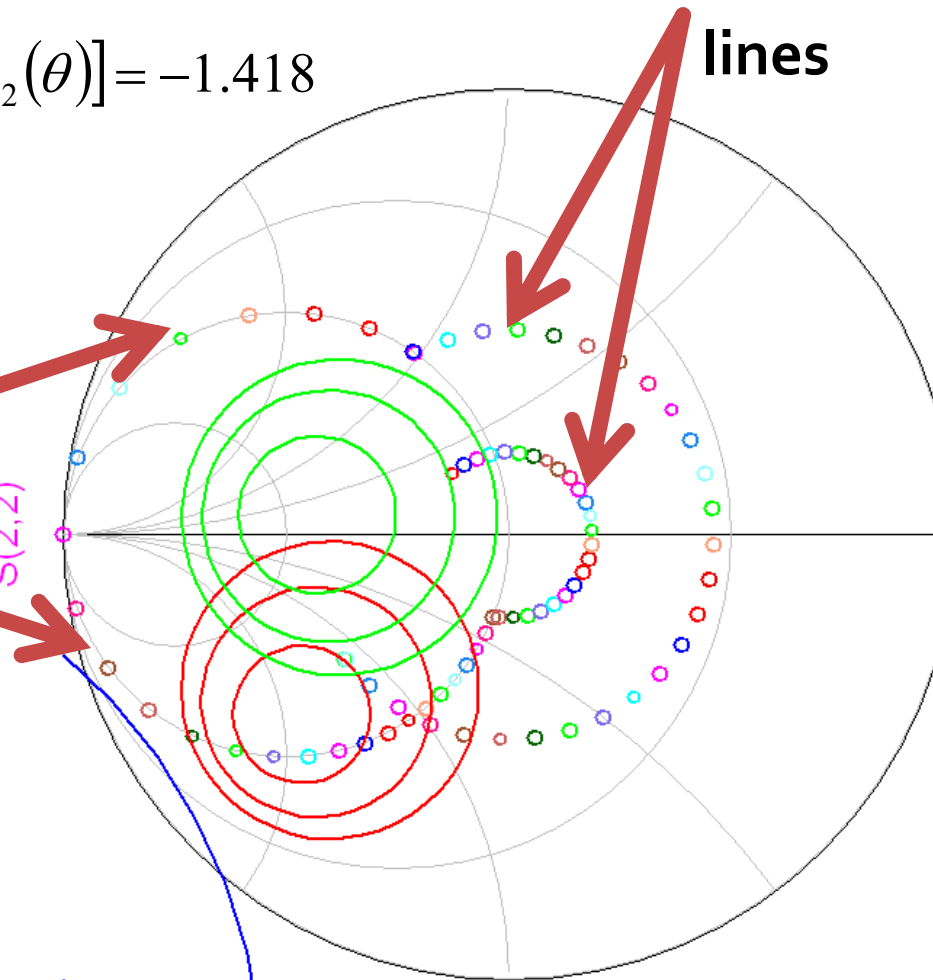
$$\text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = -1.418$$

$$\theta_{sp} = 125.2^\circ$$

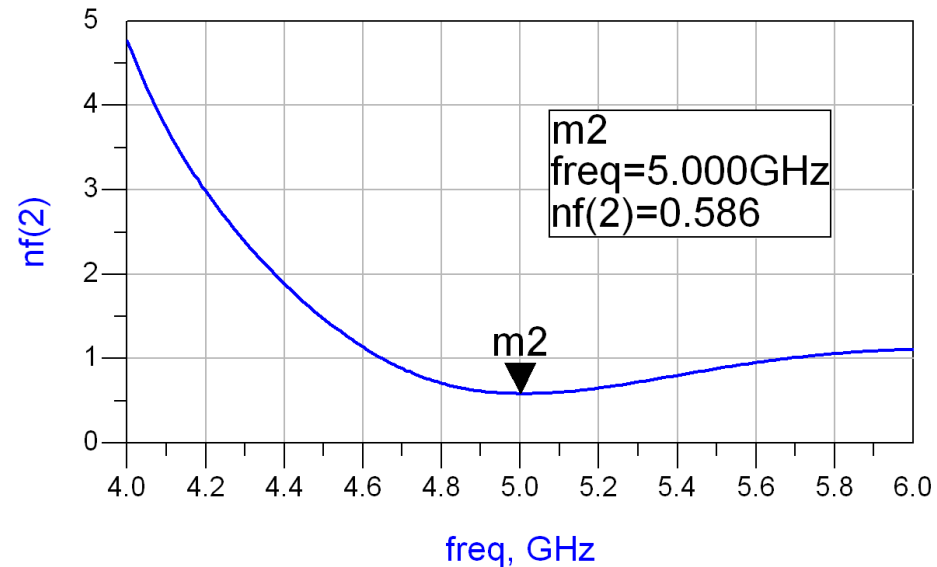
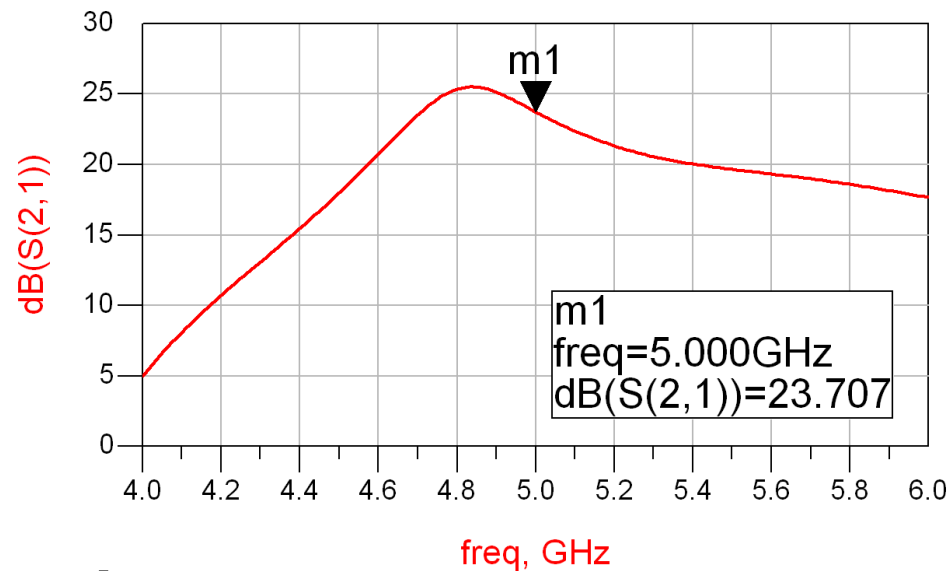
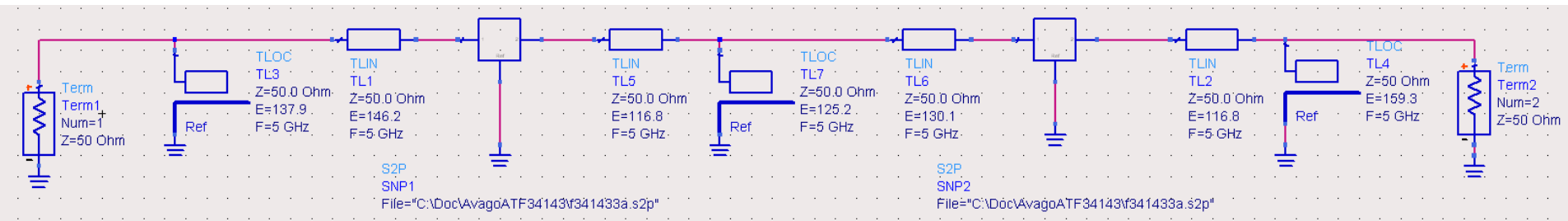
"combined"
stub

ref..CSIN
ref..CZ
ref..CCIN
S(2,2)

series
lines



Merge 1, ADS



Merge 2, Smith Chart

$$\theta_{L1} = 116.8^\circ \quad \theta_{S2} = 12.6^\circ$$

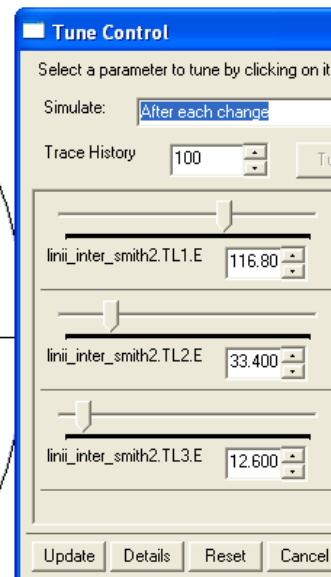
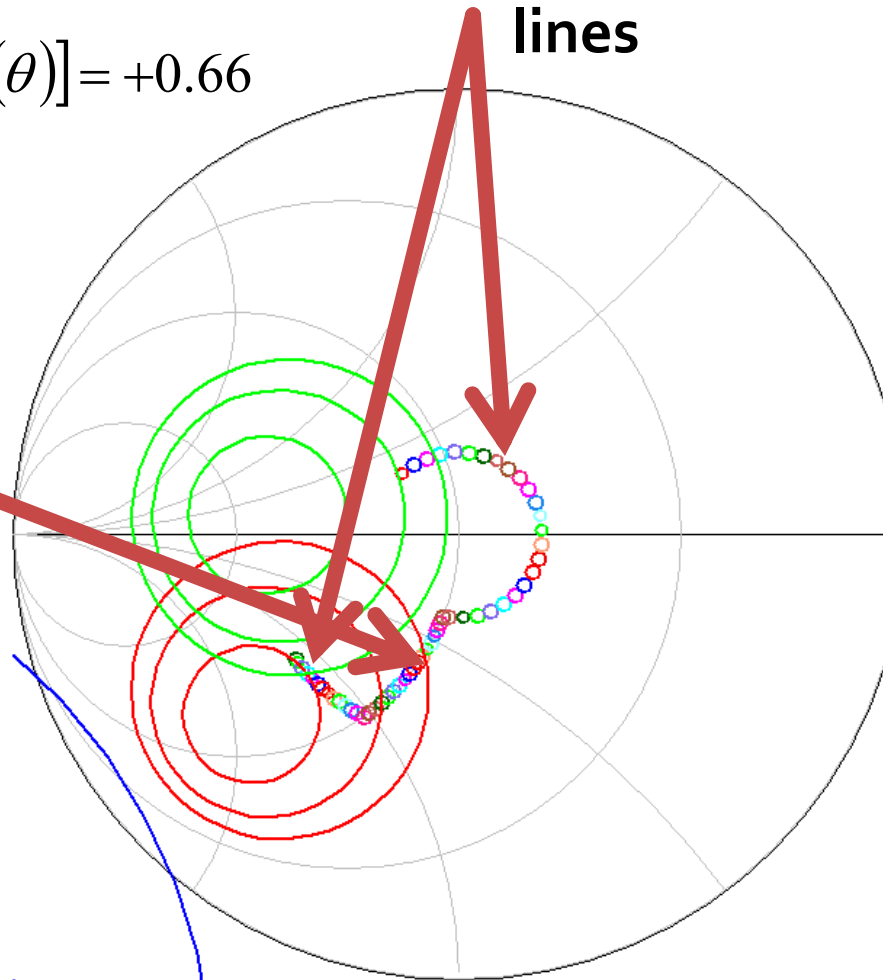
$$\text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = +0.66$$

$$\theta_{sp} = 33.4^\circ$$

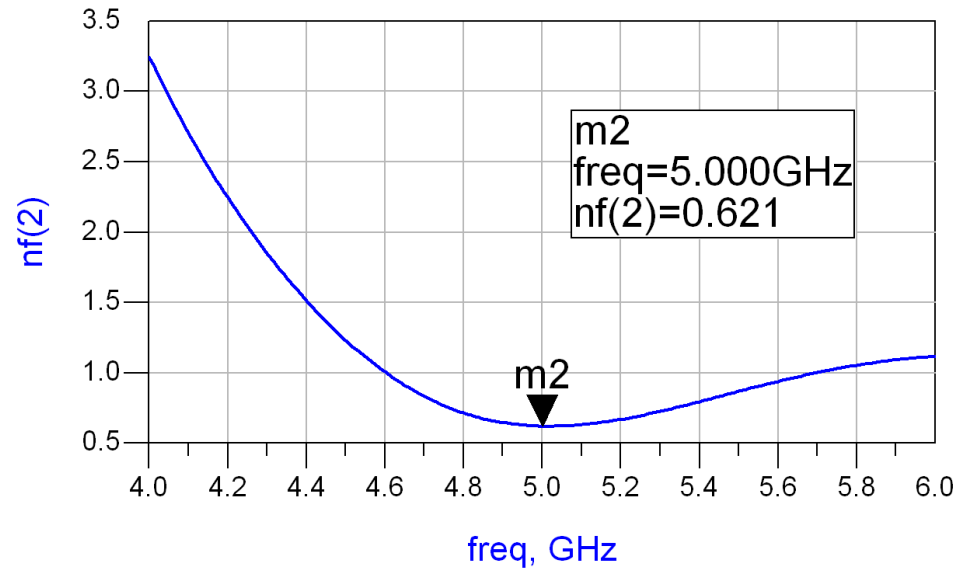
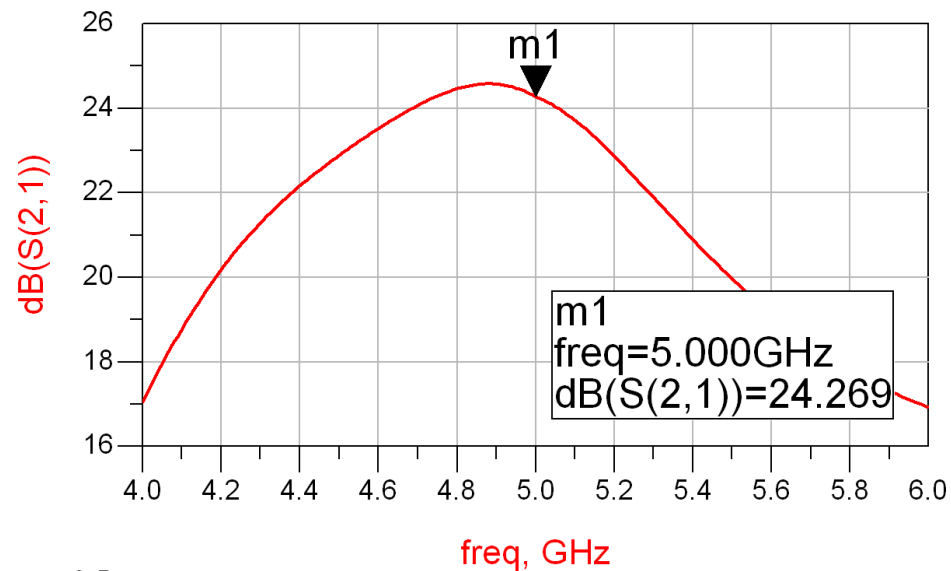
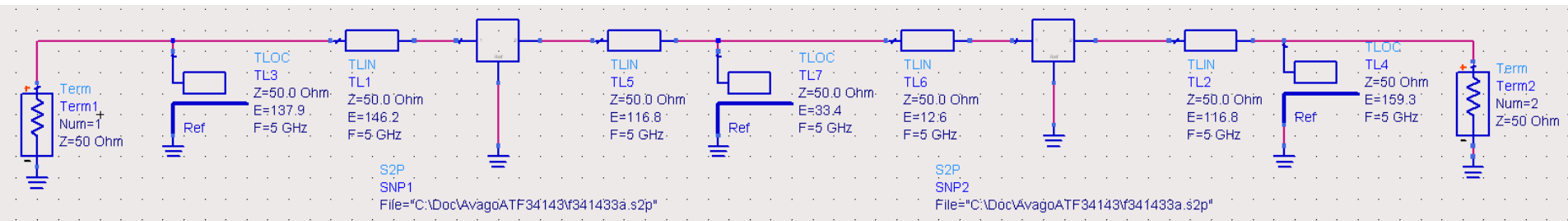
**“combined”
stub**

ref..CSIN
ref..CZ
ref..CCCN
S(2,2)

**series
lines**



Merge 2, ADS



Merge 3, Smith Chart

$$\theta_{L1} = 16.1^\circ \quad \theta_{S2} = 130.1^\circ$$

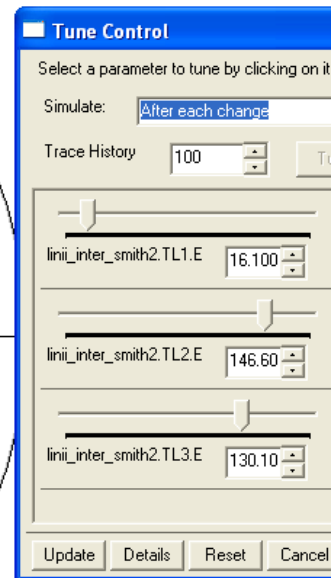
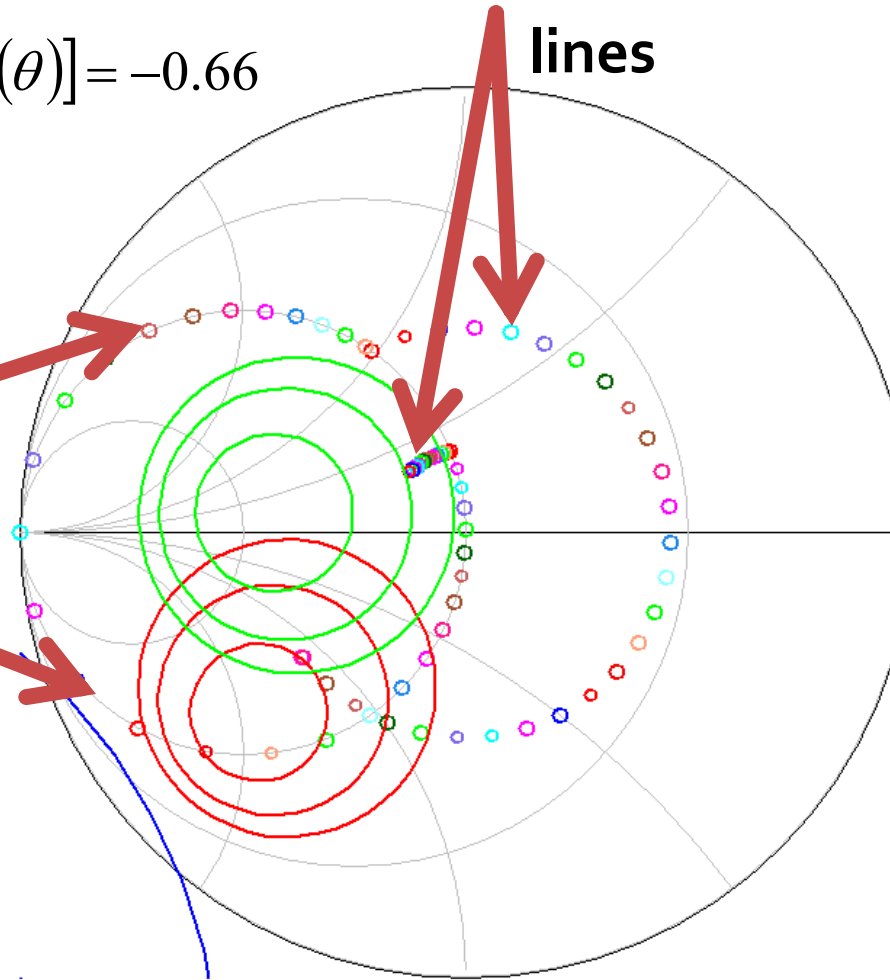
$$\text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = -0.66$$

$$\theta_{sp} = 146.6^\circ$$

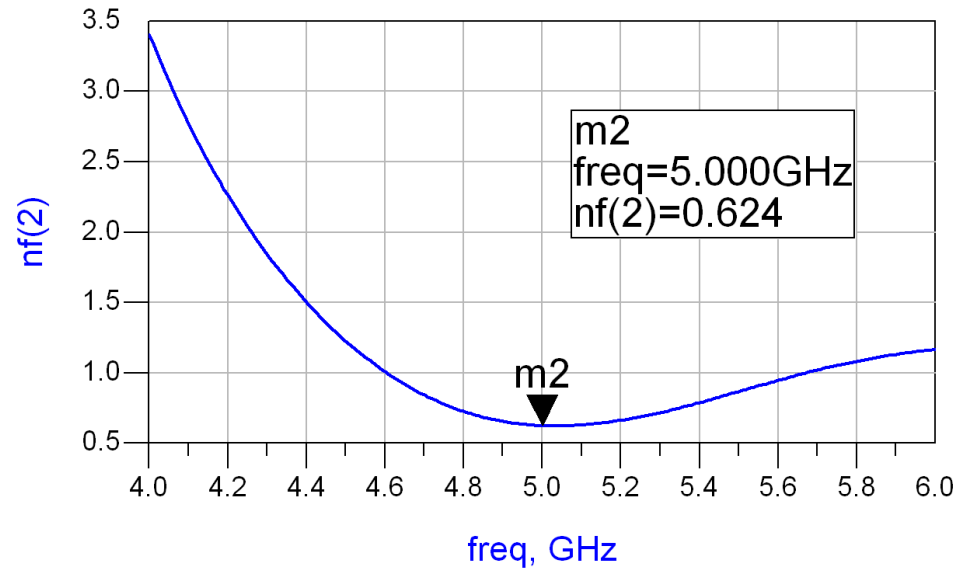
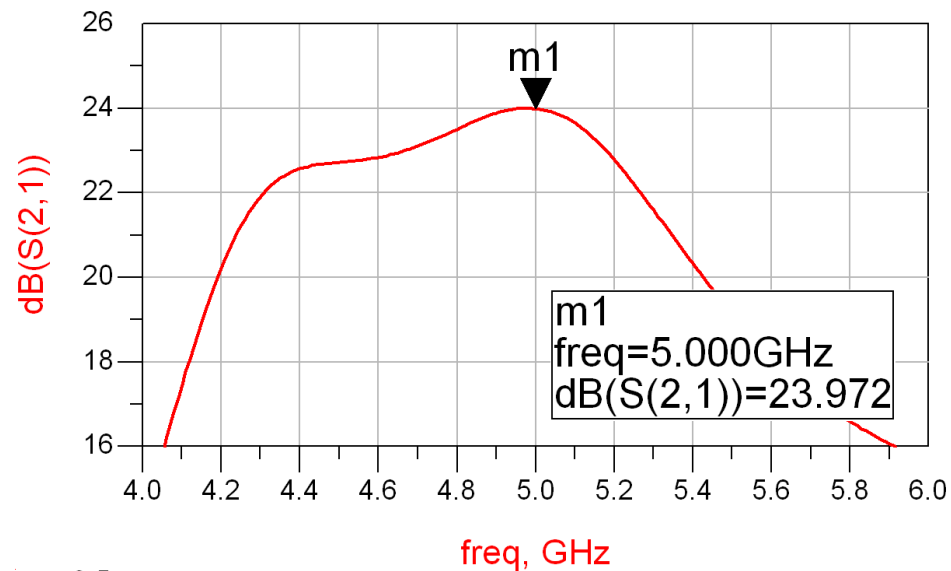
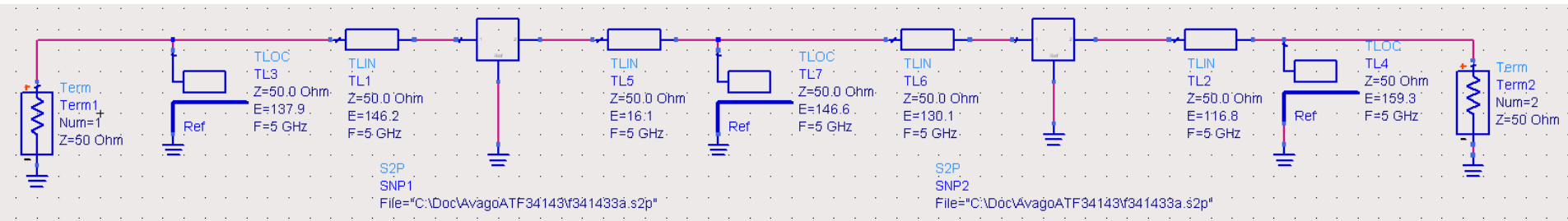
"combined"
stub

ref..CSIN
ref..CZ
ef..CCCN
S(2,2)

series
lines



Merge 3, ADS



Merge 4, Smith Chart

$$\theta_{L1} = 16.1^\circ \quad \theta_{S2} = 12.6^\circ$$

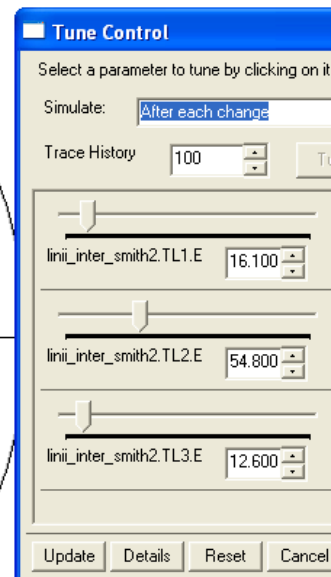
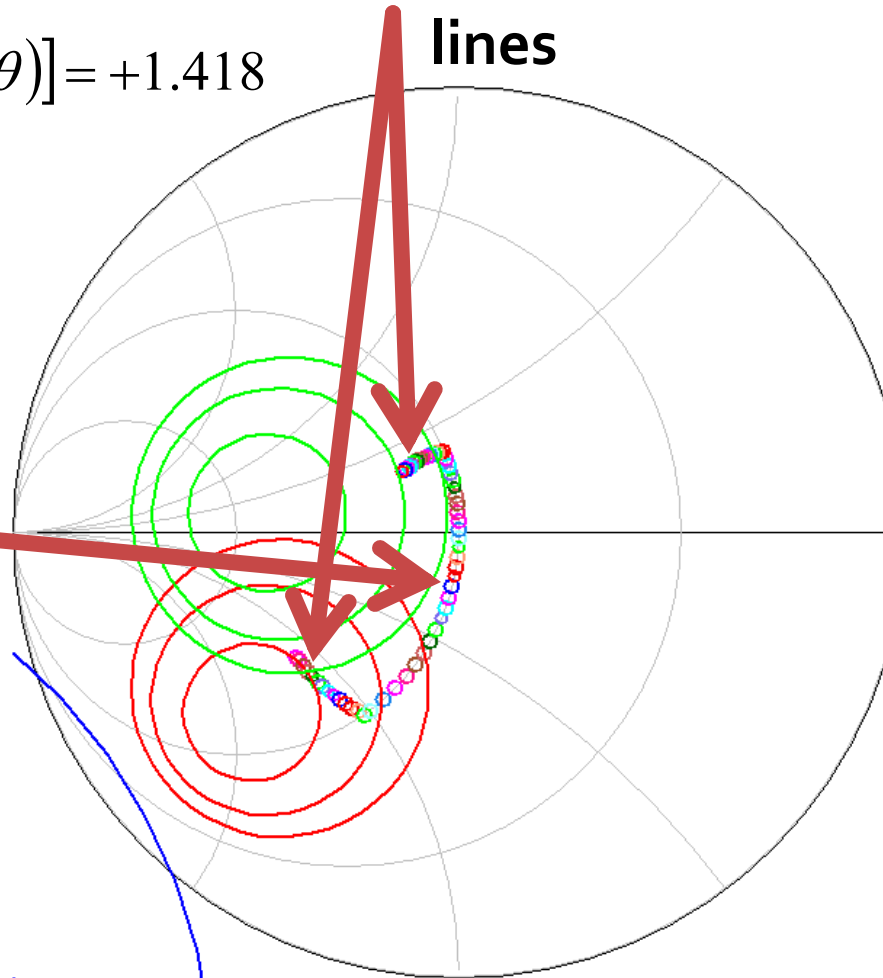
$$\text{Im}[y_{sp}] = \text{Im}[y_{L1}(\theta)] + \text{Im}[y_{S2}(\theta)] = +1.418$$

$$\theta_{sp} = 54.8^\circ$$

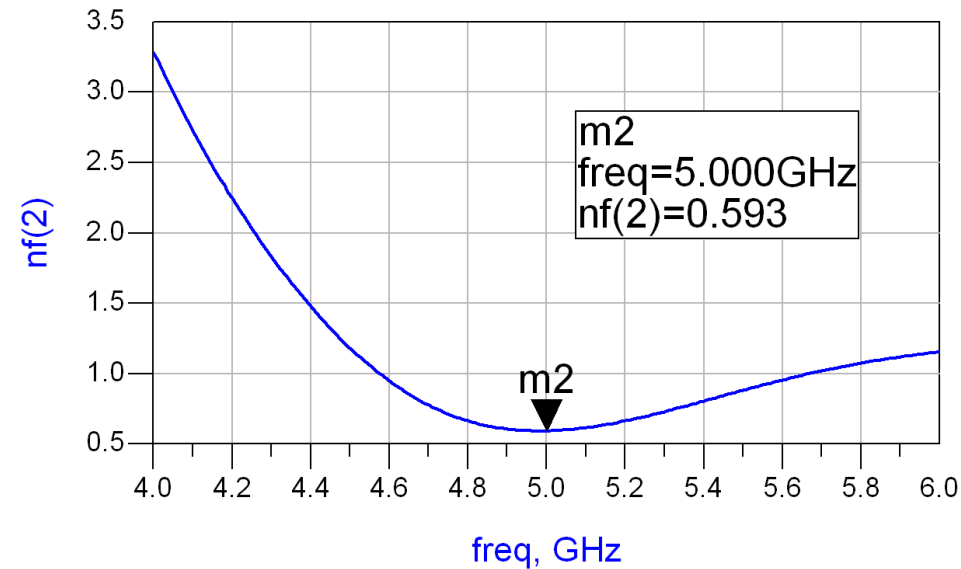
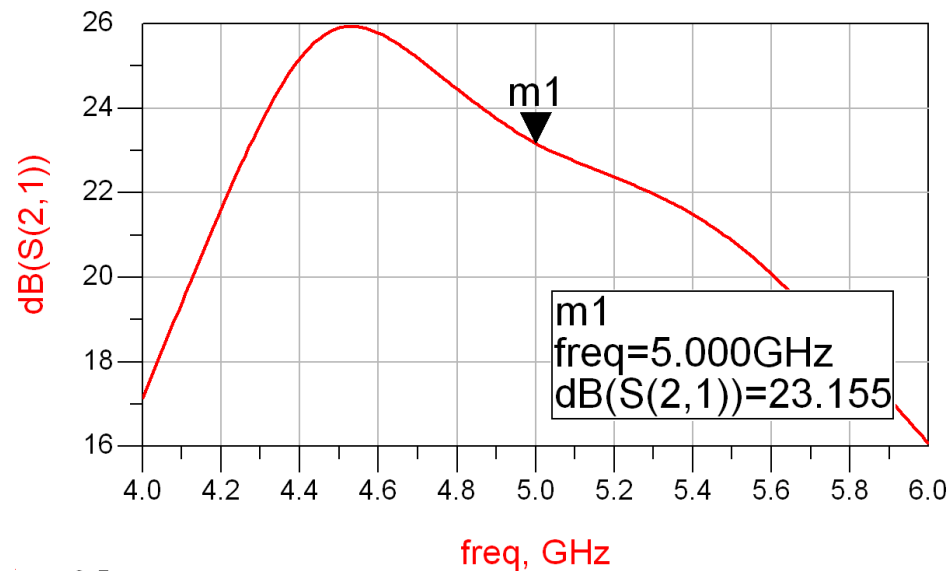
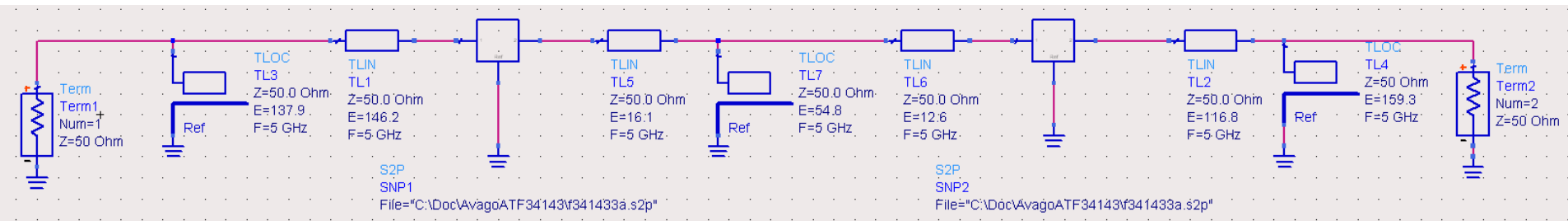
"combined"
stub

ref.:CSIN
ref.:CZ
ref.:CCIN
S(,2)

series
lines



Merge 4, ADS



Interstage matching 2

- All the combinations obtained meet the target conditions for gain and noise
- Choose a convenient one depending on:
 - the physical dimensions of the lines $l = \frac{\theta}{360^\circ} \cdot \lambda$
 - frequency bandwidth/flatness
 - stability
 - performance (noise/gain)
 - input and output reflection
 - etc.

Supplement Mini Project

Implementation in microstrip technology

- microstrip lines
 - dielectric layer
 - plane metallization (ground plane)
 - traces which will control:
 - characteristic impedance
 - physical/electrical length

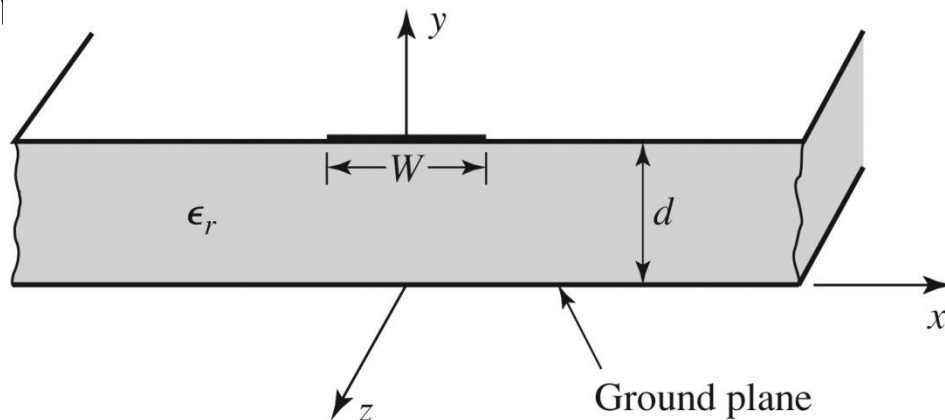


Figure 3.25a
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Implementation in microstrip technology

- quasiTEM line

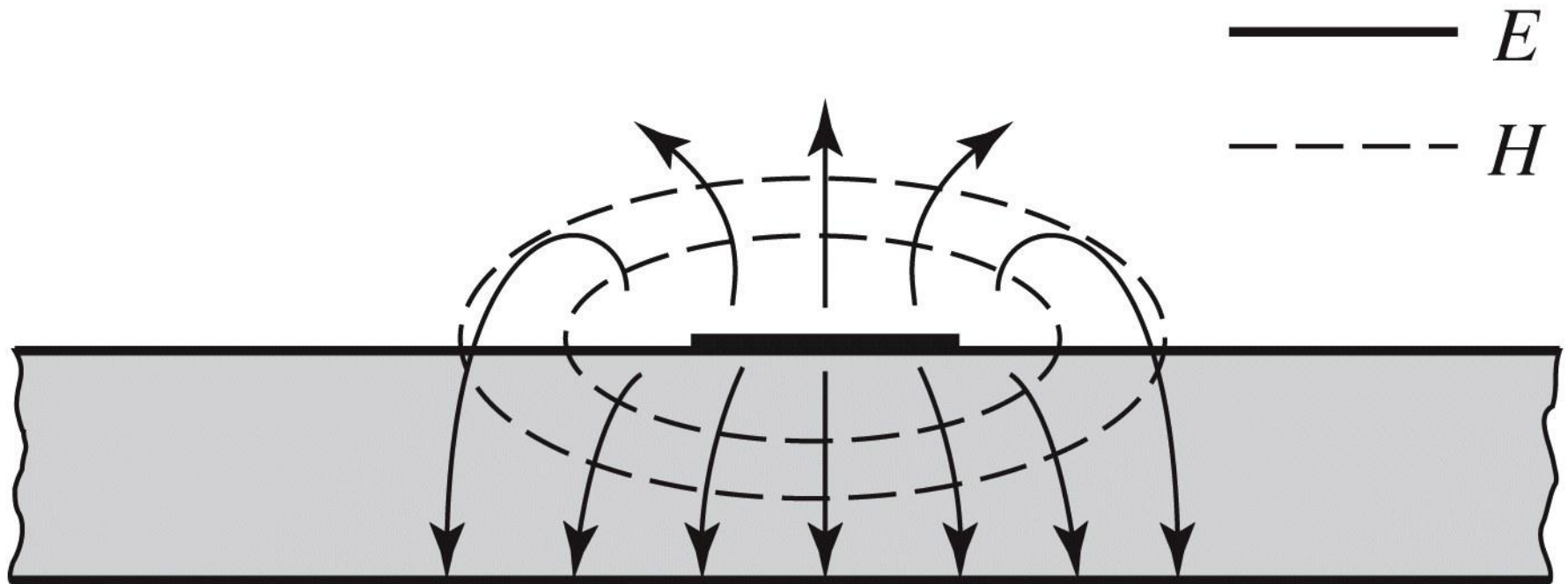
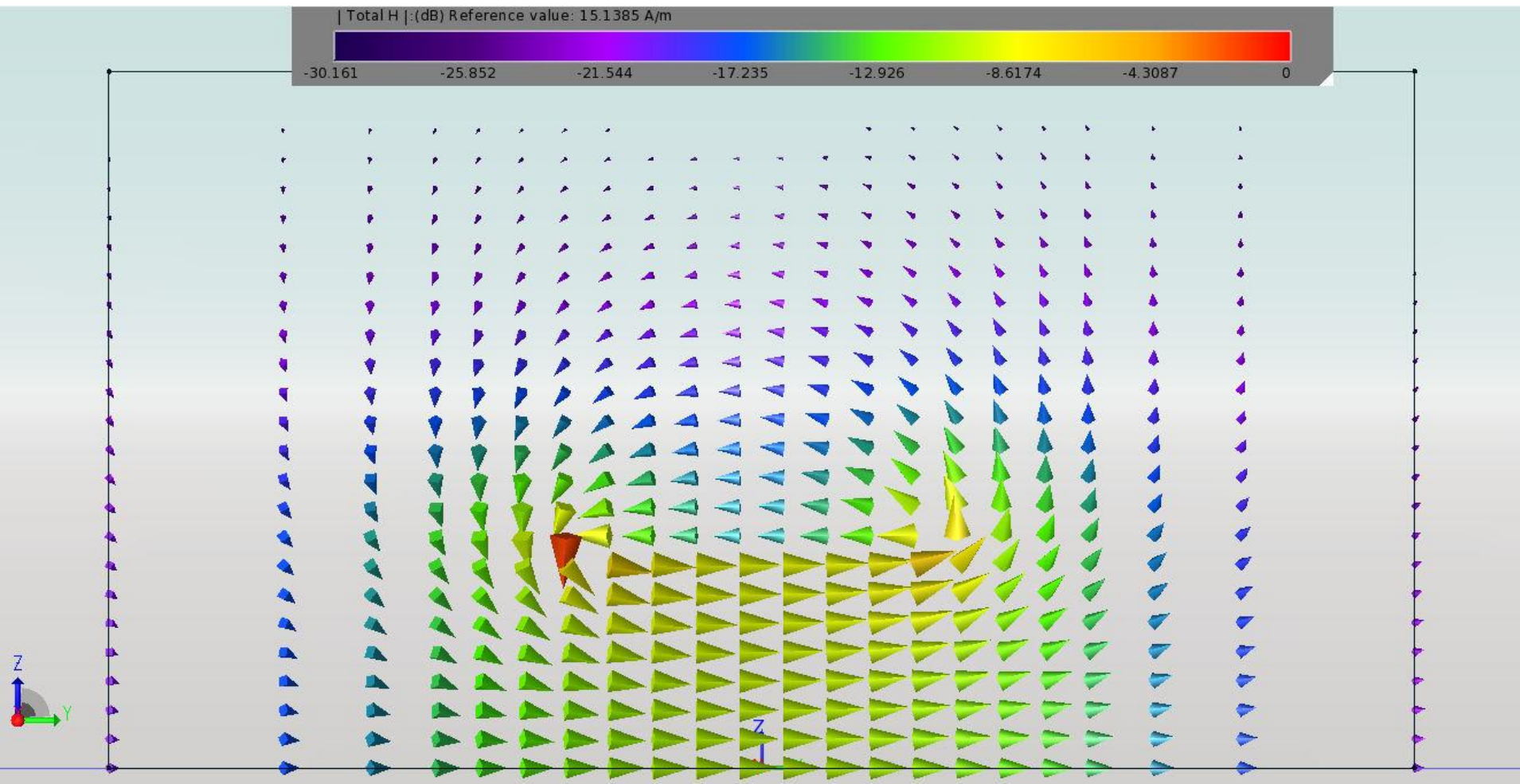


Figure 3.25b
© John Wiley & Sons, Inc. All rights reserved.

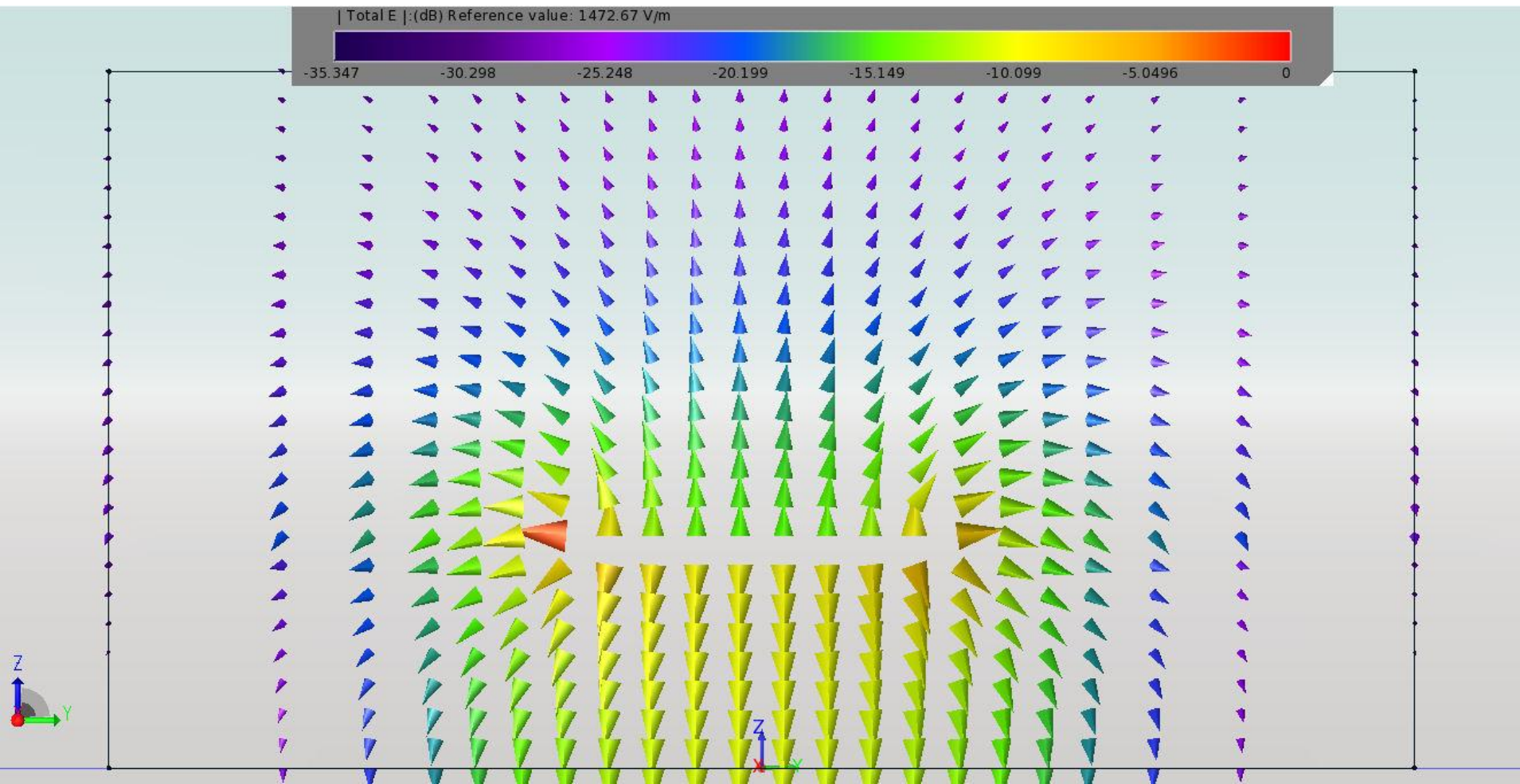
Implementation in microstrip technology

- quasi TEM line, EmPro



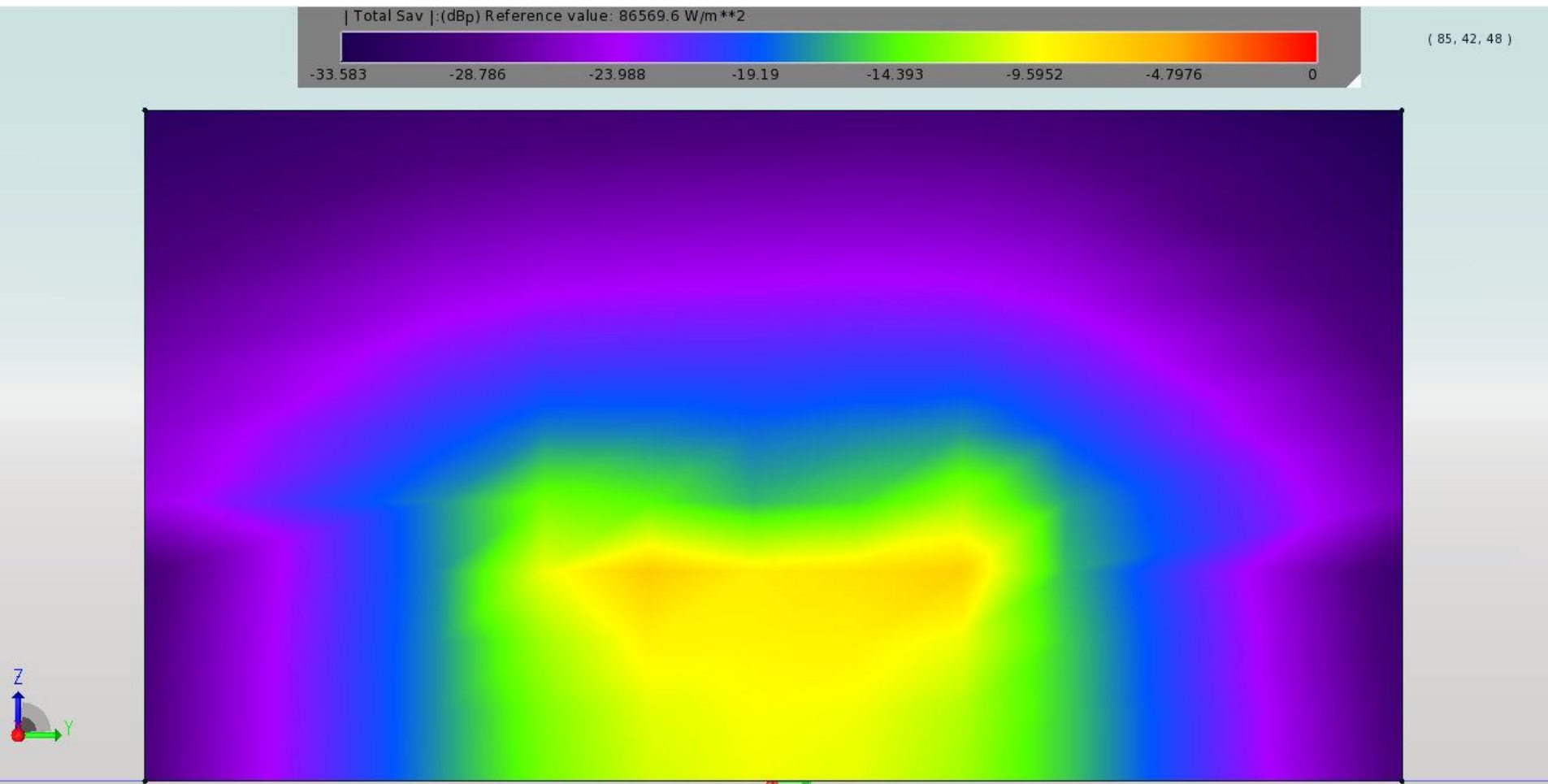
Implementation in microstrip technology

- quasi TEM line, EmPro



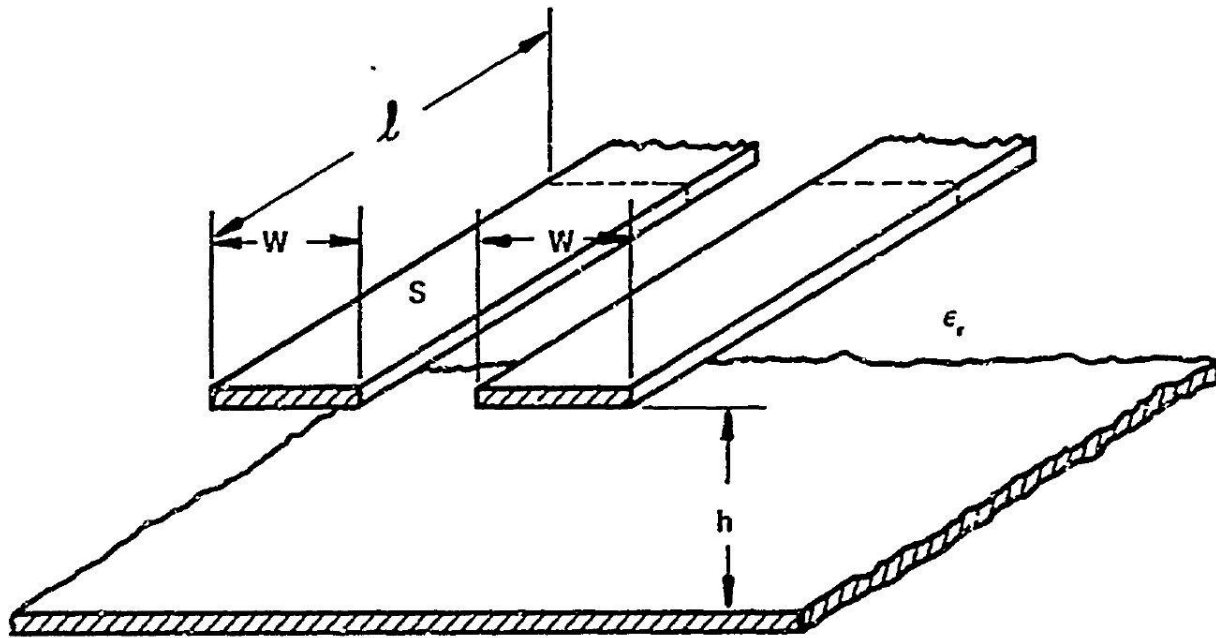
Implementation in microstrip technology

- quasi TEM line, EmPro



Implementation in microstrip technology

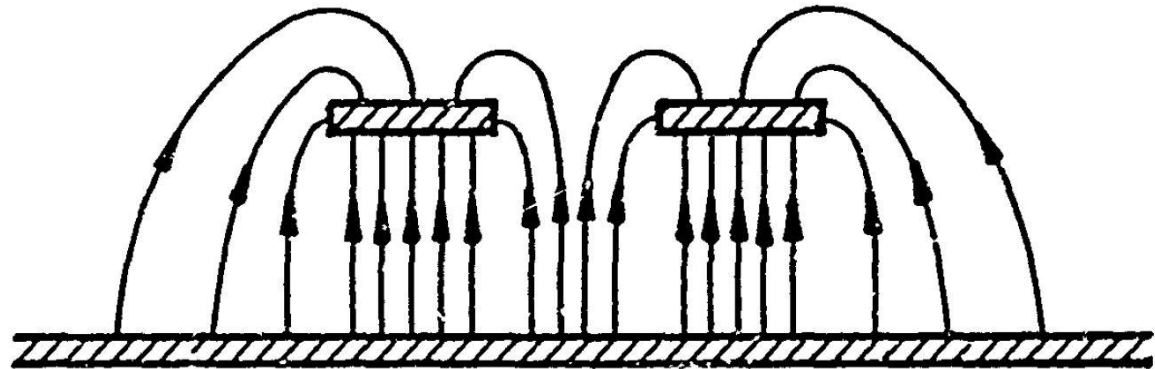
- ~ quasi TEM



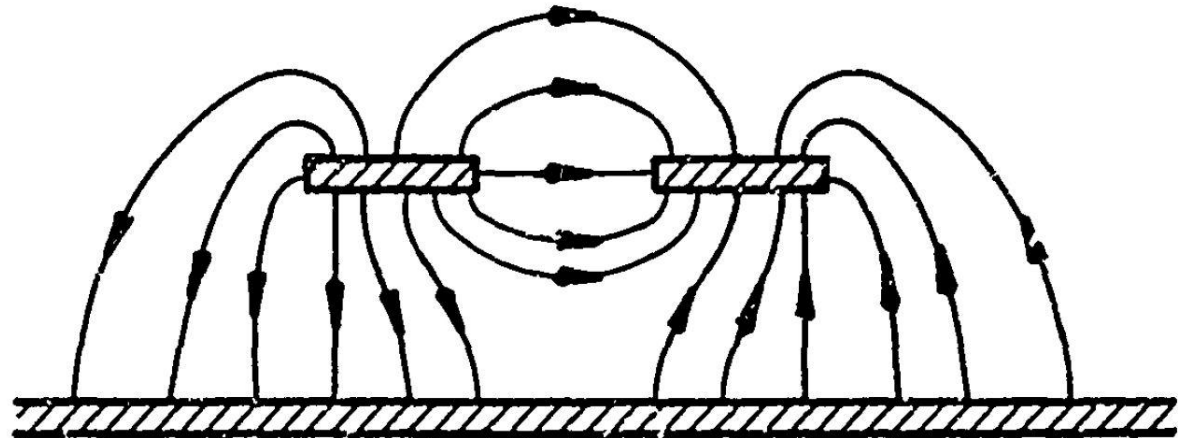
a) COUPLED STRIP GEOMETRY

Implementation in microstrip technology

- ~ quasi TEM



b) EVEN MODE ELECTRIC FIELD PATTERN (SCHEMATIC)



c) ODD MODE ELECTRIC FIELD PATTERN (SCHEMATIC)

Implementation in microstrip technology

- Equivalent geometry of a quasi-TEM microstrip line with effective dielectric constant homogeneous medium

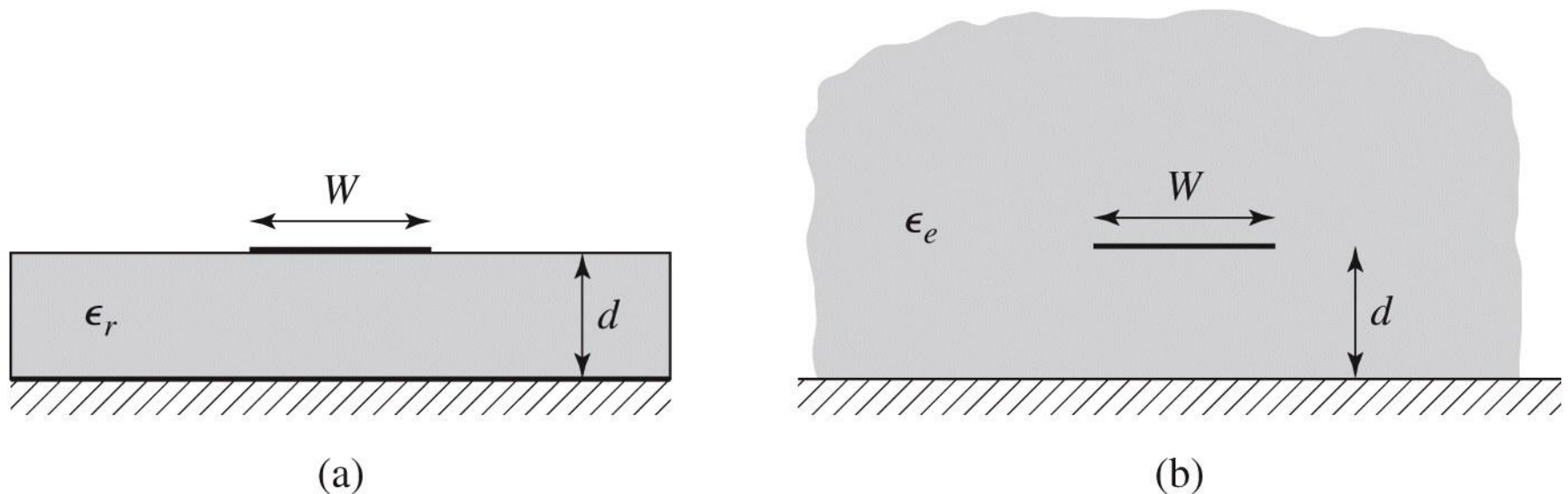


Figure 3.26
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Design

■ Empirical formulas

$$v_p = \frac{c}{\sqrt{\epsilon_e}},$$

$$\beta = k_0 \sqrt{\epsilon_e},$$

$$\epsilon_e = \frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{2} \frac{1}{\sqrt{1 + 12d/W}}.$$

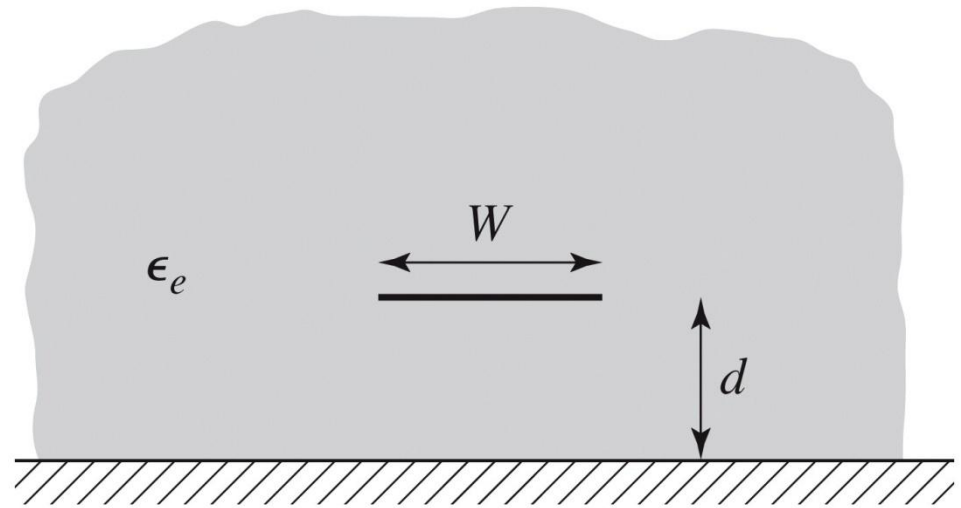


Figure 3.26b
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$$Z_0 = \begin{cases} \frac{60}{\sqrt{\epsilon_e}} \ln \left(\frac{8d}{W} + \frac{W}{4d} \right) & \text{for } W/d \leq 1 \\ \frac{120\pi}{\sqrt{\epsilon_e} [W/d + 1.393 + 0.667 \ln (W/d + 1.444)]} & \text{for } W/d \geq 1. \end{cases}$$

Design

■ Empirical formulas

$$A = \frac{Z_0}{60} \sqrt{\frac{\epsilon_r + 1}{2}} + \frac{\epsilon_r - 1}{\epsilon_r + 1} \left(0.23 + \frac{0.11}{\epsilon_r} \right)$$

$$B = \frac{377\pi}{2Z_0\sqrt{\epsilon_r}}$$

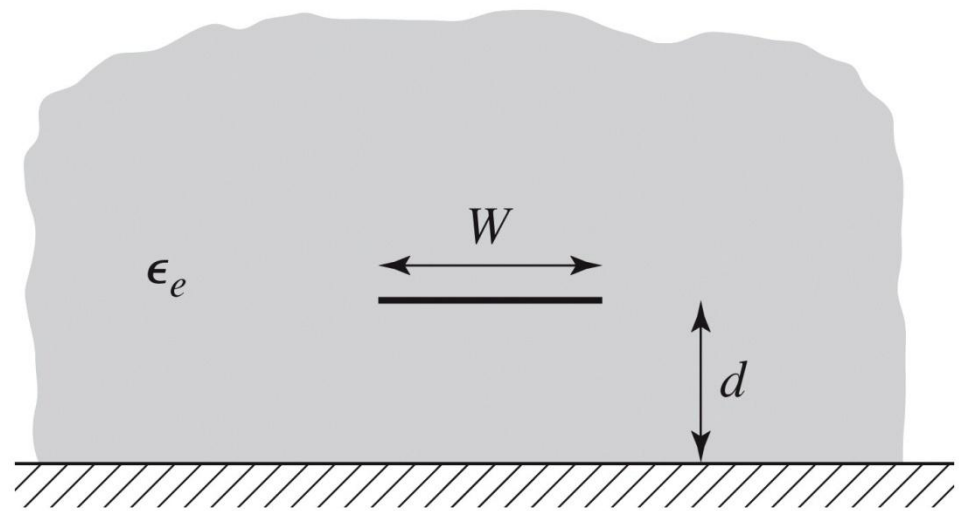
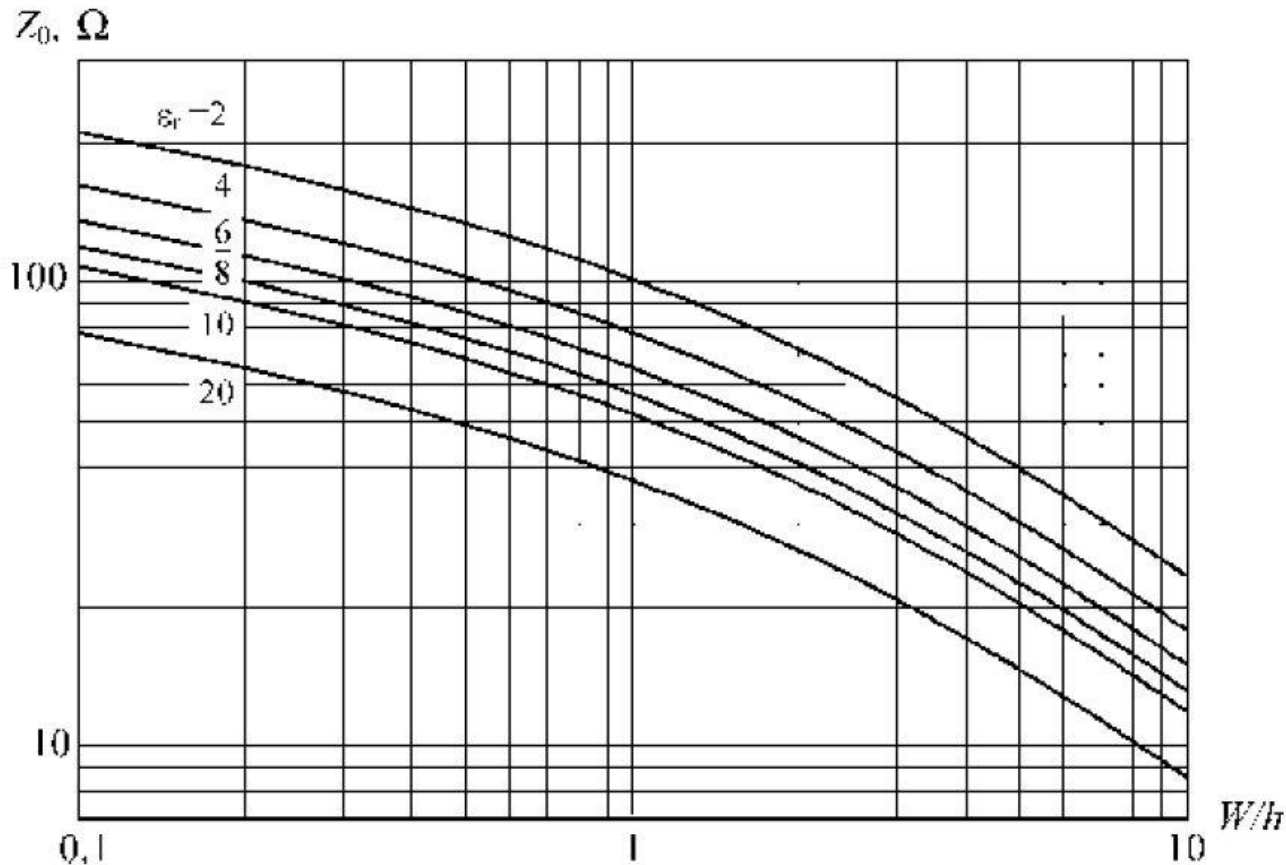


Figure 3.26b
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$$\frac{W}{d} = \begin{cases} \frac{8e^A}{e^{2A} - 2} & \text{for } W/d < 2 \\ \frac{2}{\pi} \left[B - 1 - \ln(2B - 1) + \frac{\epsilon_r - 1}{2\epsilon_r} \left\{ \ln(B - 1) + 0.39 - \frac{0.61}{\epsilon_r} \right\} \right] & \text{for } W/d > 2, \end{cases}$$

Characteristic impedance

- **Large impedances** require **narrow traces**
- **Small impedances** require **wide traces**



$$k_0 = \frac{2\pi f}{c}$$
$$\beta \ell = \sqrt{\epsilon_e} k_0 \ell,$$

Microstrip standardization

- Standardization
 - dimensions in **mil**
 - 1 mil = 10^{-3} inch
 - 1 inch = 2.54 cm
- Trace thickness
 - based on the weight of the deposited copper
 - oz/ft²
 - 1oz=28.35g and 1ft=30.48cm

Weight of the deposited copper		Trace thickness	
oz/ft ²	g/ft ²	inch	mm
0.5	14.175	0.0007	0.0178
1.0	28.35	0.0014	0.0356
2.0	56.7	0.0028	0.0712

Microstrip standardization

- Typically the height of the dielectric layers is also standardized in mil

Standard Thickness
RO4003C: 0.008" (0.203mm), 0.012 (0.305mm), 0.016" (0.406mm), 0.020" (0.508mm) 0.032" (0.813mm), 0.060" (1.524mm) RO4350B: *0.004" (0.101mm), 0.0066" (0.168mm) 0.010" (0.254mm), 0.0133 (0.338mm), 0.0166 (0.422mm), 0.020" (0.508mm) 0.030" (0.762mm), 0.060" (1.524mm)

ADS linecalc

- In schematics: >Tools>LineCalc>Start
- for Microstrip lines >Tools>LineCalc>Send to Linecalc

The screenshot shows the ADS LineCalc/untitled dialog box. The 'Component' section has 'Type' set to 'MLIN' and 'ID' set to 'MLIN: TL25'. The 'Substrate Parameters' section has 'ID' set to 'Alumina' and a table of properties: H (15.000 mil), Er (9.600 N/A), Mur (1.000 N/A), Cond (5.96E+7 N/A), Hu (3.9e+034 mil), T (1.400 mil), and TanD (1.000e-4 N/A). The 'Physical' section has 'W' (13.660 mil) and 'L' (386.030 mil). The 'Electrical' section has 'Z0' (50.098900 Ohm) and 'E_Eff' (294.984000 deg). The 'Calculated Results' section shows 'K_Eff = 6.276', 'A_DB = 0.060', and 'SkinDepth = 0.025'. A diagram of a microstrip line is shown on the right. The status bar at the bottom indicates 'Values are consistent'.

LineCalc/untitled

File Simulation Options Help

Component
Type MLIN ID MLIN: TL25

Substrate Parameters
ID Alumina

Property	Value	Unit
H	15.000	mil
Er	9.600	N/A
Mur	1.000	N/A
Cond	5.96E+7	N/A
Hu	3.9e+034	mil
T	1.400	mil
TanD	1.000e-4	N/A

Physical
W 13.660 mil
L 386.030 mil

Synthesize Analyze

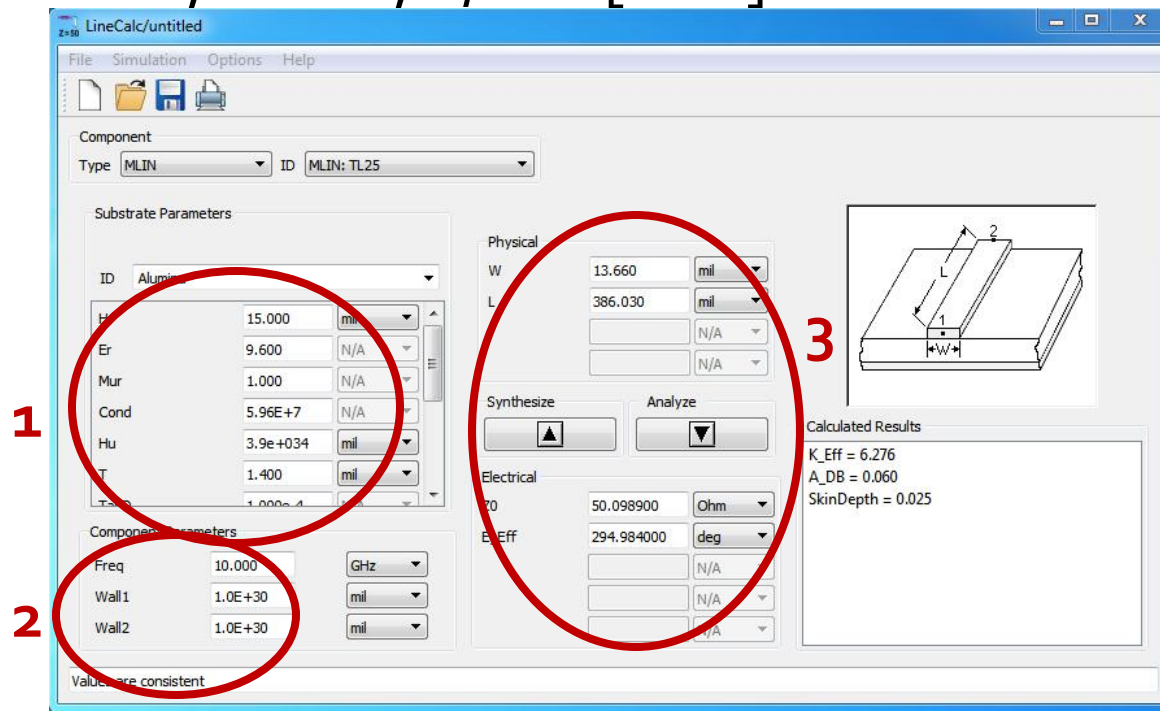
Electrical
Z0 50.098900 Ohm
E_Eff 294.984000 deg

Calculated Results
K_Eff = 6.276
A_DB = 0.060
SkinDepth = 0.025

Values are consistent

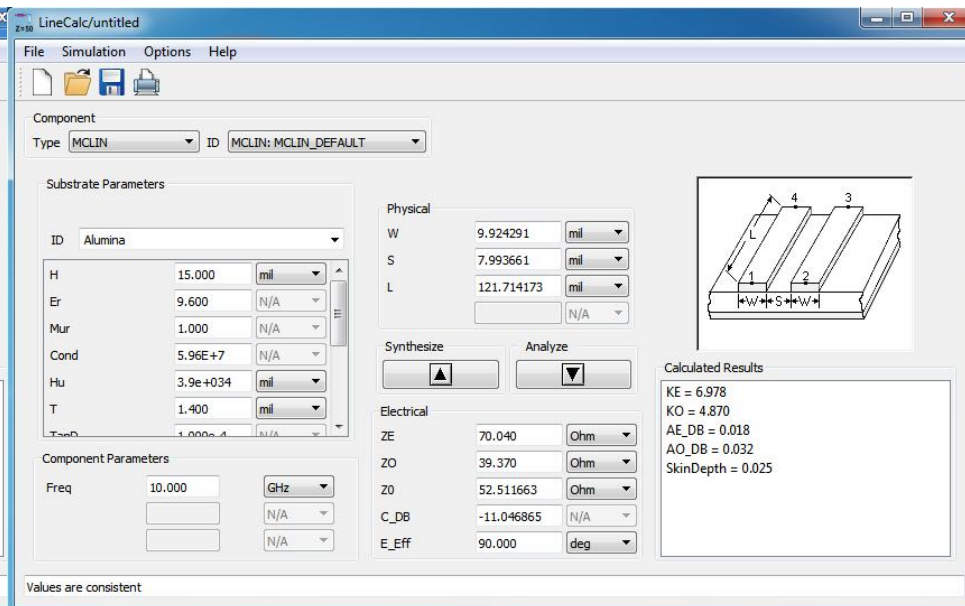
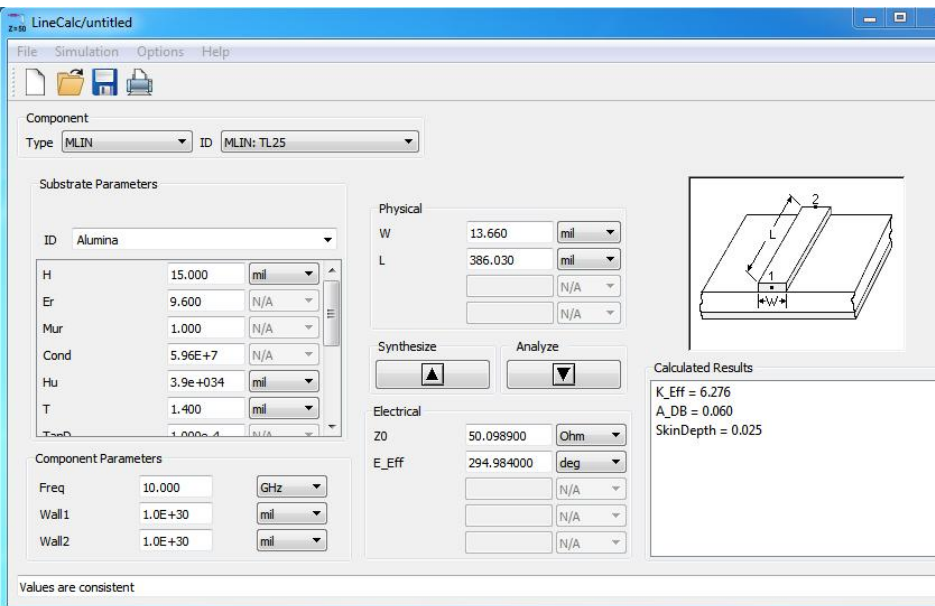
ADS linecalc

- 1. Define substrate (receive from schematic)
- 2. Insert frequency
- 3. Insert input data
 - Analyze: $W, L \rightarrow Z_o, E$ or Z_e, Z_o, E / at f [GHz]
 - Synthesis: $Z_o, E \rightarrow W, L$ / at f [GHz]



ADS linecalc

- Can be used for:
 - microstrip lines MLIN: $W, L \Leftrightarrow Z_0, E$
 - microstrip coupled lines MCLIN: $W, L, S \Leftrightarrow Z_e, Z_0, E$



ADS linecalc

LineCalc/untitled

File Simulation Options Help

Component
Type: MCLIN ID: MCLIN: MCLIN_DEFAULT

Substrate Parameters

ID	Alumina
H	15.000 mil
Er	9.600 N/A
Mur	1.000 N/A
Cond	5.96E+7 N/A
Hu	3.9e+034 mil
T	1.400 mil
TanD	1.000e-4 N/A

Component Parameters

Freq	10.000 GHz
	N/A
	N/A

Physical

W	9.924291 mil
S	7.993661 mil
L	121.714173 mil
	N/A

Synthesize Analyze

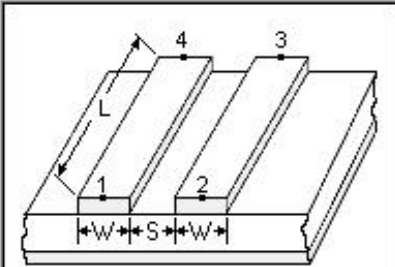
Electrical

ZE	70.040 Ohm
ZO	39.370 Ohm
Z0	52.511663 Ohm
C_DB	-11.046865 N/A
E_Eff	90.000 deg

Calculated Results

KE = 6.978
KO = 4.870
AE_DB = 0.018
AO_DB = 0.032
SkinDepth = 0.025

Values are consistent

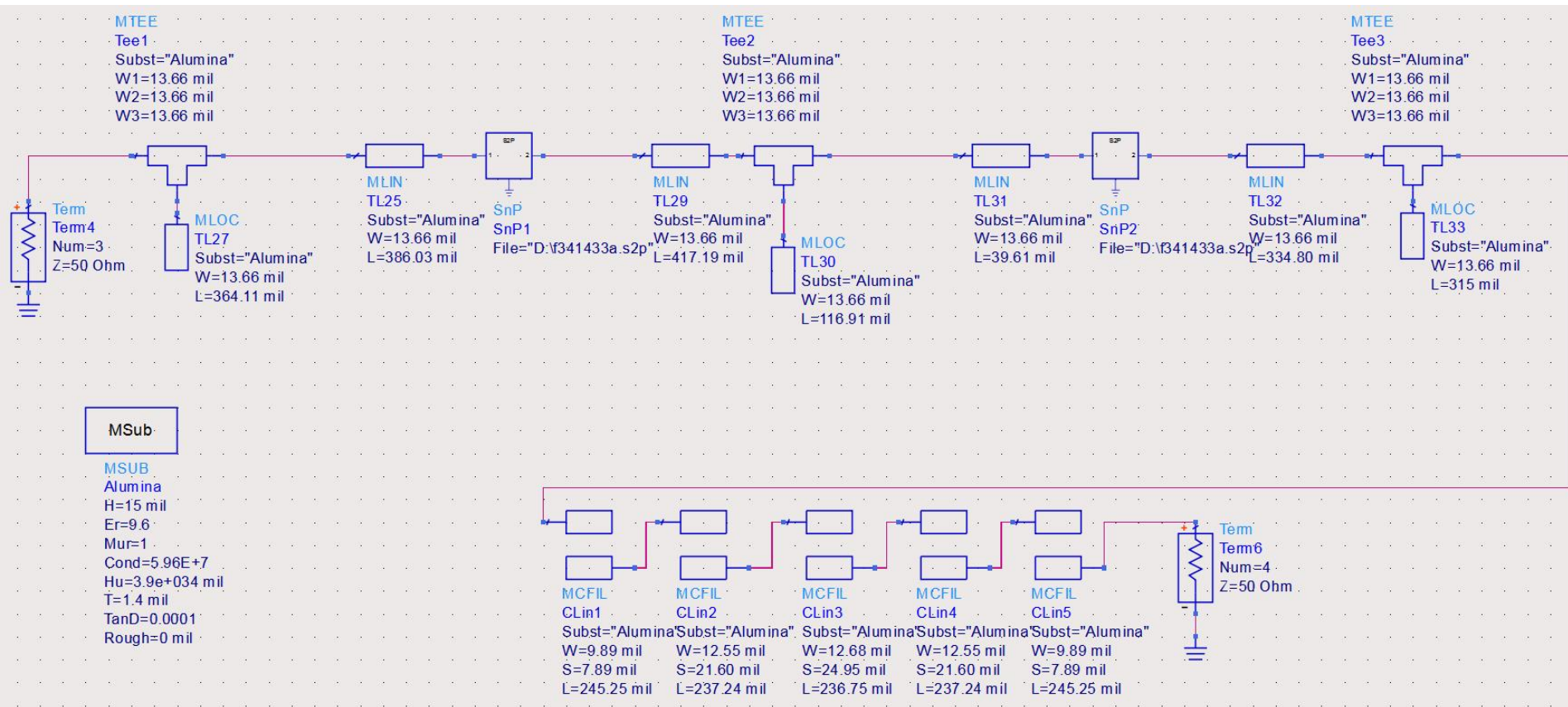


The diagram illustrates a microstrip line on a substrate. It shows a series of three rectangular strips. The width of each strip is labeled 'W', and the spacing between them is labeled 'S'. The total length of the structure is labeled 'L'. Four numbered points are marked: 1 is at the start of the first strip, 2 is at the start of the second strip, 3 is at the end of the third strip, and 4 is at the end of the fourth strip.

Transmission lines

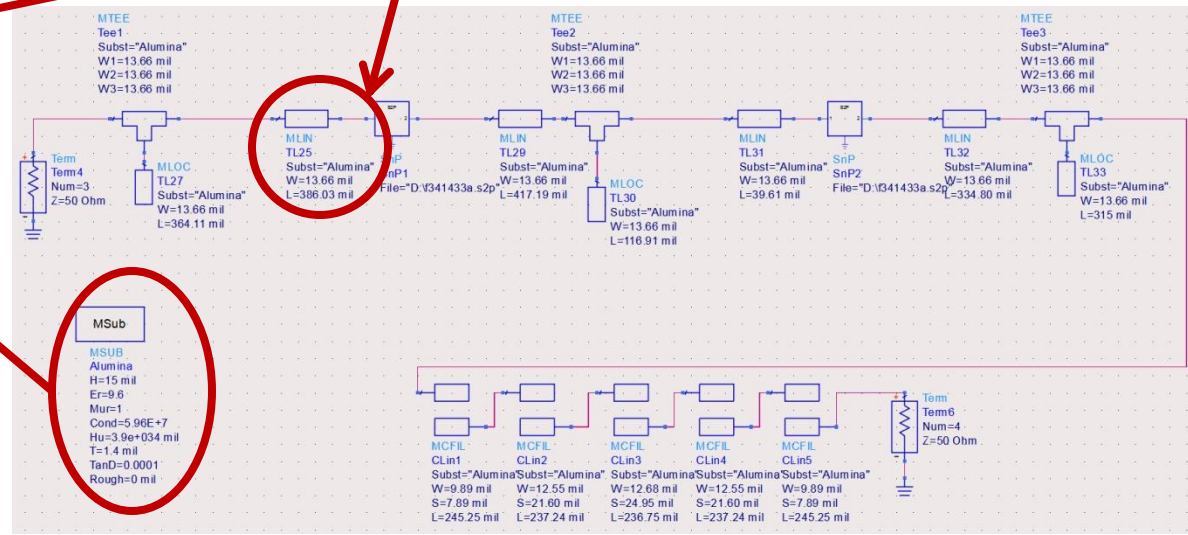
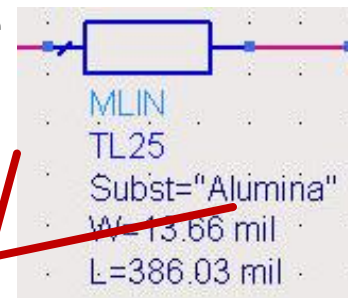
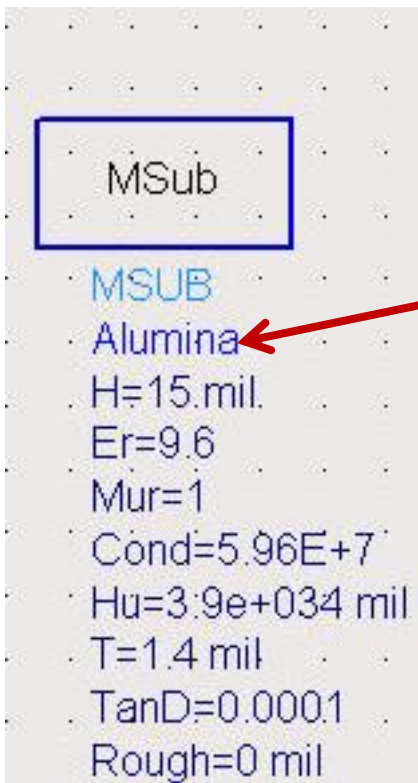
- <http://rf-opto.etti.tuiasi.ro>
- Transmission lines / Rogers
 - more precise formulas including
 - t , trace thickness
 - f , frequency
 - formulas for
 - microstrip
 - strip
 - coupled lines

Implementation in microstrip technology



Implementation in microstrip technology

- On all schematics you must have an substrate model/component
- Microstrip lines and coupled lines are computed in Linecalc for the same substrate

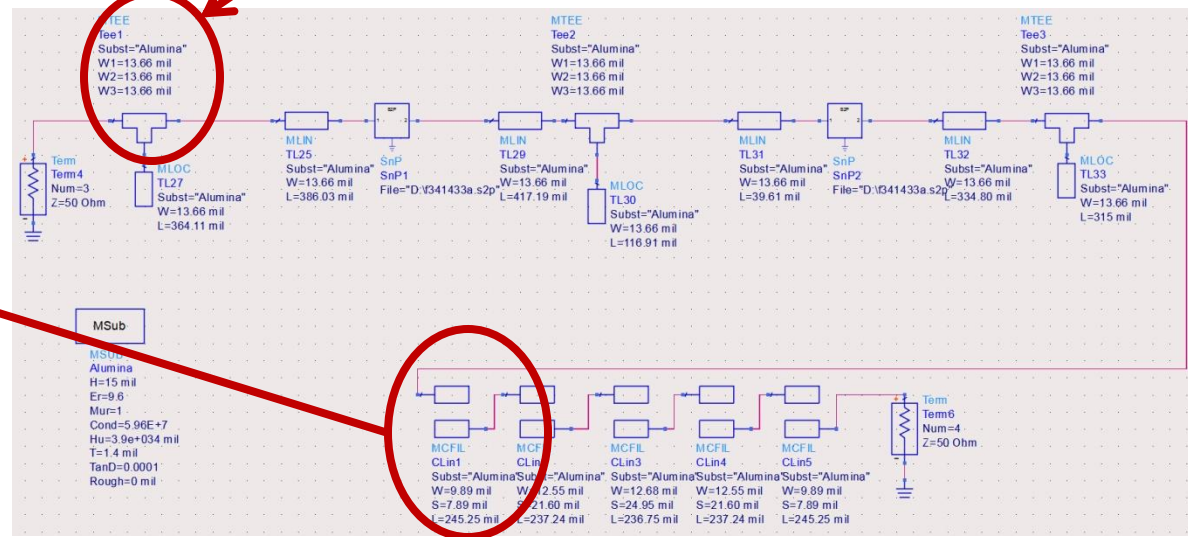
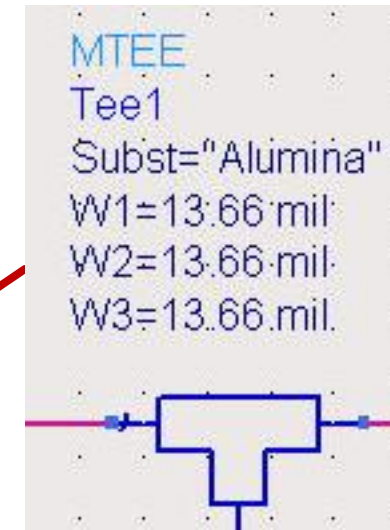


Implementation in microstrip technology

- We use components from the “Transmission Lines – Microstrip” palette
 - MSUB - substrate
 - MLIN – series line
 - MLOC – open-circuit shunt stub
 - MTEE – modeling of T junction (shunt stub connection to main line)
 - MCFIL – coupled line filter section (more accurate model than MCLIN – takes into account that two adjacent sections are physically close)

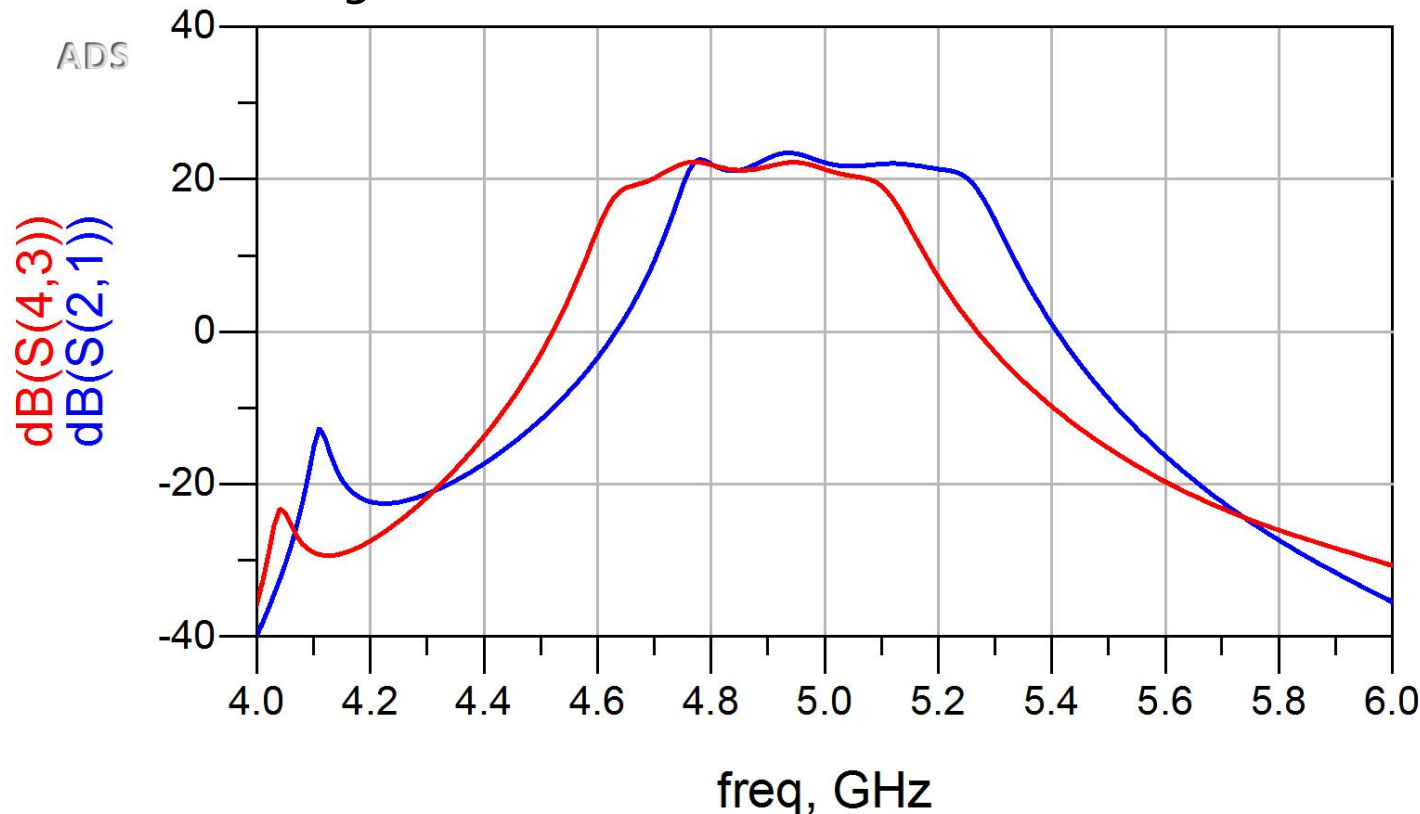
Implementation in microstrip technology

- Attention is required when inserting parameters for MTEE and MCFIL by checking in the schematic the width of the lines connected to each port.



Implementation in microstrip technology

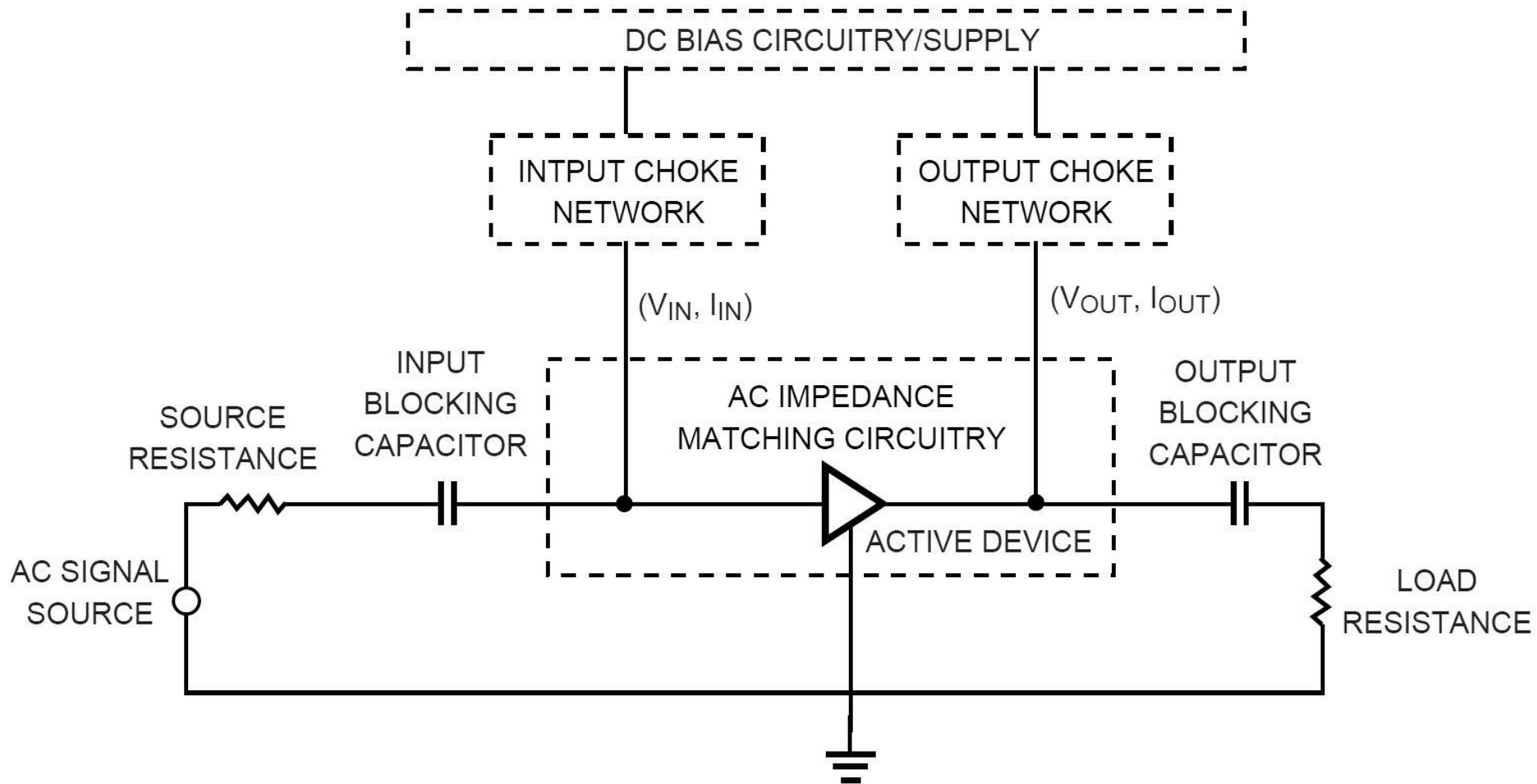
- Usually there is a shift of the transfer function (red) towards lower frequencies compared to the ideal model (blue)
 - due to the MCFIL/MCLIN difference
- Tune the length of filter elements to move the filter bandwidth around $f_0 = 5\text{GHz}$



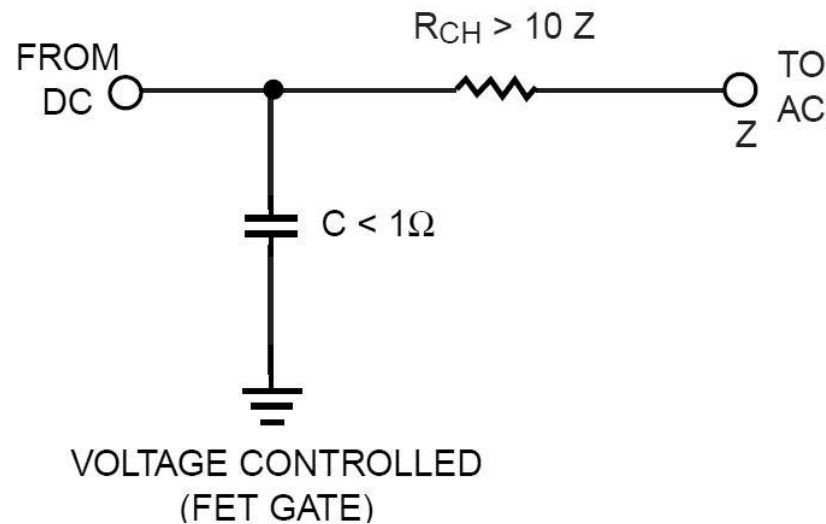
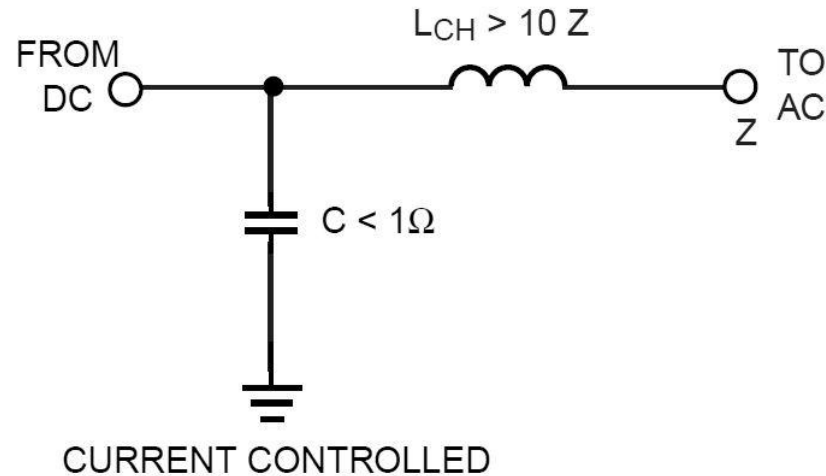
DC Bias

- <https://rf-opto.etti.tuiasi.ro>
- Agilent Application Notes
 - decoupling signal from DC Bias circuitry
 - DC Bias circuits for microwave transistors
- Appcad has tools for designing DC Bias circuits

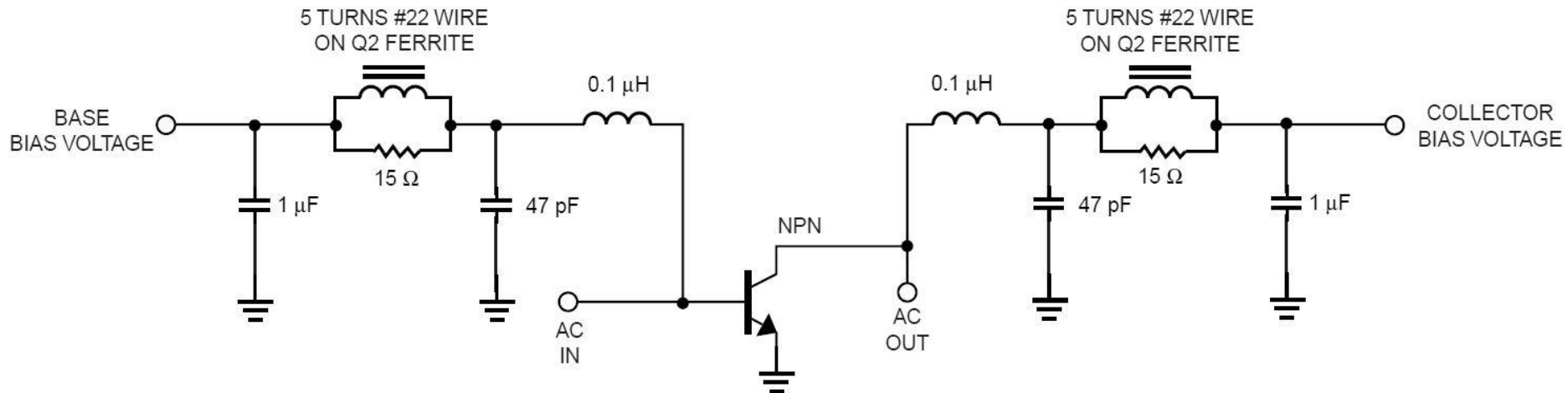
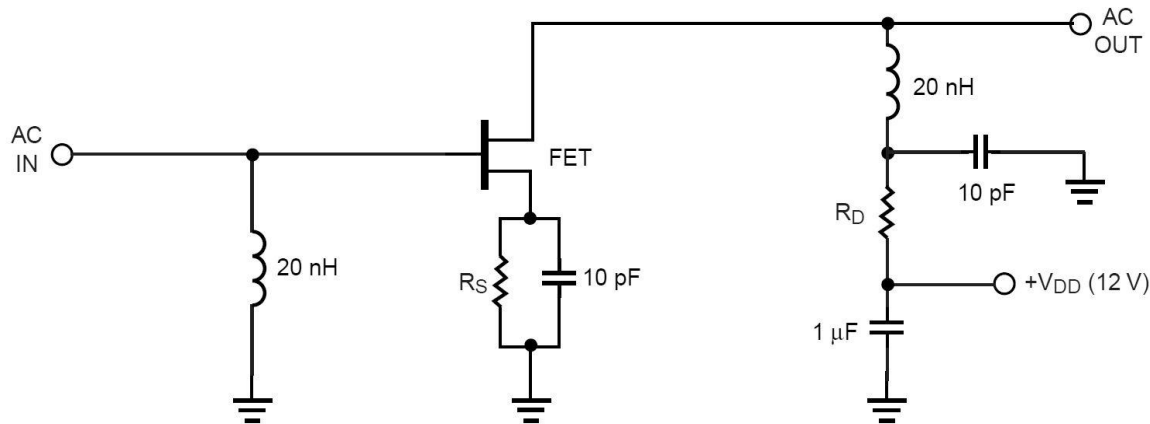
DC Bias



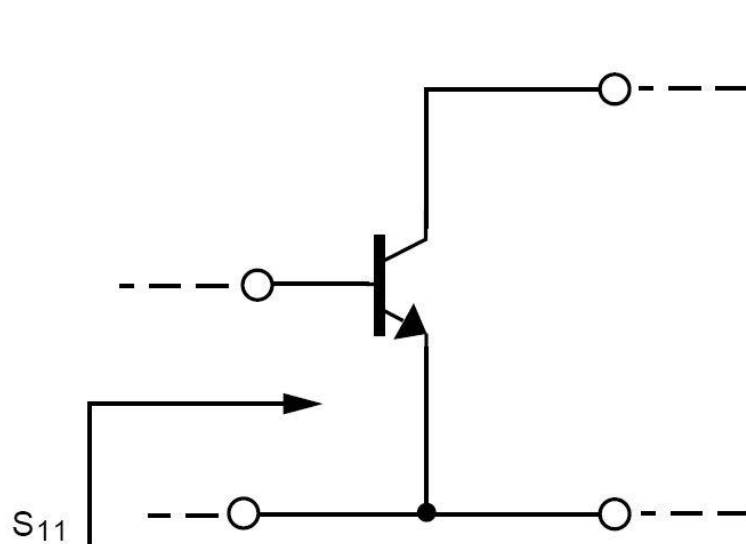
DC Bias, typical choke



DC Bias, typical schematics/values

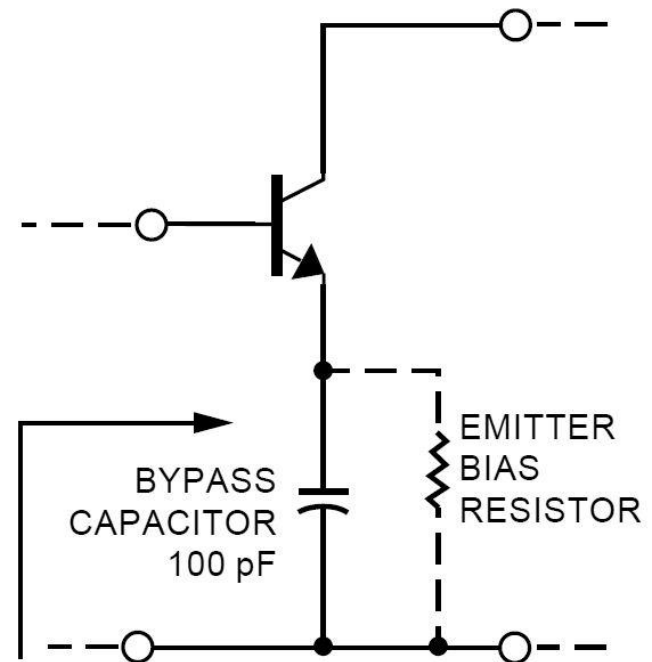


DC Bias, elements in E/S



$$S_{11} \text{ (AT 4 GHz)} = 0.52 \angle 154^\circ$$

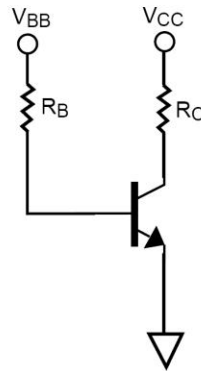
$$S_{11} \text{ (AT 0.1 GHz)} = 0.901 \angle -14.9^\circ$$



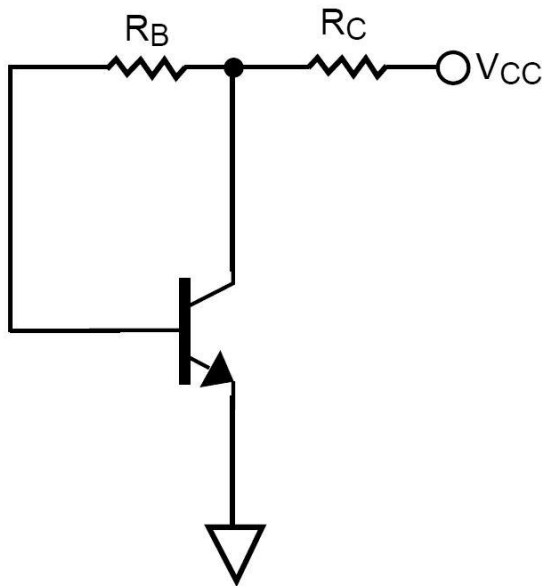
$$S'_{11} \text{ (AT 4 GHz)} = 0.52 \angle 154^\circ \text{ UNCHANGED AT 4 GHz}$$

$$S'_{11} \text{ (AT 0.1 GHz)} = 1.066 \angle -8.5^\circ \quad |S_{11}| > 1 \text{ AT 0.1 GHz}$$

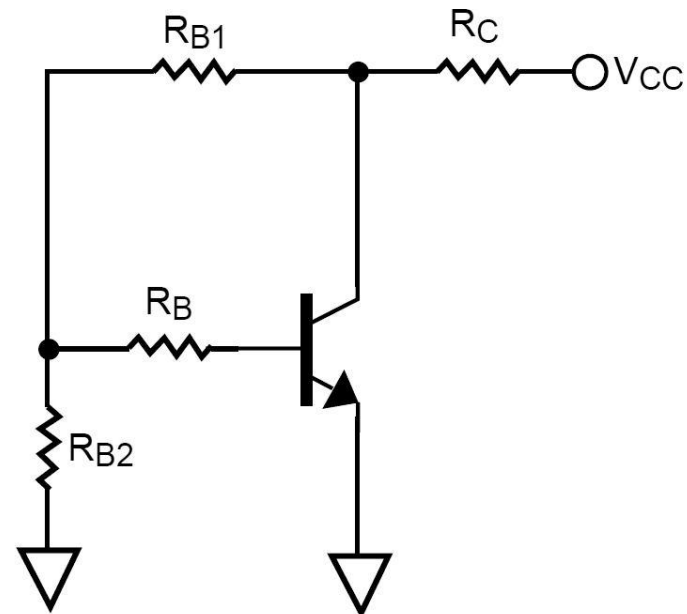
DC Bias, bipolar transistors



NON-STABILIZED



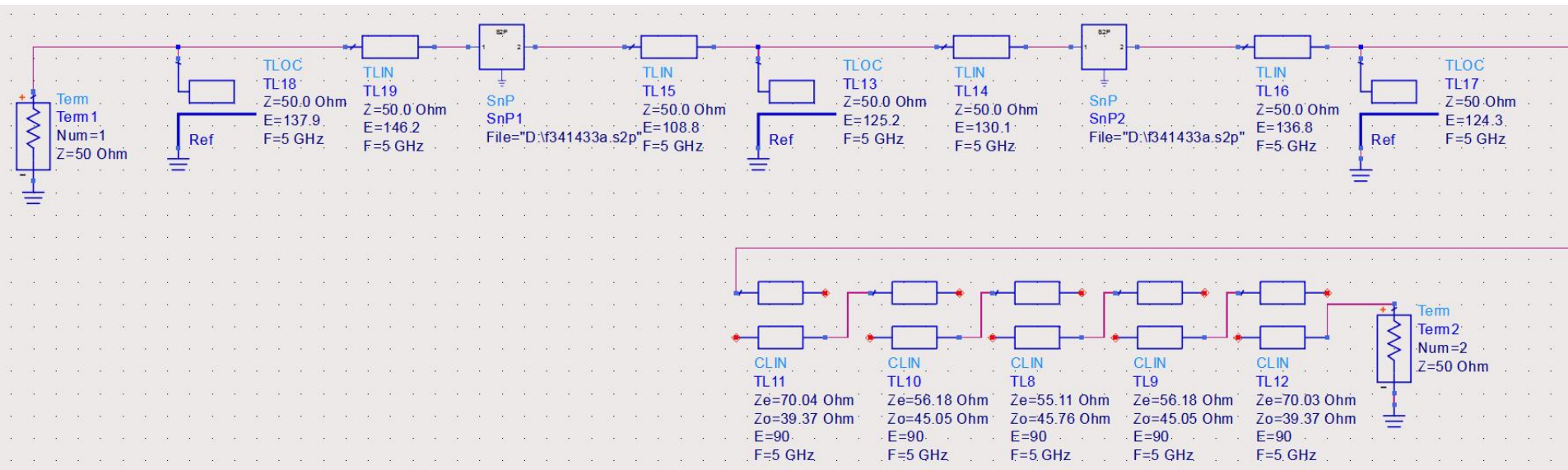
VOLTAGE FEEDBACK



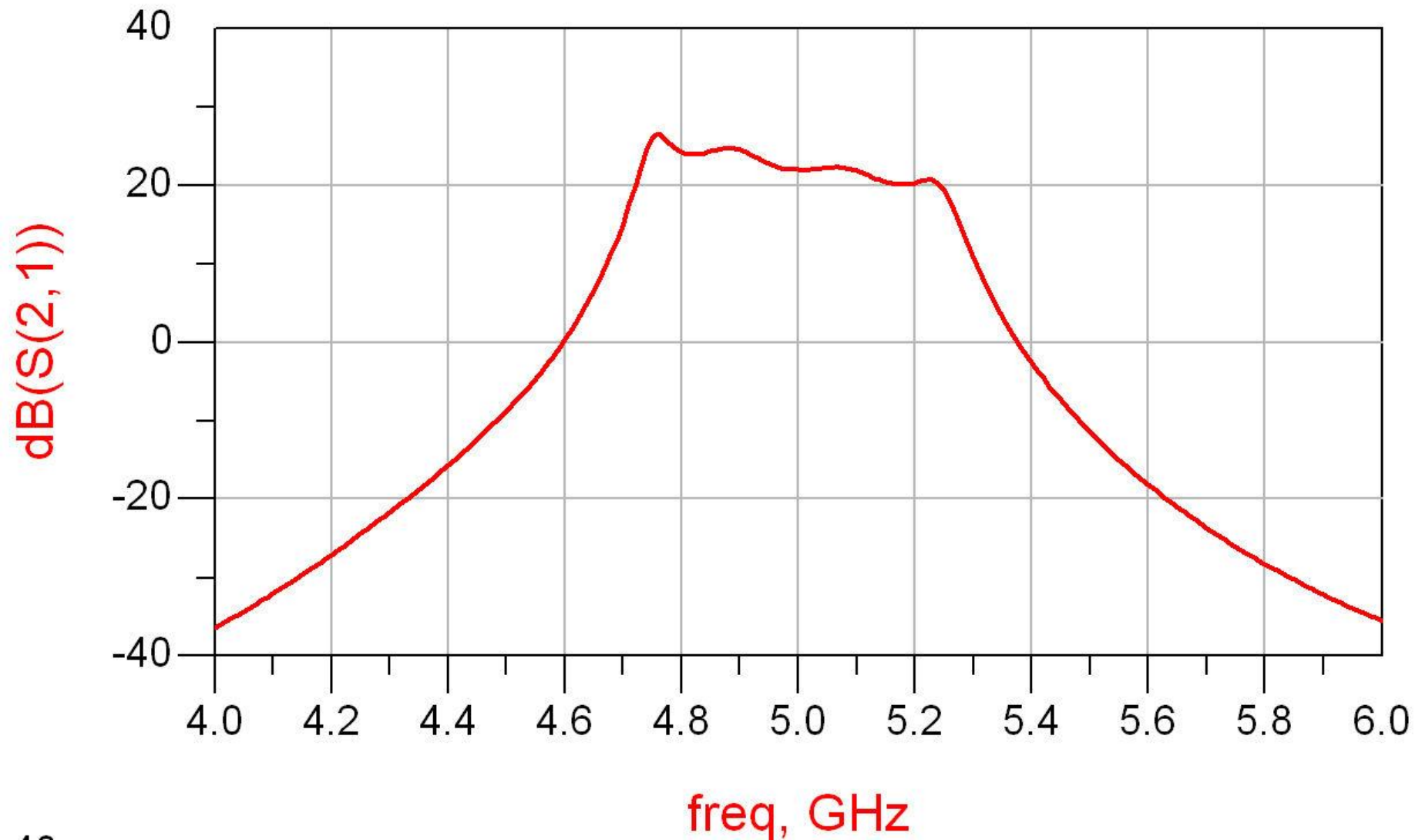
VOLTAGE FEEDBACK AND CONSTANT
BASE CURRENT SOURCE

Example project

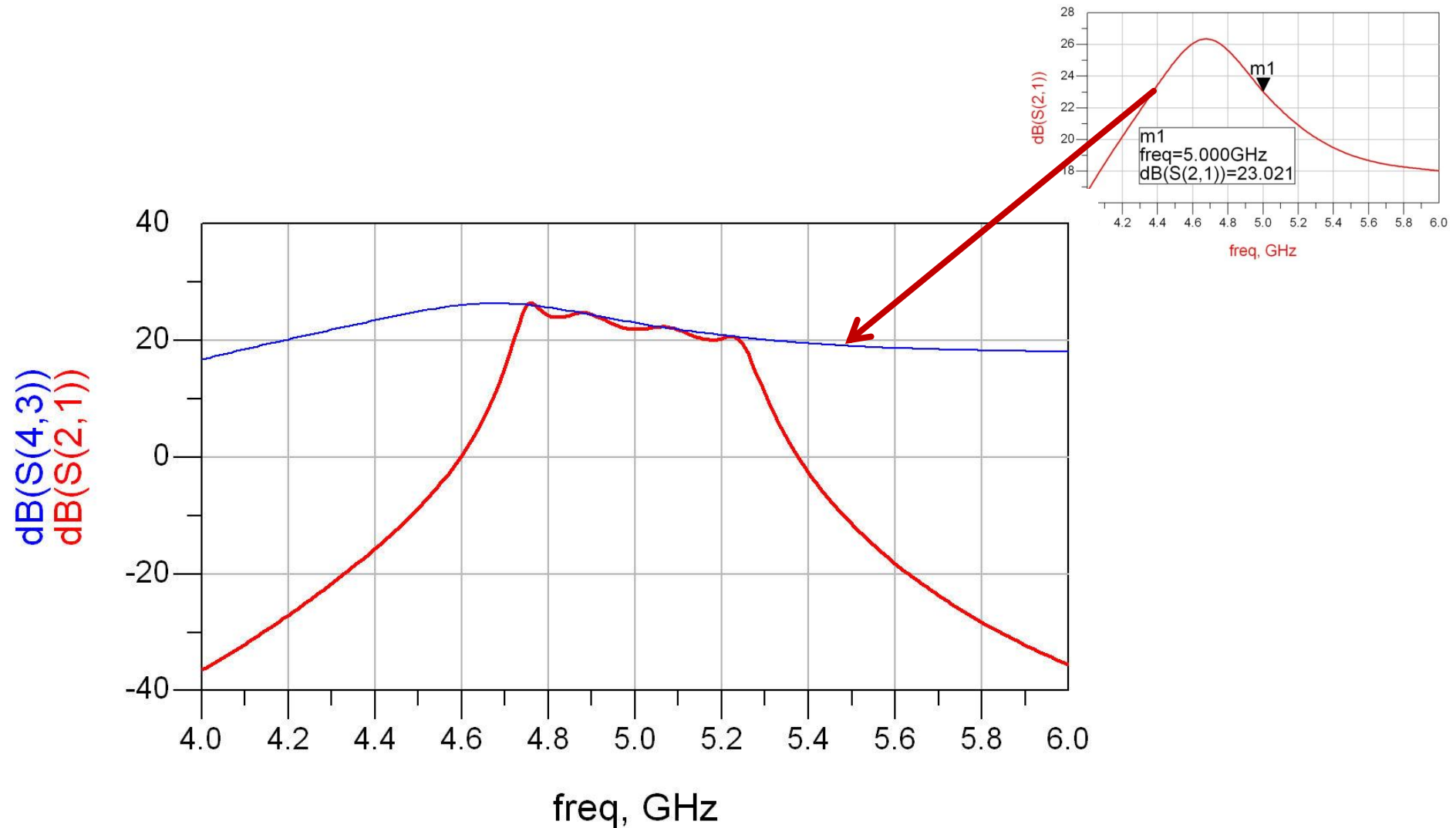
- Unify the two schematics
 - L10 – amplifier
 - L12 – filter



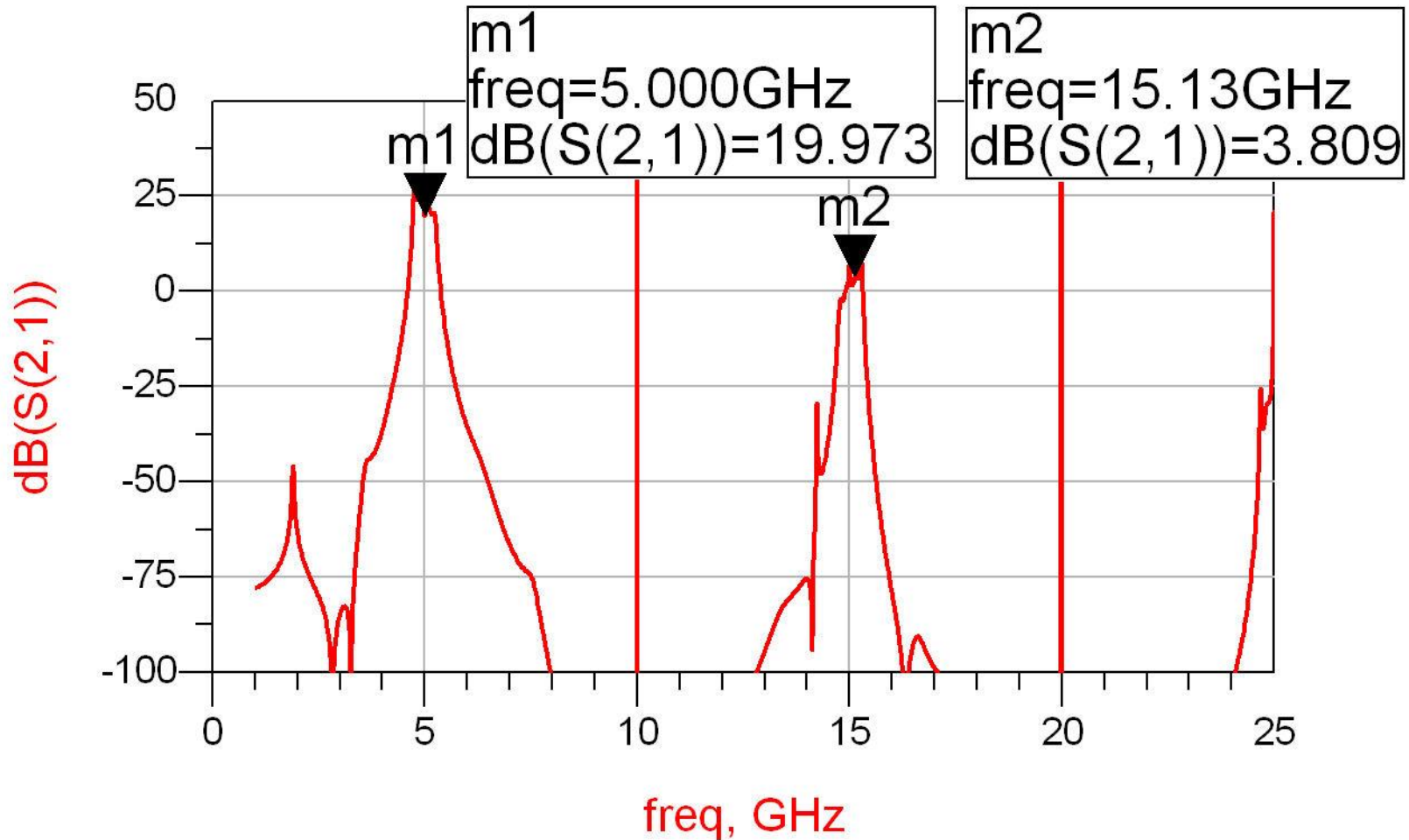
Result (unbalanced)



Result (unbalanced)

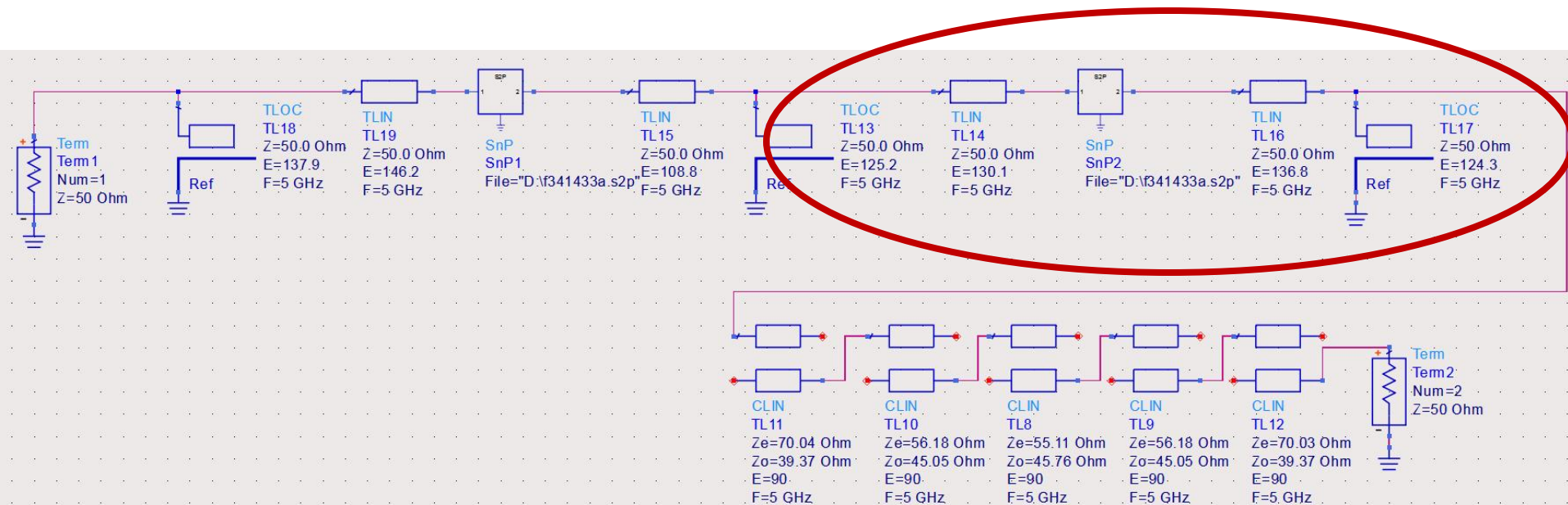


Result (~periodic in frequency)

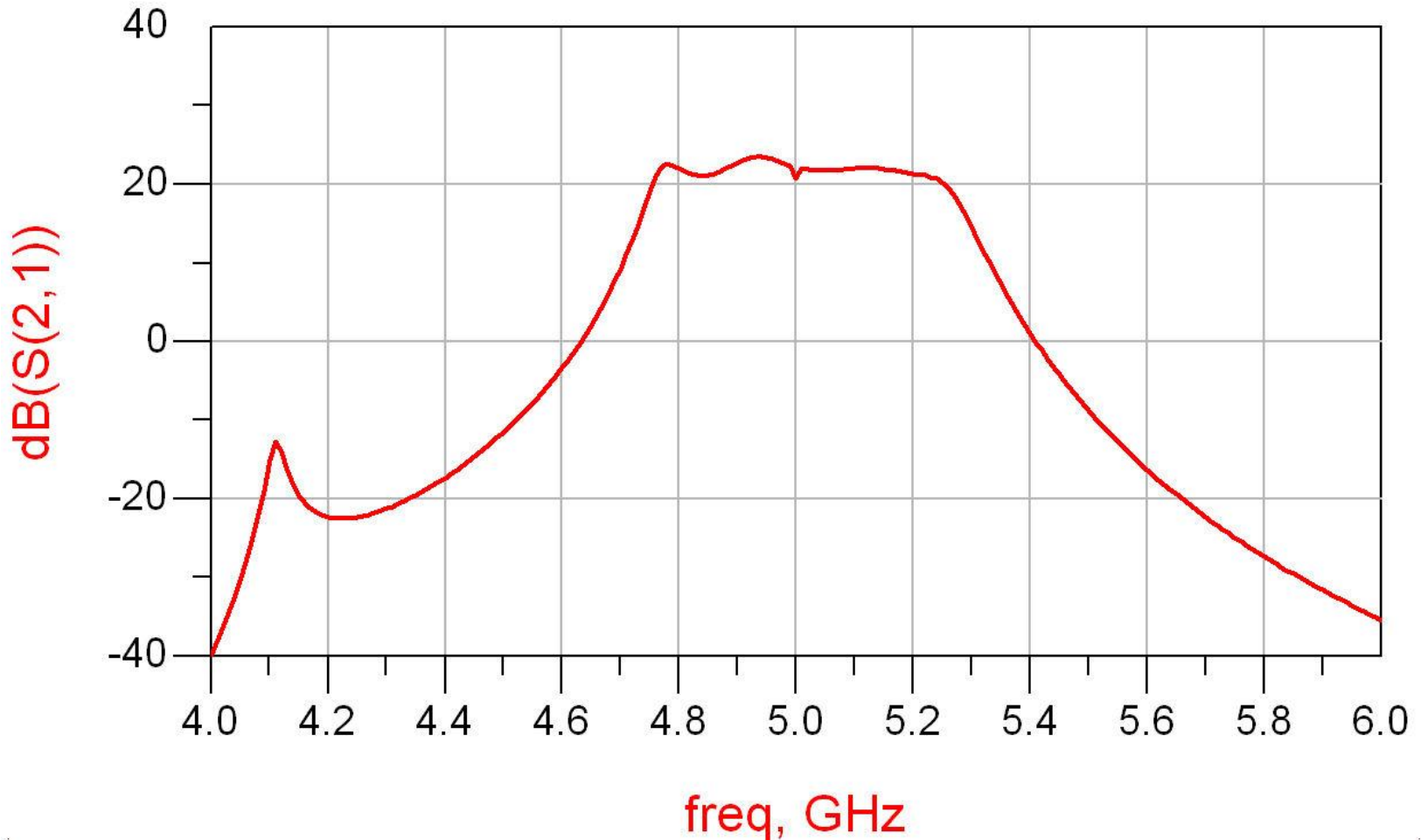


Tune -> balance

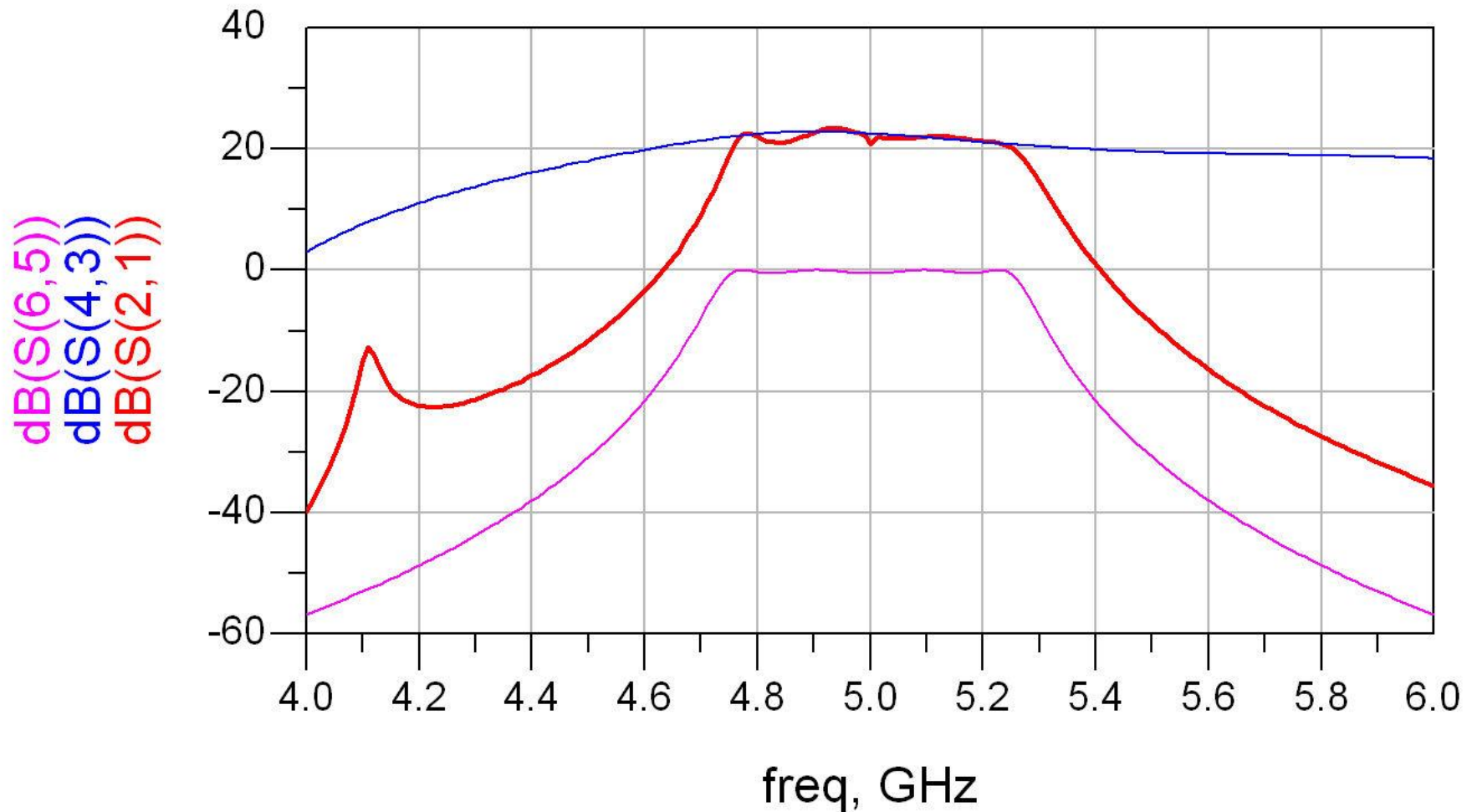
- purpose: balance the gain characteristic of the amplifier (maximum at design frequency)
 - favor tuning lines at the end of the amplifier
 - eliminate/minimize effect of the tune on noise



Tune -> balance, result

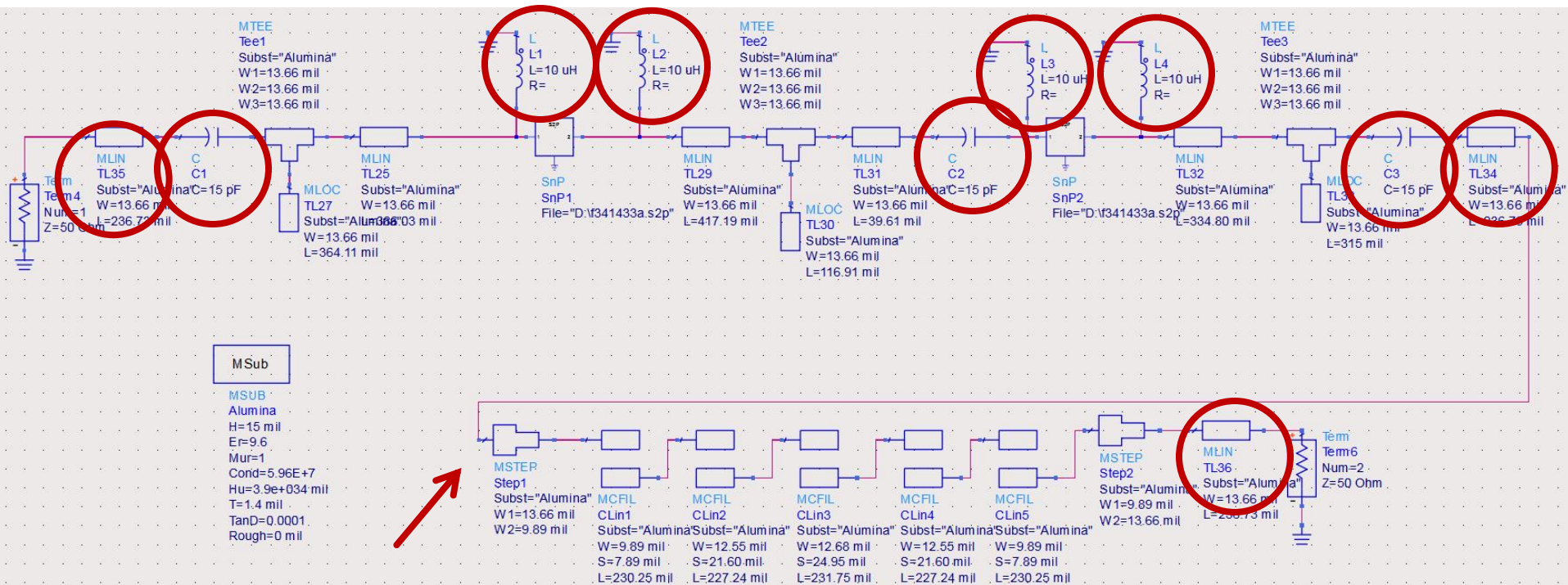


Amplifier, Filter, Total

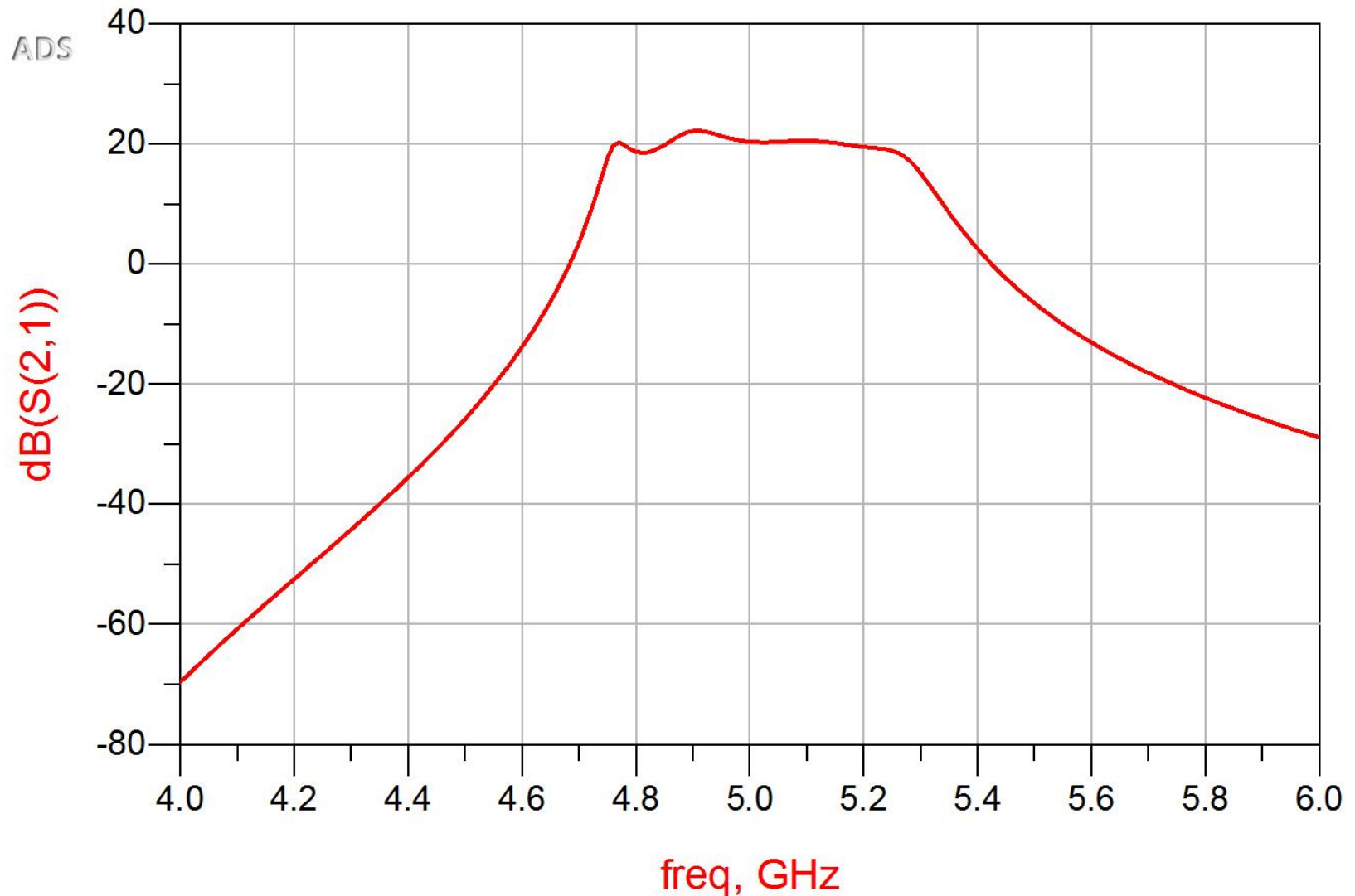


DC Bias elements in ADS schematic

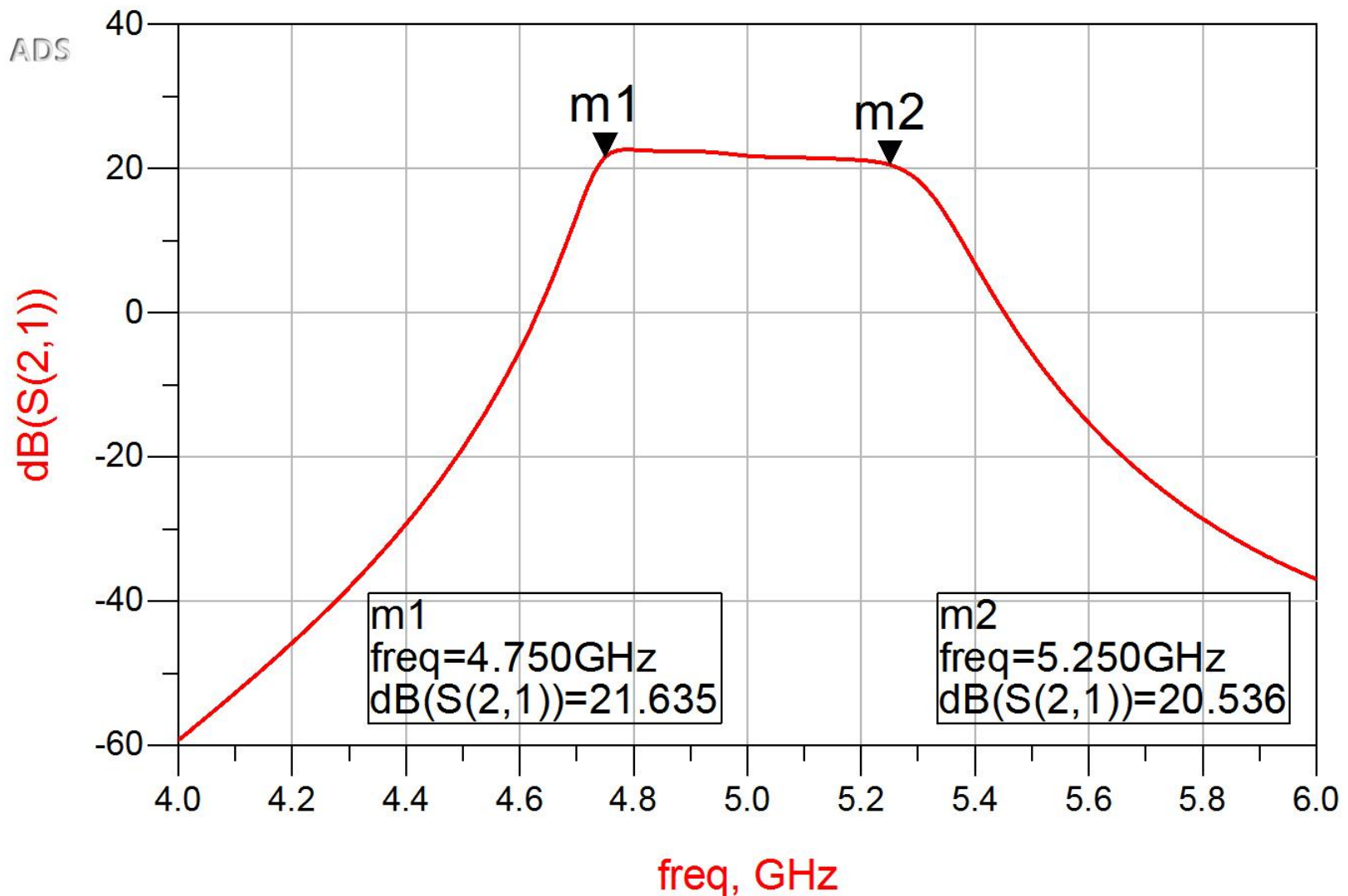
- Insert L (RF chokes) and C (decoupling)
- additional 50Ω connection lines
 - source
 - load
 - between blocks



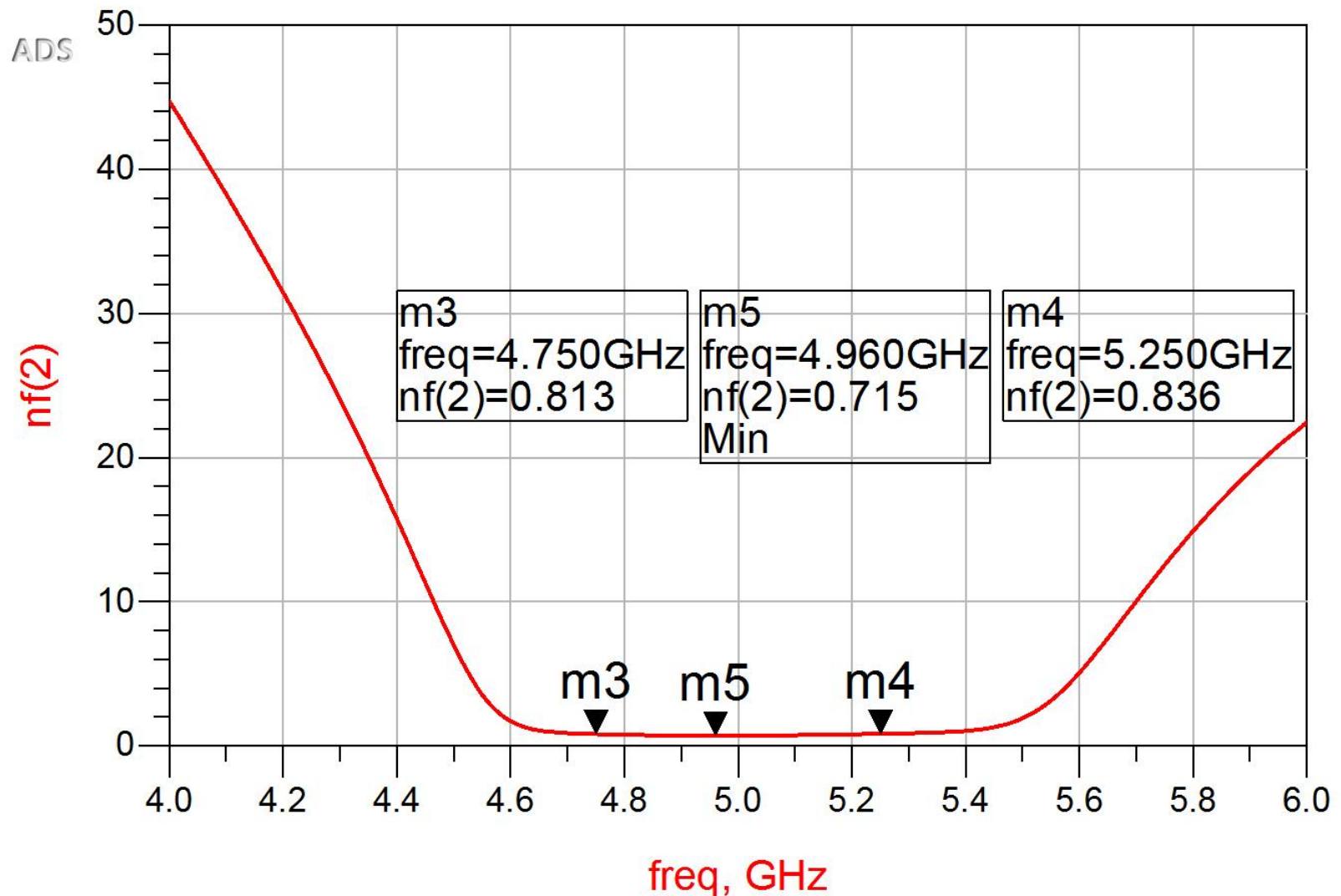
Gain -> Tune/Optimization



Final result (Gain)

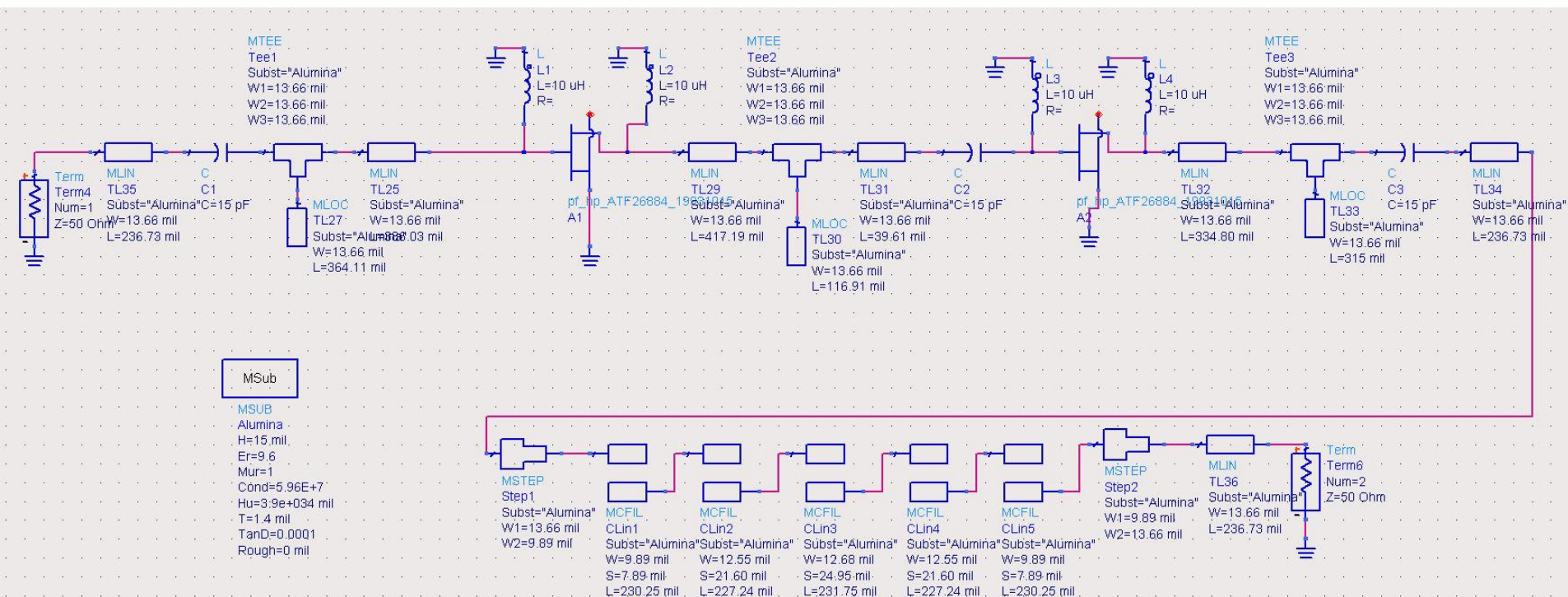


Final result (Noise)

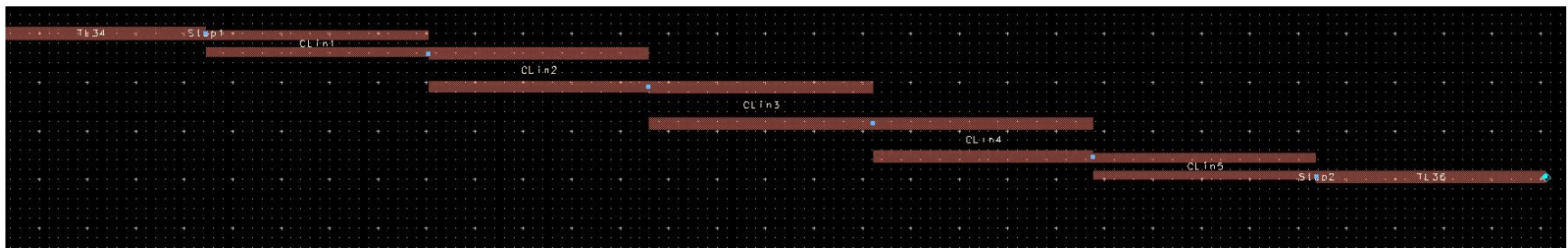
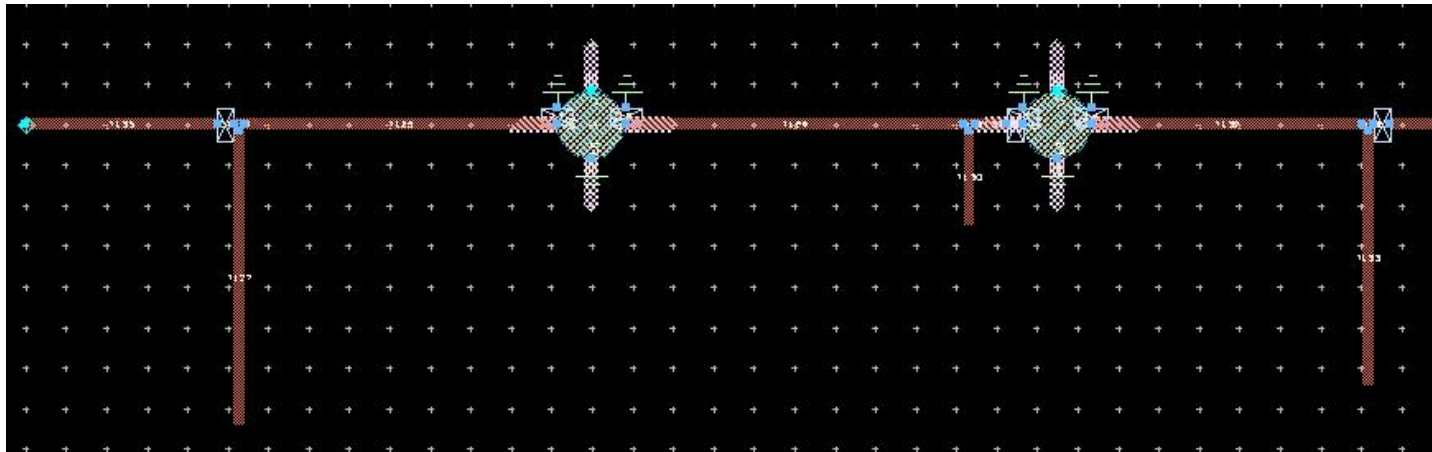
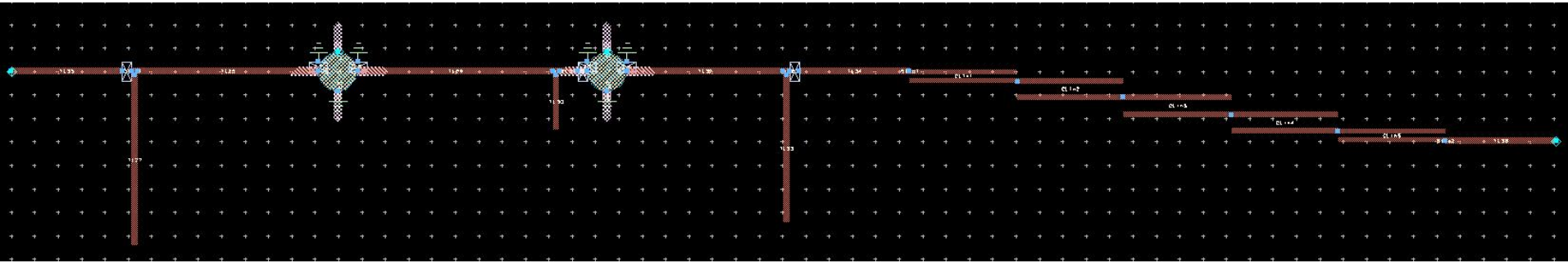


Layout (Example)

- Temporary replacement of the transistors and lumped elements (LC) with elements for which ADS has case information



Layout (Example)



Contact

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- rdamian@etti.tuiasi.ro